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FEASIBILITY STUDIES OF AN ON-LINE
IDENTIFICATION TECHNIQUE

A thesis submitted for the degree
of Doctor of Philosophy

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Summary.

This thesis is concerned with the study of a non-sequential identification technique, so that it may be applied to the identification of process plant mathematical models from process measurements with the greatest degree of accuracy and reliability.

In order to study the accuracy of the technique under differing conditions, simple mathematical models were set up on a parallel hybrid computer and these models identified from input/output measurements by a small on-line digital computer.

Initially, the simulated models were identified on-line. However, this method of operation was found not suitable for a thorough study of the technique due to equipment limitations. Further analysis was carried out in a large off-line computer using data generated by the small on-line computer. Hence identification was not strictly on-line.

Results of the work have shown that the identification technique may be successfully applied in practice. An optimum sampling period is suggested, together with noise level limitations for maximum accuracy.

A description of a double-effect evaporator is included in this thesis. It is proposed that the next stage in the work will be the identification of a mathematical model of this evaporator using the technique described.

I wish to thank Dr. H. Bay for his criticisms

of the technicians who helped

me during the course of this work.

A paper, entitled "A study of an on-line identification technique", and based on part of the work presented in this thesis, has been accepted for presentation at an I.Ch.E./B.C.S. Symposium to be held in Nottingham in September, 1971. The title of the Symposium is "On-line Computer Methods relevant to Chemical Engineering."

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Chapter 1

1.1 Introduction.

Since the early part of the 20th Century increasing use has been made of measuring instruments and automatic controllers for the control of industrial processes (43). Industrial process automation has been concerned with the measurement and control of such variables as pressure, temperature, level and flow. These individual controllers were grouped into control centres where the human operator was provided with indicating equipment, high and low level alarms and recording equipment.

Control system design procedures have been generally based on the use of the complex function theory of mathematics. These procedures were 'borrowed' from electrical circuit theory and were essentially for the analysis of single input, single output linear systems. They include the use of the Laplace transform for problem solution and Bode diagrams, Nyquist diagrams and Root locus plots for stability analysis (44).

Due to the nature of the analogue controllers used almost exclusively up until comparatively recently, the form of the controllers has been limited to the well known PID controller. (Proportional-Integral-Derivative). These analogue controllers have generally been pneumatic in operation.

1.2 Application of computers and electronic equipment for control.

Early in the 1950's the first electronic control instruments were introduced, and at this time it was predicted that there would be a steady decline in the use of pneumatic controllers. Typically, 1965 was seen as the crossover point when the use of electronic controllers would exceed 50% of total (45). This crossover point has still not been reached, primarily due to the higher cost of electronic controllers and also to the fire hazards encountered in the use of electronic equipment in flammable atmospheres.

At this time interest began to arise in the use of digital computers for data-logging applications. In this case the computer was

used merely as a recording instrument, logging signals from various measuring instruments. Controllers were still pneumatic, and electronic signals for the computers were obtained from pneumatic/electronic converters. Notice that the computer was now being used on-line; in other words it had to keep pace with the plant whose operation it was monitoring.

Interest in the use of data-logging systems was soon superseded by the desire to use computers for closed-loop control. The first recorded use of a closed loop installation went on stream at the Texaco, Port Arthur refinery in the U.S.A. in 1958 (45). This system used an RW 300 supervisory computer to operate the set points of pneumatic controllers. Since this time many applications of closed-loop computer control have been made.

1.3 Methods of computer control.

In modern computer control applications, a hierarchical system of control is generally used. Starting with the process, the first requirement is for control of the type normally achieved using analogue PID controllers, whilst the second is for control of set points, the set points being computed from a steady state plant model according to some production schedule.

These two requirements are usually carried out separately. Individual loop control is carried out by analogue controllers, or by a small, relatively unsophisticated control computer. The computer software would generally be at Assembler language level, i.e. high efficiency but high implementation cost. The set points are computed using a more sophisticated high level language program in a considerably larger computer, this computer being called the supervisory computer.

In cases where the supervisory computer is controlling analogue controller set points, this is termed supervisor-set-point-control, or S.S.P.C. Where a small computer is used to carry out the functions of analogue controllers, the term direct digital control, or D.D.C. is used.

1.4 Justification for using computer control.

The use of computer control cannot be justified as an economical alternative to the use of analogue controllers, and justification for control computers is rarely based on this proposition. The advantages of using computers on-line may be summarised as follows (46):

- (1) The speed of the computer allows it to collect far more data about the process from measuring instruments than standard recording equipment.
- (2) Its high degree of resolution allows it to read such data far more accurately. This accuracy is, of course, limited by the accuracy of the measuring instrument itself.
- (3) Its large memory allows the computer to accumulate far more data for comparison and analysis.
- (4) Its calculating power and speed allow it to use complex relationships instead of individual items of data as the bases for decisions.
- (5) It can be provided with confidential cost and price data and management directives which cannot with impunity be made available to human operators.
- (6) The computer can be provided with far more facts about the relationships between process variables.

The principal justification for a control computer may therefore be seen to be a far greater knowledge of the process being controlled and considerably superior control thus being achieved.

1.5 Impact of control computers on control theory.

Until the advent of computers, there was little need for the development of any control theory further than that already mentioned. However, once on-line computers had arrived, workers began to take a closer look at the problem of controlling complex processes.

The theory used until this time had been developed for simple linear processes. Chemical plants, on the other hand, are generally

multivariable, non-linear and time-varying processes; multivariable due to the many inputs and outputs of the system; non-linear due to, for instance, the presence of non-linear flow characteristics and reaction rates; and time-varying due to the effect of fouling on the operation of heat exchangers and furnaces, ageing of catalysts in catalyst beds, day-to-day variation in ambient temperature and wind effects, etc.

Modern methods of analysis at present being developed to cope with the problems outlined above include the mathematical description of the process in state variable form (47); the use of the second method of Lyapunov to study stability (48); the development of methods to identify plant models, discussed later by the author in detail; methods of control system design for multivariable systems utilising a classical mechanics approach (49), and the Inverse Nyquist Array (50); and optimisation techniques developed by Bellman and Pontryagin (51).

Given the techniques outlined above, however, computer control is at present still principally based on the approaches mentioned earlier for simple systems. Reasons for this are manifold. Possibly the most important reason for the retention of PID controllers is the familiarity of present day plant operators with them. Use of more sophisticated control algorithms requires a considerable amount of retraining, which is expensive.

Modern Control theory is still very much in its infancy at present. Future years will probably show a marked swing towards the use of more sophisticated control methods as more processes come under computer control, and more experience is accumulated. These trends will be dependent to a certain extent on labour costs, but if the present increase in labour costs is continued, the trends will be accelerated.

1.6 Implementation of computer control on existing plant.

In general most computer control applications have been on existing plant. It is useful at this stage to consider how best a possible computer control application may be approached.

The first problem to be faced before any computer is purchased is that of establishing a relevant steady-state mathematical model for the plant. From this mathematical model studies can be made to establish the cost-sensitive areas of the process, where the most likely gains are to be made from computer control. Apart from the question of maximising profit through close control of the cost-sensitive process variables, other aspects can be considered at this stage. These are the identification of the areas of the process where control is difficult for practical reasons, areas of the process where labour costs can be reduced by the use of a control computer and areas where close control is required due to the hazardous nature of the process being controlled.

Having established the areas of the process where computer control will be introduced, the next stage is the establishment of dynamic models for these areas. From these dynamic models, simulation studies and the application of modern control techniques will reveal optimal control configurations.

The identification of a dynamic model can be separated into two parts. The first is the development of the structure of the model, or the mathematical form of the relationships between process variables. These structures can be developed from the application of the theory of the process under consideration, or may be more simple approximating forms. The complexity of the model will depend upon the use to which it is going to be put.

Having established the structure of the model, the next stage is to determine the values of the model parameters, such that the model response corresponds as closely as possible with the response of the process under consideration. Techniques for computing the values of these parameters are known as identification techniques. The model parameters are computed from a knowledge of the input and output characteristics, deduced from input/output data for the process under consideration. Thus from data taken from the process itself, accurate

models can be established which are essential for sound control system design. Given this control system design, computer control can be implemented with excellent chances of success.

The identification of the dynamic model is of considerable importance, as can be seen, and a great deal of effort is currently being put into developing new identification techniques. Not many cases of their actual implementation have been reported, however.

1.7 Other uses of process models.

In the identification of the plant model in the case above there may well be time-varying process parameters, as have been discussed previously. Thus it may well be necessary to continually update controller settings to give optimal control as the system parameters vary. One way of doing this may be to continually update the process model using a rapid identification technique, and hence continually recompute the optimal controller settings. Implementation of such schemes have been reported (52, 53).

The identification of more sophisticated models is a necessity if more modern control techniques are to be implemented. From these models optimal control trajectories can be computed by the use of such techniques as dynamic programming or Pontryagin's principle.

1.8 Implementation of identification techniques.

The greatest problem in the application of identification techniques to real plant is the requirement that such a plant be disturbed as little as possible from its normal operating conditions. This is to ensure that no off-specification product is produced, and that production schedules can be adhered to.

Methods of identification attempt generally to use noisy signals inherent in large plant operation as forcing functions. Obviously a dynamic model cannot be identified if the process is completely stationary. Other methods use normal operating condition changes made by the supervisory computer or the operators. A third approach is to add pseudo-random noise with known characteristics to the system inputs.

All these approaches have their uses.

1.9 Analysis of identification technique behaviour.

Before an identification technique can be reliably used on real plant, it is necessary to know the effect on the accuracy of the technique of such considerations as noise, sampling period, sample size, etc. Little has been reported in the literature about the analysis of any identification technique with this thought in mind. A few authors have reported the study of the use of identification techniques for particular process plant models.

The author has approached this problem in what he considers as realistic a way as possible. Methods have been developed to study the behaviour of a particular identification technique using simulated process models. At the same time work is being carried out in the Department of Chemical Engineering to commission on-line instrumentation for a pilot scale double-effect evaporator and it is upon this plant that the identification technique will be tested in future work.

Originally these two projects were initiated as a single project by the author. However, the work involved was too extensive for one project and so it was split, the author continuing with the study of the identification technique. Some details of the evaporator system will be given to show the type of plant to be used as a testbed for the identification technique.

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Chapter 2

The problem of identification can be defined mathematically as follows:

Given a set of equations governing the behaviour of a system,

$$\dot{\underline{x}}(t) = \underline{f}\{\underline{x}(t), \underline{d}(t), t\} + \underline{b} \underline{w}(t)$$

$$\underline{y}(t) = \underline{g}\{\underline{x}(t), t\} + \underline{c} \underline{v}(t)$$

where $\underline{x}(t)$ are the system states; $\underline{d}(t)$ are the state parameters defining the model, which, it is assumed, may vary with time; $\underline{b}, \underline{c}, \underline{f}$ and \underline{g} are linear or non-linear transition functions; $\underline{y}(t)$ are the system outputs; $\underline{w}(t)$ are the uncontrolled system inputs and $\underline{v}(t)$ are measurement noises.

It is required to estimate $\underline{d}(t)$, given a knowledge of $\underline{y}(t)$ and $\underline{w}(t)$.

In certain cases estimation of $\underline{x}(t)$, the system states, is also possible.

2.1 Classification of identification techniques.

Identification techniques can be split into two distinct groups, sequential and non-sequential. In sequential estimation techniques, the computation is initiated by using trial initial values of the parameters, and every additional set of observations is used to update these values. As the number of observations increases, obviously the accuracy of prediction of the parameters increases.

Non-sequential estimation methods rely on taking a number of observations of $y(t)$ at different times and then effectively fitting a best-fit curve to the dynamic response of the system.

Apart from the classification of estimation techniques into sequential and non-sequential types, different techniques are required for linear and non-linear systems. Hence identification techniques can be subgrouped into 4 different classes.

- (a) Linear, non-sequential techniques.
- (b) Non-linear, non-sequential techniques.
- (c) Linear, sequential techniques.

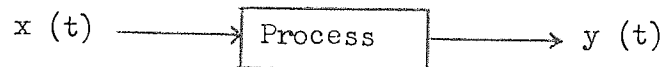
(d) Non-linear, sequential techniques.

2.2 Linear, non-sequential techniques.

Correlation Analysis:

The principal technique used in this group is that using correlation analysis. Briefly, the method is derived as follows (4):

Given a linear process with an input $x(t)$ and an output $y(t)$



The relationship between input and output is

$$y(t) = \int_{-\infty}^{\infty} h(\tau) x(t-\tau) d\tau \quad (\text{Superposition Integral}) \quad 2.2.1$$

where $h(\tau)$ is the impulse response of the process.

In terms of frequency the above may be written

$$Y(w) = H(w) X(w).$$

Here $H(w)$ is the process frequency response or transfer function and $Y(w)$ and $X(w)$ are the Fourier transforms of $y(t)$ and $x(t)$.

It can be shown using the superposition integral that:

$$\phi_{xy}(t) = \int_{-\infty}^{\infty} h(\tau) \phi_{xx}(t-\tau) d\tau \quad 2.2.2$$

and hence,

$$\Phi_{xy}(w) = H(w) \cdot \Phi_{xx}(w).$$

ϕ_{xx} and ϕ_{xy} , and Φ_{xx} and Φ_{xy} are correlation

functions and spectral density functions respectively and are related to $x(t)$ and $y(t)$ as follows:

$$\begin{aligned} \phi_{xx}(\tau) &= \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T x(t) x(t+\tau) dt \\ \phi_{xy}(\tau) &= \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T x(t) y(t+\tau) dt \\ \Phi_{xx}(w) &= \frac{1}{2\pi} \int_{-\infty}^{\infty} \phi_{xx}(\tau) e^{-i\omega\tau} d\tau \\ \Phi_{xy}(w) &= \frac{1}{2\pi} \int_{-\infty}^{\infty} \phi_{xy}(\tau) e^{-i\omega\tau} d\tau \end{aligned}$$

On inspection of equation 2.2.2 it can be seen that it has the form of the superposition integral, given in equation 2.2.1. If it were possible to find a forcing function whose autocorrelation function had the shape of a unit impulse, then the impulse response of the system would be given by $\phi_{xy}(t)$. As it happens, the auto-

correlation function of white noise is an impulse, so driving the system with white noise allows the estimation of the impulse response directly from the cross-correlation function.

There are two principal drawbacks to this technique. First of all, the solution gives either the impulse response of the system as a function of time, or the frequency response as a function of frequency. Both are sets of numbers from which system parameters have to be estimated indirectly. Secondly, to obtain reasonable estimates of the impulse or frequency response, the system under consideration must be disturbed with white noise, or noise with characteristics similar to white noise. White noise has the characteristic that it excites all frequencies of the system with an equal amplitude. In practice it is virtually impossible to obtain, but near approximations are made with the Random Telegraph Signal and the Pseudo-random binary chain code. Hutchinson and Shelton (5) have studied the application of the above technique to a refinery distillation column and compared the use of the Random Telegraph Signal with the Pseudo-random binary chain code. The latter signal was found to be more advantageous.

Woodburn, King and Everson (6) have used the technique to study the estimation of process parameters in packed towers where mixing is taking place. The design of test signals is discussed.

Least Squares Techniques.

Least Squares methods have been suggested and used by Bray, et al (7) and Chien and Aris (8).

Bray, et al applied the technique to the model-making of a Water-gas shift converter, whilst Chien and Aris applied it to a batch reactor.

A linear predictor of the form

$$y(t) = \sum_i b_i x_i(t)$$

is used, where $y(t)$ is the system output and $x_i(t)$ are the system inputs.

Values of b_i are required to minimise the sum of the squares,

$$S = \sum_{n=0}^{t-1} \left\{ y(t-n) - \sum_i b_i x_i(t-n) \right\}^2$$

More recent observations were weighted more heavily than older observations by using a weighting function of exponential form.

The drawback of this technique is the limitation on the form of the mathematical model of the system, which is constrained to be a linear algebraic relationship between the system outputs and the various inputs.

Another approach to this problem is to use a least squares curve-fitting technique in the Laplace domain. The effect of transforming systems of linear differential equations is to convert them to sets of algebraic equations, to which least squares curve-fitting can easily be applied. A numerical technique must be used to transform the known values of input and output as functions of time to values of input and output as functions of the Laplace operator, s . Such techniques have been suggested by Bellman, et al (9) and Carr, et al (10,27). The difference between the techniques used by the two authors is only in the type of numerical transformation technique used. The author has utilised that suggested by Bellman in his work. A review of numerical Laplace Transform techniques is given in a later section.

2.3 Non-linear, non-sequential techniques.

Quasilinearisation.

The estimation of system parameters in more general systems, including non-linear systems, can be carried out using quasilinearisation.

This method has been used by Bellman, et al (11), Lee (12) and Gavalas & Seinfeld (13) to determine reaction rate constants from kinetic data.

Consider the system described by the equations,

$$\dot{\underline{x}} = \underline{f}(\underline{x}, \underline{a}, t),$$

$$\underline{x}(0) = \underline{a}$$

2.2.3

where \underline{a} is a vector of unknown system parameters and \underline{x}

are the system states. Given a set of observed values of the output b_i , taken at times t_i , it is required to choose the $\underline{\alpha}$ to minimise the sum of the squares.

$$S = \sum_{i=1}^N \{ x_i(t_i) - b_i \}^2$$

Combining the $\underline{\alpha}$ with the \underline{x} into a new vector, \underline{z} , equation 2.2.3 may be written

$$\dot{\underline{z}} = \underline{f}(\underline{z}, t), \quad \underline{z}(0) = \underline{z}_0 \quad 2.2.4$$

and

$$S = \sum_{i=1}^N \{ z_i(t_i) - b_i \}^2 \quad 2.2.5$$

Using some arbitrary starting values for the unknown system parameters, $\underline{z}(0)$, equation 2.2.4 is now integrated to give the solutions of the equation at t_i , the observation times.

Equation 2.2.4 is linearised about $\underline{z}^{(0)}$, the solutions of 2.2.4, to give

$$\dot{\underline{z}}^{(1)} = \underline{f}(\underline{z}^{(0)}, t) + \left[\frac{\partial \underline{f}}{\partial \underline{z}} \right]_{\underline{z}^{(0)}} \{ \underline{z}^{(1)}(t) - \underline{z}^{(0)}(t) \}$$

This gives a linear ordinary differential equation in $\underline{z}^{(1)}$, the new estimate of the unknown system parameters.

This can be solved analytically to give a general solution consisting of a particular solution plus n homogeneous solutions, where n is the number of states included in vector \underline{z} . At $t = 0$ these solutions will give the unknown system states.

These solutions can be substituted in equation 2.2.5 and hence the new estimates of the unknown system states can be determined by solving the equations

$$\frac{\partial S}{\partial \underline{\alpha}_i} = 0, \quad i = 1, 2, \dots, N.$$

This process can be repeated until all the unknown system states converge within set limits.

Problems arising with the use of this technique are suggested by Seinfeld (14) as:

(a) Non-convergence due to poor initial estimates of the unknown parameters.

(b) Difficulty in the solution of the algebraic equations because of ill-conditioning.

It is difficult to determine if either of these points will be important in a particular problem before actual computation is carried out.

Donnelly & Quon (15) have proposed a modification of the algorithm to improve the convergence characteristics. However, it appears to make the algorithm even more complex than it already is. The complexity of the algorithm is possibly its greatest drawback. However, it is still a useful technique for identifying non-linear equations.

A method termed the method of parameter influence coefficients has been found by Allison (16) to be identical to quasilinearisation, apart from procedural differences. For a set of system equations in state variable form, quasilinearisation is advantageous, whilst for other forms of the system equations the method of parameter influence coefficients should be used.

2.4 Linear, sequential estimation techniques.

Linear sequential estimation techniques are developments of a digital filtering technique suggested by Kalman (17). This is basically a technique for obtaining accurate estimates of system states from noisy measurements. The system parameter estimation problem is tackled by embedding them in the system state equations as system states. Kalman's estimator constrained the uncontrolled system inputs and the measurement noise to be Gaussian in form. The estimator is used to identify parameters when the system under consideration is disturbed by random noise only. Kalman deduced the estimator using Hilbert space theory and developed the estimator for the discrete form of the system equations. This form of the problem emphasises a statistical approach to the development of the estimator.

Kalman and Bucy (18) extended this work to the continuous form of the system equations and Cox (19) deduced the estimator using

dynamic programming.

Another approach to the sequential estimation problem was made by Bellman, et al (20) and Detchmندی and Sridhar (21), who made no assumptions about the form of the disturbances and applied a more straightforward least squares approach. They developed this approach for continuous systems, while Sridhar and Pearson (22) developed it for discrete systems. Gavallas and Seinfeld (23) have applied the filter proposed by Detchmندی & Sridhar to the estimation of states and kinetic parameters in a tubular reactor with catalyst decay.

Sequential estimation techniques have distinct advantages for the estimation of parameters in noisy systems, however, the estimators are recursive in form and require a considerable number of matrix manipulations. This makes them considerably slower than non-sequential techniques, which is a distinct disadvantage in industrial systems where time is at a premium due to the large amount of house-keeping done by the on-line computers.

2.5 Non-linear, sequential techniques.

Coggan & Noton (24) have developed a rigorous treatment of the non-linear sequential estimation case utilising a local quasi-linearisation technique. The method of Detchmندی & Sridhar (21) utilises a global quasilinearisation technique and is more approximate than that of Coggan & Noton.

2.6 Estimation Techniques for distributed parameter systems.

Methods have been developed by Seinfeld (25) and Tzafestas and Nightingale (26) for the estimation of parameters in distributed parameter systems. However, they are very complex and not really practical for on-line work.

2.7 Numerical Laplace Transform Techniques.

As the author's work centres around the use of a numerical Laplace Transform technique, it is appropriate to give a review of the literature appertaining to this subject.

Numerical Laplace Transform techniques can be divided into two types, one of which is concerned with the calculation of $f(t)$, given a knowledge of $f(s)$, its Laplace Transform; and the other which is concerned with the calculation of $f(s)$, given values of $f(t)$ in the time domain.

The author's prime interest is with the latter type, knowledge of the values of $f(s)$ being required from known values of $f(t)$ such that identification can be carried out in the Laplace domain.

For completeness, the first type of numerical transform techniques will be briefly reviewed before a more detailed study of transform techniques of the second type is carried out.

Early work done on the numerical inversion of the Laplace Transform was based on a formula suggested by Widder (28) from a general inversion formula proposed by Post (29). This formula represents the general case of a set of inversion methods suggested by Alfrey (30), ter Haar (31) and Schapery (32). Cost (33) has reviewed these methods for use in some problems of visco-elastic stress analysis. The general formula is based on the shifting property of the Dirac delta function, and may be written,

$$f(t) = \lim_{n \rightarrow \infty} \left[\frac{(-1)^n s^{n+1}}{n!} \frac{d^n}{ds^n} f(s) \right]_{s = \frac{n}{t}}$$

Erdélyi (34) has derived inversion formulae giving $f(t)$ as a series of orthogonal functions, where the coefficients of the expansion are finite linear combinations of the values assumed by $f(s)$ at a set of equidistant points.

Salzer (35, 36, 37) has studied the use of quadrature formulas for the solution of the inversion integral,

$$f(t) = \frac{1}{2\pi i} \int_{c-i\infty}^{c+i\infty} f(s) e^{st} ds.$$

Coming now to the estimation of $f(s)$, given $f(t)$, Bellman (38) has developed an approach utilising a Legendre-Gauss quadrature approximation for the solution of the integral,

$$f(s) = \int_0^{\infty} e^{-st} f(t) dt$$

Apart from obtaining $f(s)$ from a knowledge of $f(t)$, the inverse problem is also solved, giving the method a marked advantage over other transform methods. Carr & Cook (39, 42) have developed similar methods utilising slightly different quadrature formulae. Luke (55) has reviewed the original work by Bellman, and includes some useful references on numerical Laplace Transform techniques.

A drawback of the inversion formulae developed by Bellman is that $f(t)$ and $f(s)$ are only obtained for a restricted number of non-equidistant points. However, Piessens (40) has developed a method for extending the number of values of $f(t)$ obtained from inversion of $f(s)$ and Felts & Cook (41) have derived a method for extending the range of the estimated values of $f(s)$ from a knowledge of $f(t)$.

Bellman's method may be summarised as follows:

The Laplace Transform is defined:

$$f(s) = \int_0^{\infty} e^{-st} f(t) dt \quad 2.7.1$$

Introducing a new variable of integration for the independent variable, $r = e^{-t}$,

$$f(s) = \int_0^1 r^{s-1} f(-\ln r) dr \quad 2.7.2$$

The above equation can be approximated by a Gaussian quadrature formula, giving,

$$f(s) = \sum_{i=1}^N w_i r_i^{s-1} f(-\ln r_i) \quad 2.7.3$$

where the w_i are weighting functions.

Bellman computes the roots, r_i , and weights, w_i in the above equation using the Legendre polynomials. The roots and weights are tabulated (38) for $N = 3$ to $N = 15$, as are the values of $t_i = -\ln r_i$. The matrix $w_i r_i^{s-1}$ is tabulated (3) as a square matrix for values of N from 3 to 15. The Tables for $w_i r_i^{s-1}$ and t_i are shown in Appendix V.

The numerical inversion of the Laplace Transform by Bellman will not be considered here, except to say that the method generates an inversion matrix which is ill-conditioned.

A point worth noting, however, about the numerical transform technique, is the use of time scaling factors.

Consider a function $f(at)$, where a is a time scale factor, then

$$\begin{aligned} \mathcal{L}\{f(at)\} &= \int_0^{\infty} e^{-st} f(at) dt \\ &= \frac{1}{a} \int_0^{\infty} e^{-\frac{st}{a}} f(t) dt = \frac{F\left(\frac{s}{a}\right)}{a} \end{aligned}$$

Introducing the numerical approximation for $F\left(\frac{s}{a}\right)$,

$$\begin{aligned} F\left(\frac{s}{a}\right) &= a \sum_{i=1}^N w_i r_i^{s-1} f(-a \ln r_i) \\ &= a \sum_{i=1}^N w_i r_i^{s-1} f(at_i). \end{aligned}$$

Note that the transform has been time-scaled; however the matrix $w_i r_i^{s-1}$ is not affected.

2.8 Conclusion.

Considering the identification techniques discussed, obviously the techniques giving the largest amount of information are the sequential identification techniques. However, these require a great deal of computation time.

Opting for an identification technique which gave promise of being economical in both accuracy and computer time, the author chose to study the possibilities of identification in the Laplace domain using a numerical Laplace transform technique. This technique has the added advantage that many chemical engineers are familiar with the Laplace transform.

Choice of the particular Laplace Transform technique to be used was limited, Bellman's being chosen as the coefficients of the formula were well documented.

Non-linear processes to be identified would be approximated in their operating region by linearised models.

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Chapter 3

In this chapter the apparatus used by the author in his work is discussed. The basic items of equipment used were a double-effect evaporator, an E.A.L. MDP-200 data-logging system, an E.A.L. HY-48 parallel hybrid computer and a PDS.1020 digital computer. The author also had access to an I.C.L. 1905 digital computer. These items of equipment will be discussed in turn and the connections between the various items of equipment will be discussed.

Photographs of the equipment are shown in figures 3.3 and 3.4.

3.1 The double-effect evaporator.

The evaporator system, consisting of a climbing film effect followed by a forced circulation effect, was purchased from Kestner-A.P.V. Ltd. and is capable of evaporating 300 lbs/hr. of water. A line drawing of the evaporator system is given in fig. 3.1.

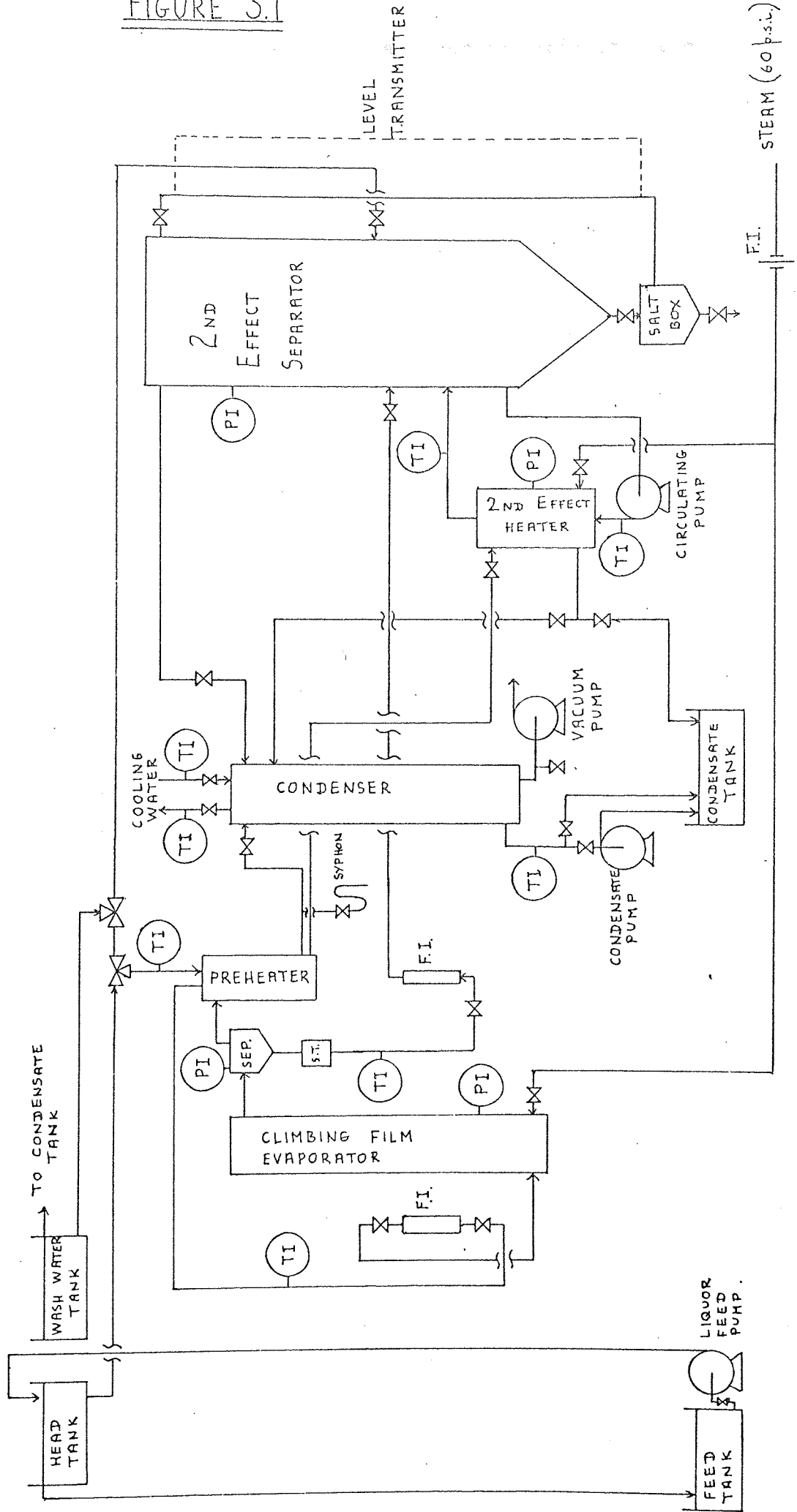
The weak liquor to be concentrated is prepared in the weak liquor feed tank. From here it is pumped up to the weak liquor head tank. From here it flows under gravity head to either the preheater of the 1st effect, or to the 2nd effect separator. The two effects can thus be operated separately or in series. Operating the two effects in series will be considered first.

Weak liquor passes through the preheater, where it is heated by vapour from the first effect separator. It then passes through a rotameter to the base of the climbing film evaporator.

The climbing film evaporator is heated on the shell side by steam supplied from an external source. Condensed steam is removed through a steam trap to the condensate tank. The weak liquor is partially evaporated in the climbing film tubes and the mixed phase passes to the first effect separator.

From here the vapour passes to the preheater; any vapour left un-condensed in this unit can be passed to the condenser or the shell side of the 2nd effect heater as desired. The liquor, now in a concentrated form, passes to the 2nd effect separator.

FIGURE 3.1



DOUBLE EFFECT EVAPORATOR (MODIFIED)

Liquor in the 2nd effect separator is circulated through a heat exchanger, where further heat is added. On return to the separator, vapour flashes off under the decreased pressure. This vapour then passes to the condenser. Any solids precipitating can be collected in the salt-box and then drained.

Heat to the 2nd effect heater can be supplied either by steam from the external steam supply or uncondensed vapour from the 1st effect preheater. Generally in the latter case additional steam is necessary to keep the 2nd effect separator liquor level steady.

The system can be run under vacuum or at atmospheric pressure, vacuum being drawn on the condenser.

When running the first effect alone, concentrated liquor is collected in the 2nd effect separator, or the line to the 2nd effect separator is broken and an S-bend syphon attached under the steam trap. Liquor can then be collected separately. When working under vacuum this latter alternative is not possible.

The 2nd effect can be run alone under vacuum or at atmospheric pressure utilising the weak liquor supplied directly from the feed tank.

3.1.1 Instrumentation.

Rotameters were supplied on the liquor feed lines to both effects, but not on the liquor line from the 1st effect to the 2nd effect. Thermocouples were supplied to monitor the following temperatures:

Preheater inlet.

Climbing film evaporator inlet.

1st Effect separator outlet.

2nd Effect heater inlet.

2nd Effect heater outlet.

Condenser cooling water inlet.

Condenser cooling water outlet.

Condensate from the condenser.

There were Bourdon pressure gauges to monitor the following pressures:

Climbing film evaporator shell-side pressure.

2nd Effect heater shell-side pressure.

2nd Effect separator pressure.

The thermocouple readings could be monitored by a self-compensating potentiometer on a remote control panel. The Pressure gauges and the pump controls were also positioned on this control panel.

3.1.2 Modifications.

The only modifications made of any importance were the addition to the plant of a number of on-line measuring instruments. The rotameter on the liquor feed line to the climbing film evaporator was removed and replaced by a Fischer-Porter variable area flowmeter with an output signal in the range 4-20mA, and a similar instrument was fitted on the line to the 2nd effect separator. The reason for the choice of variable area flowmeters was in both cases the low flows encountered, together with the low permissible pressure drop across the instruments. This was particularly so in the case of the flowmeter between the two effects, where the allowable head was measured in inches WG.

An orifice plate was inserted in the steam line to the evaporator and the steam flow monitored by a Fischer-Porter differential pressure transducer, again with a 4-20mA output signal.

The level of liquor in the 2nd effect separator was monitored by differential pressure transducer, the take-off points being as shown in fig. 3.1.

The 3 pressures monitored by the Bourdon gauges were also monitored by Bell & Howell pressure transducers, each giving a 0-40 mV output. An additional transducer was installed to monitor the pressure in the 1st effect separator.

3.2 The E.A.L. HY-48 parallel hybrid computer.

This is a standard 10 volt parallel hybrid machine, consisting of an analogue section with a complement of:

- 34 D.C. Amplifiers.
- 10 Track/Store Amplifiers.
- 14 Integrators.
- 30 Manual set Potentiometers.
- 30 Servoset Potentiometers.
- 4 Bipolar multipliers.
- 1 X^2 D.F.G.
- 5 V.D.F.G.'s.
- 5 Manual function switches.
- 6 Comparators.
- 12 D/A switches.
- 6 D.P.D.T. switches.

and a logic section with a complement of:

- 2 Clock Timers.
- Integrator logic controls.
- T/S Amplifier logic controls.
- Comparator logic outputs.
- D/A switch logic controls.
- D.P.D.T. switch logic controls.
- 4 General purpose registers.
- 2 Down-counters.
- 4 Function switches.
- 2 Monostables.
- 2 Differentiators.
- 20 2-input AND gates.
- Logical mode control.
- Logic '1' and logic '0' sources.

The logic section was driven from a digital clock with a variable frequency up to 1 Mc/s. The Analogue and logic sections could be controlled by separate Mode switches, or from the logic section of the computer. Trunk lines existed on both the logic and analogue sections for the transmission of signals to other items of equipment via plugs in the back of the machine. Trunk lines in the analogue section of the machine were used to transmit signals through wiring from the analogue section to the MDP-200 data logger, discussed in a later section.

3.3 The PDS 1020 digital computer.

This was a first generation digital computer with a 4.6 μ s cycle time delay-line memory system. It had a 4 K word memory, each word consisting of 16 bits and sign. There were seven hardware registers: the accumulator, next instruction register, present instruction register, word length register, index register, link address register and sign register. Arithmetic was decimal, and included hardware multiply and divide. Addressing and commands were coded in hexadecimal form.

For program control there existed 4 standard sense-switches and 10 macro switches. These latter switches could be used to force manually a jump to different sections of program. Input could be effected by on-line typewriter, keyboard or paper tape reader and output via typewriter or paper tape punch. There were also facilities for the parallel input and output of information to remote devices, in this particular case a data-logging system.

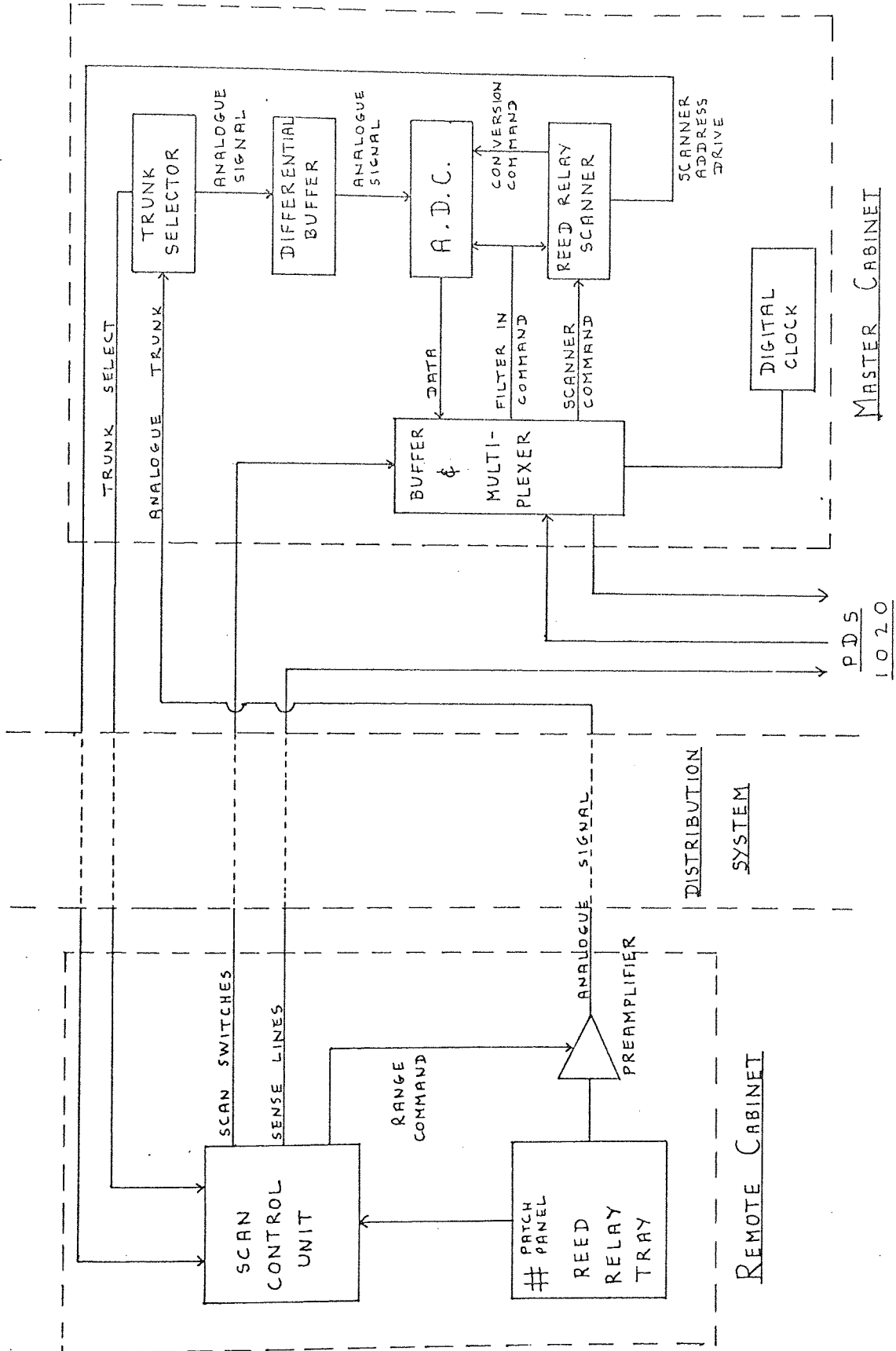
Programming was implemented through an Assembler language package.

3.4 The E.A.L. MDP 200 Data logging system.

This system was used under the control of the PDS. 1020 to digitise analogue signals and transfer the resulting numbers into the PDS. 1020 for processing. A diagrammatic sketch of the system is shown in fig. 3.2.

The data-logging system was made up in two sections. The

FIGURE 3.2



M.D.P. 200 DATA LOGGING SYSTEM

first section, housed in the master cabinet which was situated near the computer, consisted of the Buffer and Multiplexer, Digital clock, Reed relay scanner, Analogue to Digital converter, Differential buffer and Trunk selector. The second section, housed in the remote cabinet which was situated near the apparatus from which signals were to be monitored, consisted of the Scan control unit, Reed Relay tray, Gain control patch panel and the Preamplifier. The remote cabinet also housed a de la Rue Zerac Ice-point Reference chamber for thermocouple inputs; scan switches, which will be discussed later; and 4 sense lines, which had an identical action to the sense switches on the PDS.1020.

Operation of the M.D.P. 200 was initiated by the output of a command from the PDS. 1020 down the parallel output lines to the Buffer & Multiplexer unit. This unit acted as a buffer and translator between the PDS. 1020 and the MDP. 200. This command could refer to the digital clock, a particular channel on the reed relay tray or the scan switches.

The readings from the digital clock were in hours and minutes, or in seconds and $\frac{1}{10}$ seconds, depending on the command used. The digital clock could be used in two modes, the synchronous mode or the asynchronous mode. The asynchronous mode was as above.

In the synchronous mode readings of the digital clock were controlled by a timer, which could be manually set to multiples of $\frac{1}{10}$ second. In this mode the digital clock could only be read at the end of each timing period set by the timer. At all other times the MDP. 200 was held up until the end of the timing period. In this way sampling times could be controlled from the PDS. 1020.

The Scan switches were a set of four manual digi-switches on the remote cabinet. Through these, decimal numbers could be set up from the remote cabinet and read into the PDS. 1020. In conjunction with the sense-lines they could be used for remote program control.

Readings from the digital clock and scan switches were made

directly through the Buffer and Multiplexer. The reading of analogue input channels was more complex.

From the Buffer and Multiplexer the command to read a particular channel was directed to the Reed relay scanner. Filtering of the particular channel signal could be carried out remotely through a switch on the master cabinet, or through programming. From the Reed relay scanner a signal was sent to the scan control unit to activate the Reed relay on the channel under consideration.

The incoming signal was passed to the preamplifier, where any required magnification of the signal took place. Magnifications of 1, 10, 100 or 1000 were possible on the system, the required gain being set through programming or remotely on a patch-panel on the remote cabinet.

Between the remote cabinet and the master cabinet existed a distribution network of screened cabling and junction boxes, in order that the remote cabinet could be situated in any one of three laboratories. The remote cabinet could be plugged into a junction box in any one of the three laboratories and through the distribution system, communicate with the master cabinet.

The logic wiring was duplicated at each junction box but from each junction box, for the purposes of decreasing the effect of noise on the signal, a separate line existed to direct the analogue signal to the Trunk selector in the master cabinet. The Trunk selector was used to identify which junction box the analogue signal was to be routed from.

From the Trunk selector the analogue signal was routed through a Differential buffer to remove the effects of differences in electrical ground level between the remote cabinet and the master cabinet. The analogue signal was converted to a digital signal in the A.D.C. (Analogue/Digital converter) on the receipt of a conversion command from the Reed relay scanner.

The Scanning rate of the system was about 30 channels/sec.

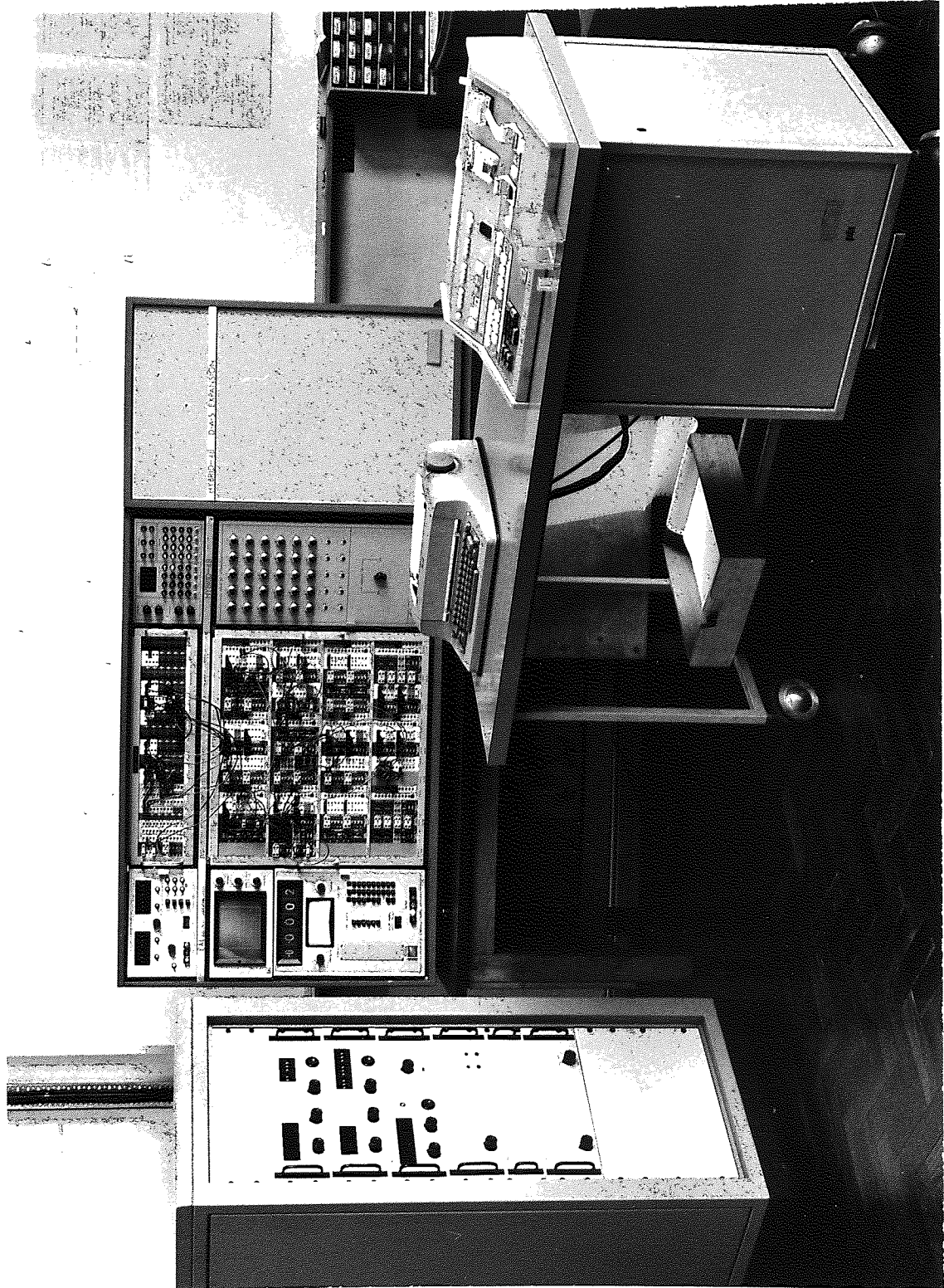
with the filter out and 8 channels/sec. with it in. The difference in scanning rates was due to the settling time of the filter.

3.5 Equipment link-ups used.

The Data-logging system was used to log signals from both the double-effect evaporator and the HY-48. A general program was written to log signals from either apparatus, this program being discussed in Chapter 5.

In addition to the equipment described above, a large I.C.L. 1905 digital computer was used for more sophisticated and complex programming problems. Algol programs analysing data collected and sorted by the PDS. 1020 were processed on this machine.

FIGURE 3.3



Photograph showing, from l. to r., the MDP. 200 Master cabinet, the HY-48 computer and the PDS. 1020 computer.

FIGURE 3.4



Photograph showing the double effect evaporator with the MDP. 200 Remote cabinet in the left background.

• Chapter 4

The estimation technique used by the author will now be presented, together with a discussion of the problems involved in utilising the technique. The methods of analysing the technique will also be discussed.

4.1 The Identification Technique.

The problem may be defined as follows:

Given a multivariable system defined by the following state equations,

$$\dot{\underline{x}}(t) = \underline{f} \{ \underline{x}(t), t, \underline{d} \} \quad 4.1.1$$

where the vector $\underline{x}(t)$ is a vector of the system states including inputs, \underline{d} is a vector of unknown parameters and initial conditions and t is time, it is required to evaluate \underline{d} , knowing $\underline{x}(t)$.

Transforming 4.1.1,

$$s \underline{x}(s) = \underline{g} \{ \underline{x}(s), s, \underline{d} \}$$

This expression defines a set of algebraic equations and may be written,

$$\underline{x}(s) = \underline{G} \{ s, \underline{d} \} \quad 4.1.2$$

Bellman's numerical Laplace transform technique (1) is now utilised to transform $\underline{x}(t)$, which is known. Utilising this technique will introduce errors, as the transforming technique is an approximate one. Further errors may, of course, be introduced by inaccuracies in the measurement of $\underline{x}(t)$ or inaccuracies in the model. Lumping these errors, the following expression can be deduced for the residuals,

$$\underline{e}_s = \underline{x}(s) - \underline{G} \{ s, \underline{d} \} \quad 4.1.3$$

\underline{e}_s are the residual errors for a particular value of s , and $\underline{x}(s)$ are now the numerically transformed system states.

It is required to find the values of the state parameters and initial conditions so that the predicted model fits the data in the best possible fashion. Mathematically, we require to maximise some objective function by a suitable choice of \underline{d} .

For each value of s there is a residual, e_s , hence we can write the Moment Matrix of residuals,

$$\underline{M} = \sum_{s=1}^N \underline{e}_s \underline{e}_s^T$$

where N = the number of observations of $\underline{x}(t)$.

It can be seen that \underline{M} is the sum of the squares of the residuals.

The general objective function to be maximised has the form

$$S(\underline{d}) = \psi(\underline{M})$$

The following objective functions are available (2):

(a) Weighted Least Squares:

$$\psi = -\text{Tr} \{ \underline{Q} \underline{M} \} \quad 4.1.4$$

where \underline{Q} is some non-singular weighting matrix.

(b) Maximum likelihood (errors in $x(s)$ are assumed to be normally distributed with zero mean and known covariance matrix \underline{V}):

$$\psi = -\frac{1}{2} \text{Tr} \{ \underline{V}^{-1} \underline{M} \} \quad 4.1.5$$

(c) Maximum likelihood (\underline{V} is unknown):

$$\psi = -\frac{N}{2} \ln \det \underline{M} \quad 4.1.6$$

where N = No. of observations.

The state parameters may also be subject to inequality constraints,

$$\psi_i(\underline{d}) \leq 0, \quad i = 1, 2, \dots, m$$

These reflect constraints which the parameters may have to satisfy, i.e. chemical rate constants must be +ve, etc.

Obviously the simplest and most rapid evaluation of \underline{d} is through the least squares criterion. The covariance matrix, \underline{V} is not likely to be known, and 4.1.6 would have to be maximised by some iterative optimisation procedure.

Equation 4.1.4 can be translated into the well-known minimisation of the sum of the squares by writing

$$\psi = \text{Tr} \underline{M}$$

\underline{Q} is assumed to be a unit matrix.

Hence d can be found by solving the set of equations,

$$\frac{\partial \psi}{\partial x_i} = 0, \quad i = 1, 2, \dots, m.$$

As the equations are linear, solution of the above is straightforward.

4.2 Implementation.

Time Scaling and sampling interval:

On a closer consideration of Bellman's transform technique, two problems of utilising the method stand out immediately.

Given the numerical Laplace transform of $x(t)$,

$$x(s) = \sum_{i=1}^N w_i r_i^{s-1} x(t_i), \quad s = 1, 2, \dots, N,$$

it can be seen that the times at which the function x is

required to be observed are given by:

$$t_i = -\ln r_i.$$

From tabulations of the values of t_i for various quadrature sizes, completed by Bellman (1) and repeated in Appendix V, it is seen that the values of t_i are unevenly spaced and that they fall within a very limited range numerically. (Maximum range: 5.115372 for a 15 point quadrature formula).

The problem of uneven spacing is a practical one, in that valuable time can be wasted in clocking the sampling interval during run-time on the computer. The problem is simplified by using the smallest computed value of t_i as the basic time unit, all other values of t_i being rounded to the nearest multiple of this smallest value of t_i . The adjustments to the t_i were found to produce a negligible error in the measured variable for the models considered. (see Appendix Id).

Overcoming the limited numerical range of the t_i was carried out using time-scaling techniques. Timescaling can be carried out either in the time domain or the Laplace domain. Consider first time-scaling in the Laplace domain. From Laplace transform theory it can be deduced that if

$$\mathcal{L}\{x(t)\} = \int_0^{\infty} e^{-st} x(t) dt = x(s),$$

then $\mathcal{L} \{ x(at) \} = \frac{x(\frac{s}{a})}{a}$

Hence: $\frac{x(\frac{s}{a})}{a} = \sum_{i=1}^N w_i r_i^{s-1} x(-a \ln r_i)$

or $x(\frac{s}{a}) = a \sum_{i=1}^N w_i r_i^{s-1} x(at_i), s = 1, 2, \dots, N$

Values of $(w_i r_i^{s-1})$ have been tabulated by the author (3), so the above equation may be written:

$$x(s) = a \sum_{i,j=1}^N M_{ij} x(at_i), s = \frac{1}{a}, \frac{2}{a}, \dots, \frac{N}{a},$$

where

$$M_{ij} = w_i r_i^{s-1}, s = j; i, j = 1, 2, \dots, N.$$

Time-scaling in the time domain is done on the state equations themselves and is relatively straightforward. $x(s)$ is computed with no time scaling. The substitution made is $t = kt_r$, where t_r is real time and k is the scaling factor.

Other Factors to be considered.

Having noted the possibilities of varying the sampling interval sizes by time-scaling, a question that arises is what the effect is of time-scale on the accuracy of prediction of the system parameters. It would be imagined that this accuracy of prediction would be related to the spread of observations over the response time of the disturbed system. Part of the work done in this thesis is directed towards a consideration of this relationship.

Other points which have to be considered are:

(a) Effect of signal noise:

Signals coming from remote on-line instruments are often corrupted by noise. The effect of different noise levels on the accuracy of prediction needs to be studied.

(b) Number of observations required:

Obviously the fewer observations it is necessary to make, the faster the speed of estimation. As the calculation of $x(s)$ requires

matrix multiplication, the speed of prediction will be approximately proportional to the square of the number of observations. Signal noise and the order of the state model may well have an effect on the number of observations required for a particular estimation accuracy.

(c) Effect of disturbing signal amplitude:

The effect of the amplitude of the disturbing signals may well have an effect on the accuracy of the predicted parameters. The required amplitude of the disturbing signal may be affected by the noise levels on the state measurements.

Obviously at steady state the system will be unobservable and no parameters can be estimated.

(d) Identification Initiation:

It is necessary to know immediately the system has been disturbed such that the required observations can be made. Some method must be found of monitoring possible disturbing signals. Here it must be pointed out that there will always be a slight error due to the fact that the time of initiation of the disturbing signal will never be known exactly. The error is negligible, however, for systems with large time constants as are found in chemical plant.

(e) Distance-velocity lags:

Work done by the author (3) on the use of the shifting theorem to identify distance-velocity lags by numerical Laplace transform techniques was unsuccessful. Estimates of any distance-velocity lags would have to be made from process measurements before the identification technique could be applied.

4.3 Models Tested.

Three models were used in the author's work, the mathematical equations governing these models being described:

$$(1) \frac{dx}{dt} + ax = a$$

$$(2) \frac{dx}{dt} + ax = b$$

$$(3) \quad \frac{dx}{dt} + ax = f(t)$$

Where a, b are unknown model parameters, x is the state variable and $f(t)$ is an input of unknown form. All initial conditions are zero.

Numerically transforming the above equations, the solutions for the unknown model parameters can be written from the identification technique:

$$(1) \quad a = \frac{\sum_{s=1}^N \frac{s^2 x(s) \{s x(s) - 1\}}{\{s x(s) - 1\}^2}}$$

$$(2) \quad a = \frac{\sum_{s=1}^N s x(s) \cdot \sum_{s=1}^N s^2 x(s) / N - \sum_{s=1}^N s^3 x^2(s)}{\sum_{s=1}^N s^2 x^2(s) - \left\{ \sum_{s=1}^N s x(s) \right\}^2 / N}$$

$$b = \frac{\sum_{s=1}^N s^2 x(s) + a \sum_{s=1}^N s x(s)}{N}$$

$$(3) \quad a = \frac{\sum_{s=1}^N \{g(s) - s g^2(s)\}}{\sum_{s=1}^N g^2(s)}$$

where $g(s) = \frac{x(s)}{f(s)}$

A specimen derivation for (1) is given in Appendix I (c).

4.4 Method of Study.

Before continuing with a detailed discussion of the various programs, a brief outline of the methods adopted will be given.

The first program written to evaluate the usefulness of this identification technique was a straightforward on-line program for the PDS. 1020, taking as its data readings monitored through the logging system from a simulation on the HY-48. The program and simulation circuit are discussed in section 5.4.

Model parameters were set by potentiometers on the HY-48 and these settings compared with the results from the identification technique. Different noise levels could be added to the simulation output from a pseudo-random noise generator on the HY-48. The statistical characteristics of the added noise were evaluated from a separate on-line program, shown in section 5.7.

Only the first model described above was studied using this program, as it very soon became clear that this was a very laborious

method of studying the technique.

The next stage of study consisted of using the PDS. 1020 as a monitoring computer only and evaluating the model parameters in an off-line program for every possible time scale and sample size, given a particular number of readings from the PDS. 1020. This off-line processing was done by an Algol program in the ICL. 1905, data being fed in from tape generated from the PDS. 1020. Details are shown in section 5.5.

This was a distinct improvement over the initial identification program, as a number of identifications could be carried out from a single run of the PDS. 1020 monitor program. The model studied was again a single parameter model with an input of known form. The tape interface between the PDS. 1020 and the ICL. 1905 was tested by a small separate program. (section 5.7).

It was still not possible to carry out an analysis of the effect of noise on the accuracy of identification without carrying out a number of runs using this program and a considerable amount of tape was used in its execution. Means and standard deviations of the results were computed separately and this tended again to be very tedious.

The finally developed test programs carried out a fixed number of runs on the HY-48 - PDS. 1020 linkup, sorted the data in the PDS. 1020 monitor program and evaluated the statistical characteristics of the results off-line. Operator effort was at a minimum in this case. Details are given in section 5.6.

Two models were tested in detail by this method, the models being numbers (2) and (3) given in the previous section. Model (2) was chosen over model (1) so that the forcing function amplitude was also *estimated*. The forcing function used on the HY-48 simulation for the case where the form of the input was unknown to the identification programs was the output of a 1st Order lag.

The parameters varied in these analyses were:

- (a) The model parameter.
- (b) The forcing function final amplitude.
- (c) The added noise levels.

For each set of the above parameters, the effect of sample size and time scale could also be studied.

Off-line programs were written to establish the accuracy of the identification technique, given true models. (section 5.3). The solutions of these true models were computed analytically.

1. The first part of the book is devoted to a general discussion of the theory of the firm. It is here that the reader will find the most interesting and original contributions of the author. The second part of the book is devoted to a detailed analysis of the theory of the firm in the context of the theory of the market. It is here that the reader will find the most interesting and original contributions of the author.

Chapter 5

5.1 Introduction.

In this chapter the digital computer software and the parallel hybrid computer circuits will be discussed in detail. Only block diagrams of the Assembler language programs will be shown, while the Algol programs will be presented in full. Assembler language programs are listed in Appendix VI.

The programs can be split into 6 groups. These groups are summarised below:

(a) The general logging program:

This program was developed as a general program to log results from runs on the double effect evaporator and simulations on the HY-48.

(b) Off-line Identification tests:

These programs were developed to compute the estimated parameters from true models and were used as backup programs for the later on-line programs.

(c) On-line Identification Programs:

This program was a true on-line program for estimating parameters from data monitored from the HY-48 or the double-effect evaporator. The HY-48 simulation used by the author with this program is shown.

(d) Single-cycle monitor programs with off-line processing:

This group includes a PDS. 1020 monitoring program and an Algol off-line processing program. The HY-48 simulation used was similar to that in (c). A slightly different model was used.

(e) Repetitive-operation monitor programs with off-line processing:

This group contains the more highly sophisticated repetitive operation programs developed from those in the preceding group.

(f) Support software:

This includes a program for the on-line estimation of the statistical characteristics of the added noise from the pseudo-random

noise generator on the HY-48. Another program was developed to test the tape interface between the PDS.1020 and the ICL. 1905.

Each of these groups will be described in detail in the following sections, program flow charts, listings or circuit diagrams being shown where relevant.

5.2 The general logging program.

This program is designed to be operated under either sense line control or sense switch control, depending on whether the program is to be operated from the remote data logging cabinet or the PDS. 1020 itself. As it is written for the PDS. 1020, it is an Assembler language program. A block diagram of the program is shown in figure 5.2.

The program is initiated from the computer, which first requires to know whether the filter is to be software controlled or out and whether control will be from the remote logging cabinet or the computer keyboard. Data can be input to the program from the remote cabinet using the scan switches under the control of sense line 3.

Having received this information, the computer goes into a cycle round sense switch/sense line 2. As the sense lines and sense switches are paralleled in this program, future reference will only be to sense switches.

At this point the operator must decide whether he wishes to carry out repetitive scans of data from the apparatus to which the data logger is connected, or whether single individual operations are to be carried out. This choice is controlled by the setting of sense switch 4 and transfer of control to either mode is initiated from sense switch 2.

Considering the repetitive mode first, information is read in concerning the range of channels to be scanned, i.e. the first and last channel numbers. Should a channel be requested outside the range possible on the data logger, an error message is output and the program halts.

The optimum gain settings for each channel are now automatically evaluated and the resultant gains for each channel are printed out. Should any channel reading go outside the range of the A.D.C. during operation of the repetitive mode, the error message OVERFLOW is printed out, channel gains are automatically recomputed and the cycle continues.

A further decision has to be made by the operator before the repetitive mode is initiated. This is whether or not the channel readings are to be automatically scaled to give true values of the parameters being monitored, i.e. temperature in $^{\circ}\text{C}$, pressure in psia., etc. This is controlled from sense switch 1. Scaling factors are input in the single operation mode and are discussed in a later paragraph.

Having computed and printed the gains, the computer goes into the cycle shown in the block diagram, until such time that sense switch 4 is switched off. Channel readings can be taken under timer control from the digital clock, should the clock be in the synchronous mode. When sense switch 4 is switched off, the program control returns to sense switch 2.

In the single operation mode, 8 possible operations can be carried out by input of a selection number through the computer keyboard or scan switches. The operations and associated selection numbers are shown below:

<u>Selection Number</u>	<u>Operation</u>
0	Program returns to start.
1	Input channel range.
2	Compute and print channel gains.
3	Read and print channels - scaled values.
4	Select input mode and filter. This operation is only possible from the computer.
5	Input and print channel calibration factors.
	Parameter values, y , are related to voltage readings, x , by a straight line relationship, $y = mx + c$.

Selection NumberOperation

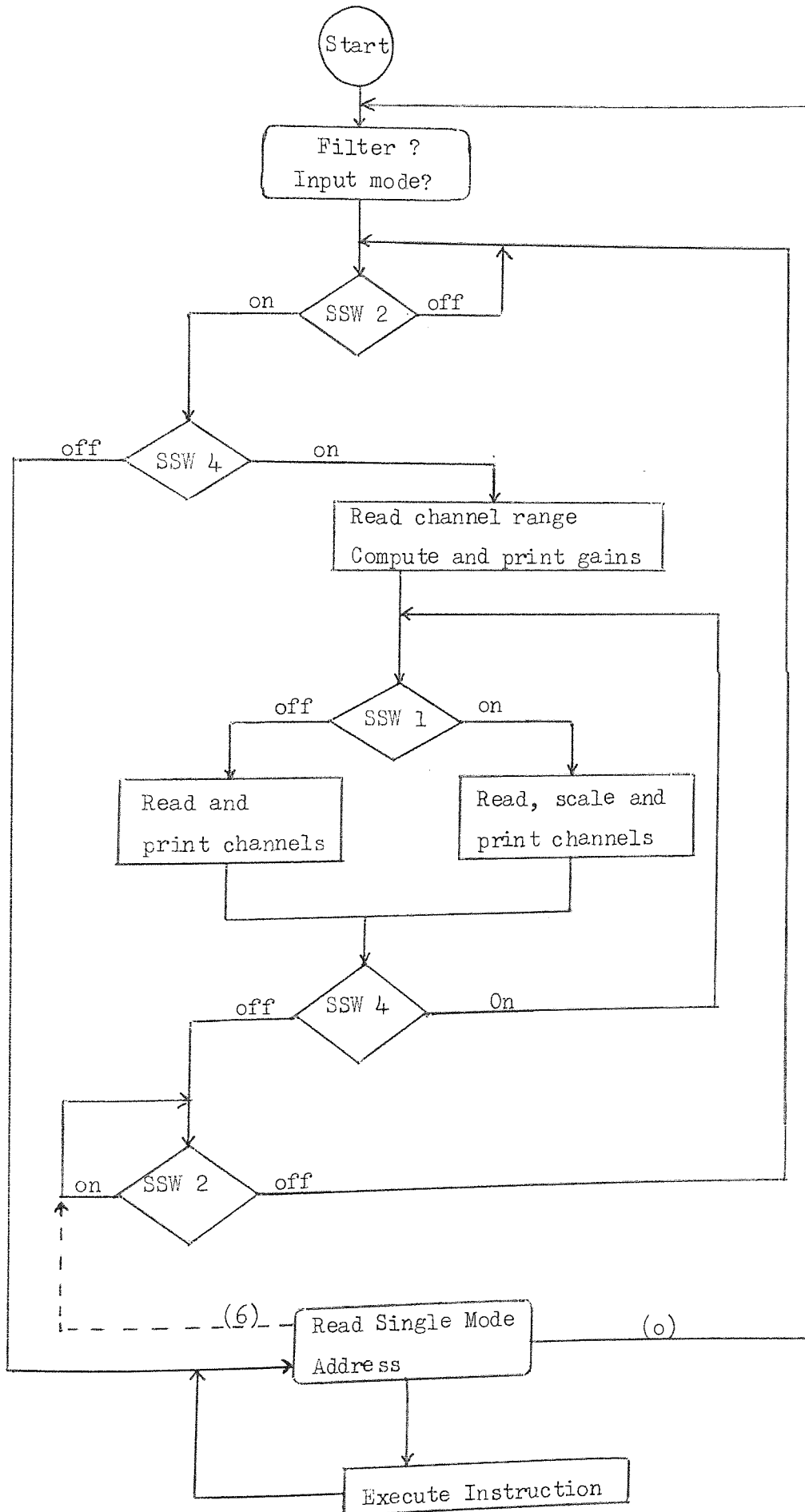
- m and c are the calibration factors to be input.
- 6 Return to main program loop.
- 7 Input channel range, input and print channel scaling factors.

Note that for this program typewriter tabs should be set in multiples of 14 to obtain the best output format.

A set of specimen results from this program is given in Appendix II a, and the program is listed in Appendix VI.

Figure 5.2.

General logging program block diagram.



5.3 Off-line identification programs.

Two off-line identification programs were written. The first, written in PDS. 1020 Assembler language, estimated results for a model with an input of known form, in this case a step function. The second was an Algol program to estimate results for a model with an unknown input. Both programs utilised the technique of calculating the response of known models from analytical relationships, and then estimating the model parameters from this known response. Comparison of the known model parameters with those estimated from the known responses gave an indication of the effectiveness of the identification technique under ideal conditions.

5.3.1 Identification of a model with known input form.

This program was written to be operated under the control of the macro switches on the PDS. 1020. Using these, the program could be entered at various points, as shown in the block diagram in fig. 5.3.1.

The program starts with the input of the sample size to be used, the elements of the matrix, $M_{is} = w_i r_i^{s-1}$ and values of the times $t_i = -\ln r_i$. The proposed time scale to be used is input, followed by the true values of the model parameters.

The required values of $x(t)$, the model outputs, are computed from analytical relationships. Hence $x(s)$ is calculated, followed by the estimation of the model parameters. The true and estimated model parameters are printed out. The values of $x(s)$ and $x(t)$ computed can be obtained by depressing macro switches G and I respectively.

Data to the program can be fed in from tape or keyed in through the keyboard, choice being controlled from sense switch 1. Two standard subroutines were used with this program, a floating point interpreter for automatic floating point arithmetic operations, and a related floating point output subroutine for the printout of floating point numbers.

Specimen results for this program are given in Appendix II b.

The model form is described mathematically,

$$\frac{dx}{dt} + ax = b, x(0) = 0$$

True values of a and b are fed in consecutively when requested.

The solution of the above equation, giving the response, $x(t)$, is

$$x = \frac{b}{a} (1 - e^{-at})$$

A similar program was written for the model form,

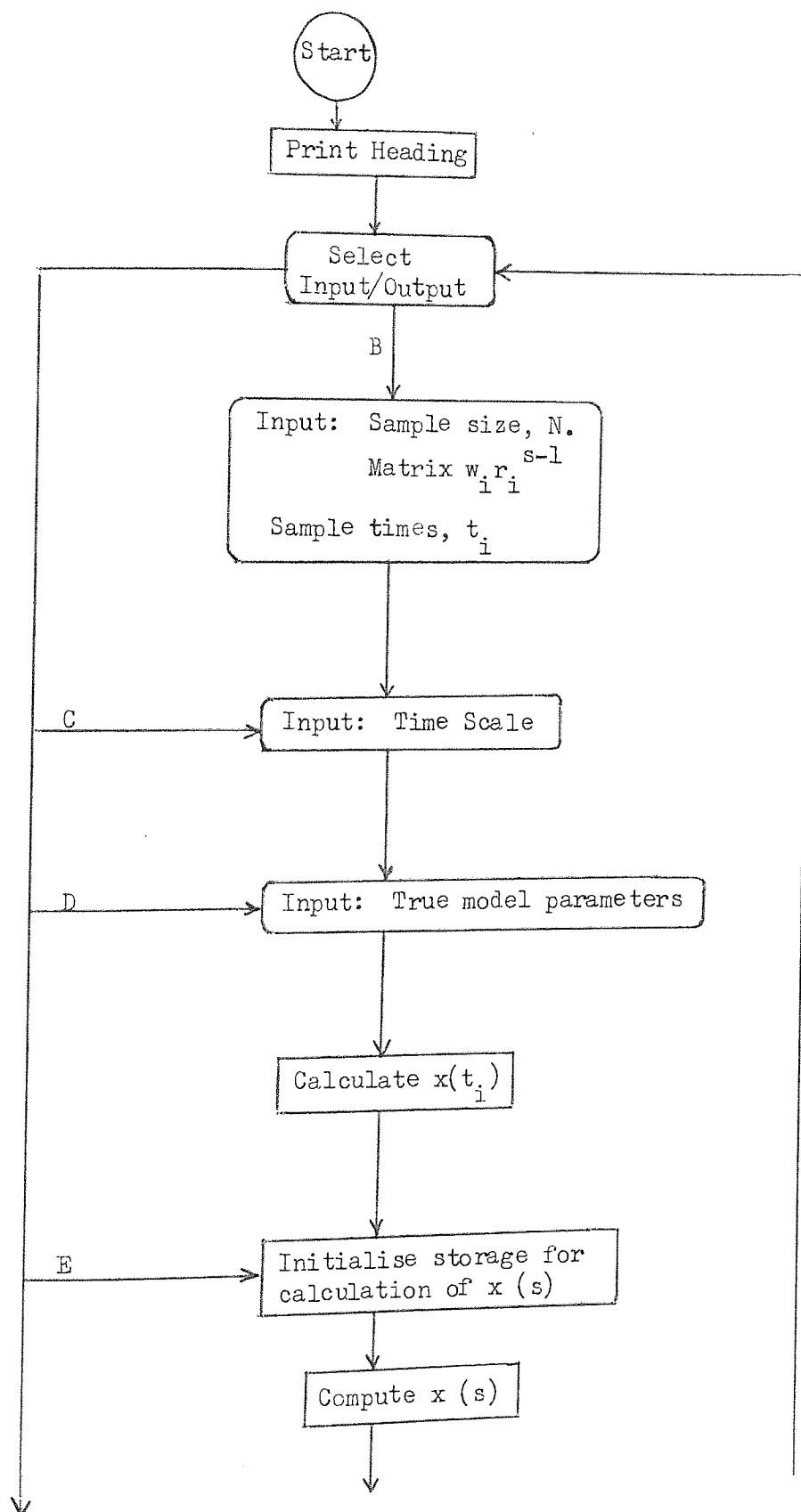
$$\frac{dx}{dt} + ax = a, x(0) = 0$$

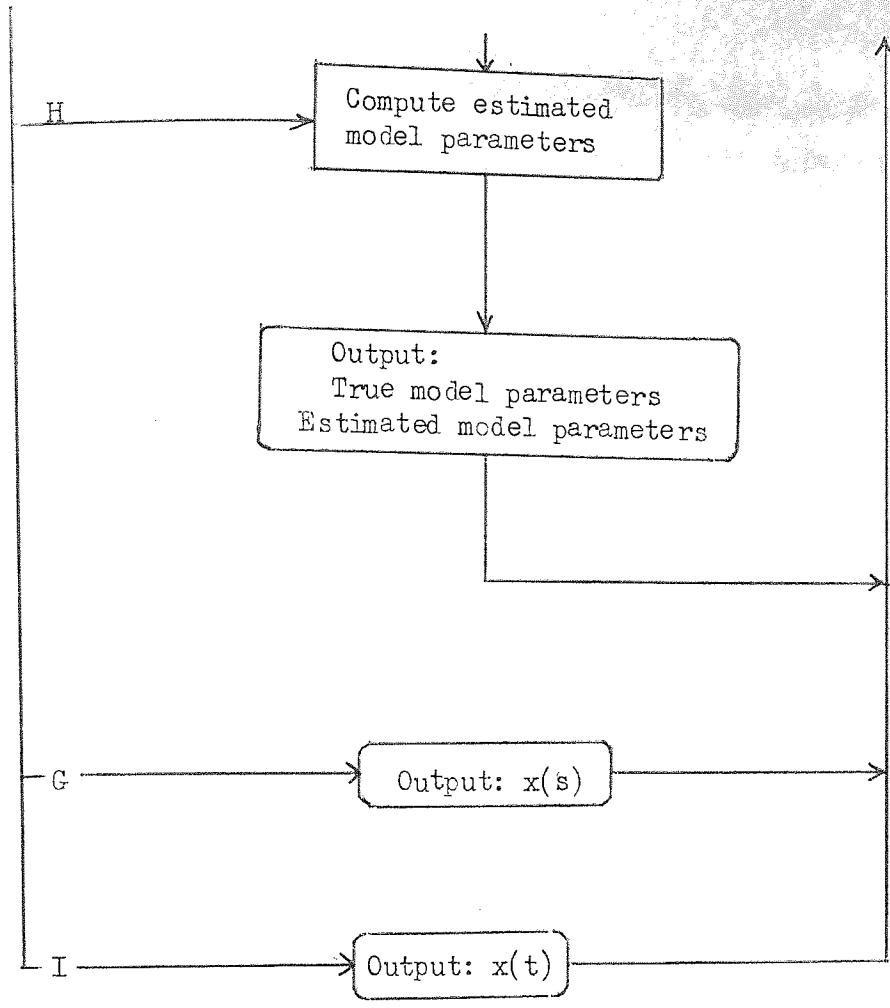
The solution is:

$$x = 1 - e^{-at}$$

Figure 5.3.1

Block diagram for the off-line identification of a model with known input form.





Standard Subroutines used:

Floating Point Interpreter.

Floating Point Output.

Note.

SSW 1 ON: Input from tape.

SSW 1 OFF: Input from K/B.

5.3.2. Identification of model with unknown input form.

This program, written in Algol, computed the response of one first order system and then used this response as an input to a second first order system. The response of this second first order system was calculated analytically. From a knowledge of the input and output curves for the second first order system, an estimation could be made of the model parameters of this system. The estimated values of these model parameters could then be compared with the true values. The program is listed in fig. 5.3.2, while a variable reference table and the input data format specification are shown in tables 5.3.2 (a) and 5.3.2 (b) respectively.

The program first requires the input of the sample size together with related values of $w_i r_i^{s-1}$ and t_i . The number of calculations required for this particular sample size is input.

The set of parameters necessary for the computation of the inputs and outputs to the system are read in. The inputs and outputs, and hence the estimated value of the model parameter, are computed for a range of time scale values and the results printed out. After every ten parameter estimations for different time scales, the values of the system inputs and outputs are printed to give some idea of the spread of samples over the total response curves.

The above process is repeated for different sets of parameters, the number of sets used being controlled by a counter, CALCS. At the end of this period a new value for the sample size is read in, and the process repeated. Should the sample size be set to zero, then the program terminates. Results from this program are shown in Appendix II b.

The forcing function is generated as the output of the following model,

$$\frac{dR}{dt} + WR = A, \quad R(0) = 0,$$

and the system model is given as

$$\frac{dX}{dt} + \text{TRUE} * X = R, X(0) = 0,$$

where R, W, A, TRUE and X are defined in table 5.3.2 (a).

Table 5.3.2 (a)

Below is a reference table for the variable defined in the program:

Variable Name	Reference
I, J, K, L	General counters
DIM	Sample size
CALCS	No. of calculations per sample size
A STORE, B STORE	Buffer stores
TRUE	True system parameter
EST	Estimated system parameter
SCALE	Time scale
W, A	Model parameters - forcing function
MATRIX	$w_i r_i^{s-1}$
TIME	t_i
G	System impulse response in terms of Laplace operator, s.
X, R	System response and forcing function respectively
XS, RS	Laplace transforms of X and R

Table 5.3.2 (b)

Input data format

Data from cards

DIM

MATRIX: row by row

TIME

CALCS

A
 W
 TRUE
 A
 W
 TRUE
 etc.

} Number of parameter settings controlled by CALCS

DIM

Repeat above procedure. To stop, set DIM = 0

Figure 5.3.2.
Off-line Identification Program for model with unknown input form.

```

'BEGIN' 'INTEGER' I,J,K,L,DIM,CALCS;
'REAL' ASTORE, BSTORE, EST, TRUE, SCALE, W, A;
'COMMENT' FIRST ORDER LAG. ;
SELECT OUTPUT (0);
START: DIM:= READ;
'IF' DIM=0 'THEN' 'GOTO' FINISH;
'BEGIN' 'REAL' 'ARRAY' MATRIX [1:DIM, 1:DIM], G, X, R, XS, RS, TIME[1:DIM];
'FOR' J:=1 'STEP' 1 'UNTIL' DIM 'DO'
'FOR' I:=1 'STEP' 1 'UNTIL' DIM 'DO'
MATRIX [ I, J ] :=READ;
'FOR' I:=1 'STEP' 1 'UNTIL' DIM 'DO'
TIME[I]:=READ;
CALCS:=READ;
'FOR' K:=1 'STEP' 1 'UNTIL' CALCS 'DO'
'BEGIN' A:=READ;
W:=READ;
TRUE:=READ;
NEWLINE (4);
WRITETEXT ('(' 'INPUT% SIGNAL% FORCING% FUNCTION = %' ')');
PRINT (A, 0, 5);
NEWLINE (2);
WRITETEXT ('(' 'INPUT% SIGNAL% TIME% CONSTANT=%' ')');
PRINT (W, 0, 5);
NEWLINE (2);
WRITETEXT ('(' 'SYSTEM% TIME% CONSTANT=%' ')');
PRINT (TRUE, 0, 5);
NEWLINE (2);
WRITETEXT ('(' 'TIME% SCALE' ('7S') 'ESTIMATE' ')');
NEWLINE (2);
L:=0;
'FOR' SCALE:=1/0.119574 'STEP' 1/0.119574
'UNTIL' (21/0.119574+0.001) 'DO'
'BEGIN' ASTORE:=BSTORE:=0.0;
'FOR' I:=1 'STEP' 1 'UNTIL' DIM 'DO'
'BEGIN'

```

```

XIIJ:=(A/W)*(1/TRUE-(W/(TRUE*(W-TRUE))))*
EXP(-TRUE*SCALE*TIME[IJ])+(1/(W-TRUE))*
EXP(-W*SCALE*TIME[IJ]);
R[IJ]:=(A/W)*(1-EXP(-W*SCALE*TIME[IJ]));
'END';
L:=L+1;
'IF' L=10 'THEN' 'BEGIN'
NEWLINE (1);
SPACE (3);
WRITETEXT ('INPUT('LOS')'OUTPUT');
NEWLINE(2);
'FOR' L:=1 'STEP' 1 'UNTIL' DIM 'DO'
'BEGIN'
PRINT(RLL1,3,5);
SPACE (2);
PRINT (XIL1,3,5);
NEWLINE (1);
'END';
L:=0;
NEWLINE (2);
'END';
'FOR' I:=1 'STEP' 1 'UNTIL' DIM 'DO'
'BEGIN'
XS[I]:=RS[I]:=0.0;
'FOR' J:=1 'STEP' 1 'UNTIL' DIM 'DO'
'BEGIN' XS[I]:= XS[I]+SCALE*MATRIX[J,I]*X[J];
RS[I]:=RS[I]+SCALE*MATRIX[J,I]*R[J];
'END';
G[I]:=XS[I]/RS[I];
ASTORE:=ASTORE+G[I]-I*G[I]2/SCALE;
BSTORE:=BSTORE+G[I]2;
'END';
EST:=ASTORE/BSTORE;
PRINT(SCALE,0,5);
SPACE(2);
PRINT(EST,0,5);
NEWLINE(1);
'END';
'END';
'END';
'GOTO' START;
FINISH:'END';

```

5.4 The on-line identification programs.

A PDS. 1020 program computed values of the numerical Laplace transform of the input from a variable number of channels on the logging system, these channels being connected to the HY-48 simulation. The program was on-line in the sense that the values of the numerical Laplace transform were continually being calculated between sampling times, with the limitation that the clock could only be read once during each timer setting period, as the computer was immobilised at this stage until the end of this timing period. Only a limited amount of computation could be done during the timing period, otherwise there was a chance that the timer increment would be missed.

A small section of program was added to this program to compute estimated parameter values for a particular model, given numerical values of the Laplace transform. The model used in this case was described mathematically.

$$\frac{dx}{dt} + ax = a, x(0) = 0$$

where a was the unknown parameter.

This model was chosen for its simplicity, together with the fact that the response of the model simulated on the HY-48 was limited to a final response amplitude of 1 machine unit at all times, as is shown by the analytical solution of the above equation,

$$x = 1 - e^{-at}$$

A block diagram of this program is shown in figure 5.4.1.

The HY-48 simulation circuit is shown in figure 5.4.2. This simulation includes a random noise generator. Two channels from the HY-48 were monitored by the above PDS. 1020 program, the first was a control channel, giving the simulation output uncorrupted by noise and the second gave the simulation output plus added noise from the noise generator. The statistical characteristics of the added noise were

computed using a small on-line support program, described in section 5.6.

The Identification program required information concerning the sample size, conversion matrix and sampling times before the identification routine could be initiated. The sampling times were taken as multiples of the smallest sampling time given by the theory for the particular required sample size. These times were scaled to giving sampling times as multiples of the clock timer setting on the logging system, usually 1 second. The time-scale factor was chosen accordingly in either the s or t domain.

From these values of sampling times, sample time counters, CX, could be evaluated, giving the number of clock timer increments between samples.

First and last channel numbers, giving the range of channels to be scanned, were read in. These channels had to be consecutive.

The identification routine could be initiated in two ways. The first was under the control of sense switch 2. The preferable alternative method was to go into a loop continuously scanning the output of one of the channels to be scanned until the value of this output changed by more than a set small value. Hence the identification routine could be started. For this method, the channel acting as control channel for the identification program had to be read in, together with the limit on the signal amplitude change before the identification routine was to be initiated.

Initialisation of some storage locations was also necessary before computation could continue. This included the zeroing of three counters which played an important part in the routine: CO, the clock counter, SC, the sample counter and NN, a matrix computation counter. The use of these counters will be dealt with in detail in the following paragraphs.

On entering the identification routine the clock was read and the clock counter, CO, was incremented by one. CO was compared with CX

to establish whether the sampling period was complete.

If it was complete, all the required channels were scanned, and the sample counter, SC, was incremented by one. If all required samples had been taken, CX was set to zero and the program continued to the matrix computation routine, which will be discussed below. If more samples were required, CX was reset and the program returned to the clock counter.

If the sampling period was not complete after the clock counter update, then the sample counter was compared with NN, the matrix computation counter. Initially NN and SC were both zero, so the program continued to cycle on the clock counter.

After SC had been updated and the channels scanned, however, SC was greater than NN, and the program entered the matrix computation routine.

This routine calculated the values of a single column of elements from the formula

$$x(s) = x(s) + w_1 r_1^{s-1} x(t_1)$$

i.e. The above formula was evaluated for $s = 1, 2, \dots, N$. Only one channel was considered for each entry to this routine. On leaving the routine, a check was made on whether $x(s)$ had been updated for all the channels read during the previous scan. If it had, NN was updated by one. Otherwise on return to the matrix computation routine $x(s)$ was updated for another channel.

Should all the scan computations have been completed, i.e. $x(s)$ evaluated for all the channels considered, then the program transferred to the parameter estimation routine. Alternatively, depending on the value of CX, which showed whether all samples had been taken or not, the program transferred to the clock counter or the matrix computation routine.

Input to this program could be from either keyboard or tape, depending on the setting of sense switch 3.

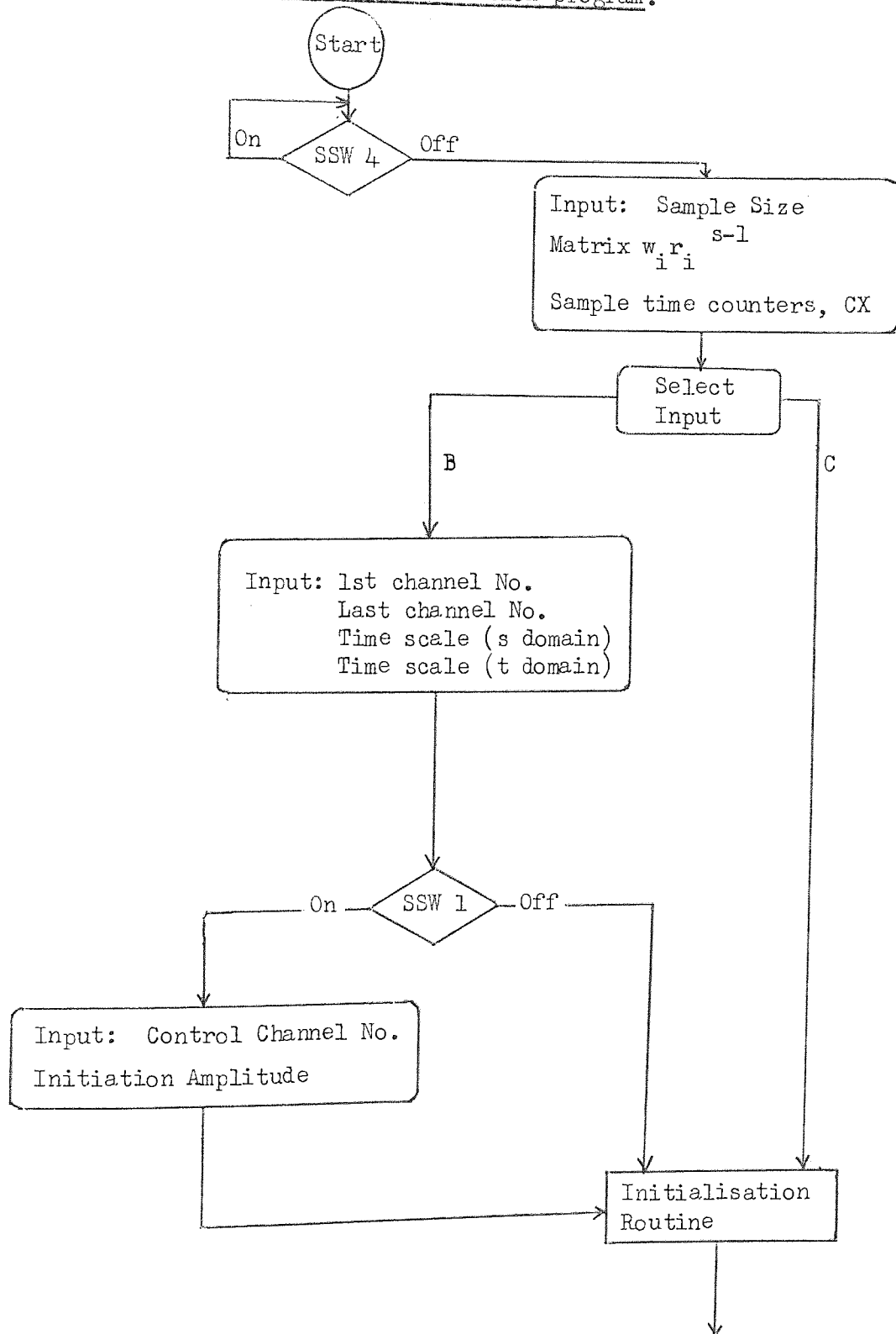
Model parameter estimation routine.

This program floated the values of $x(s)$ computed by the above

program using a standard subroutine. The parameter, a , was computed for the control channel and the channel corrupted by noise and the results were output to the typewriter. Standard subroutines used were a floating point interpreter and a floating point output routine.

Figure 5.4.1.

Block diagram of the on-line identification program.



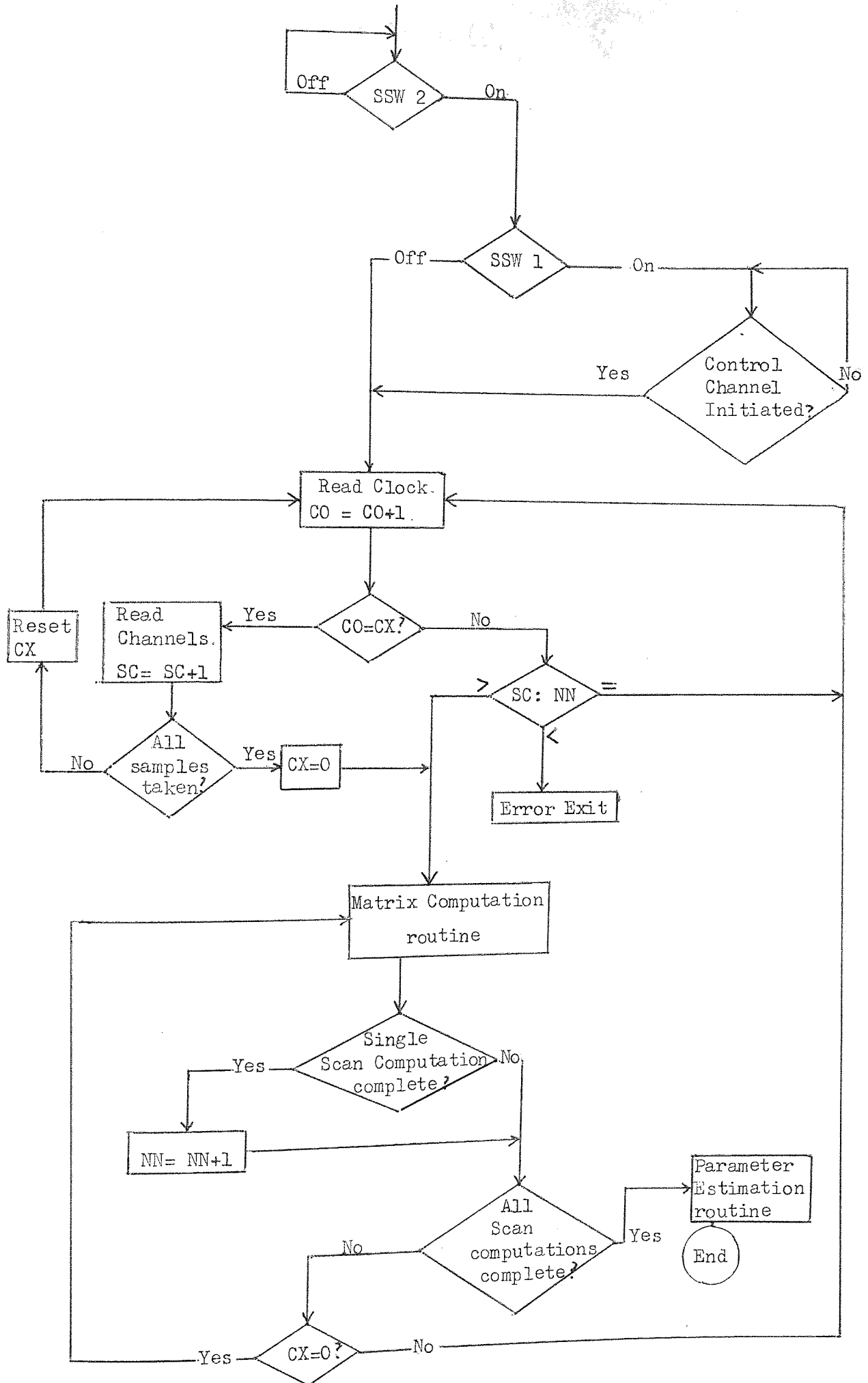
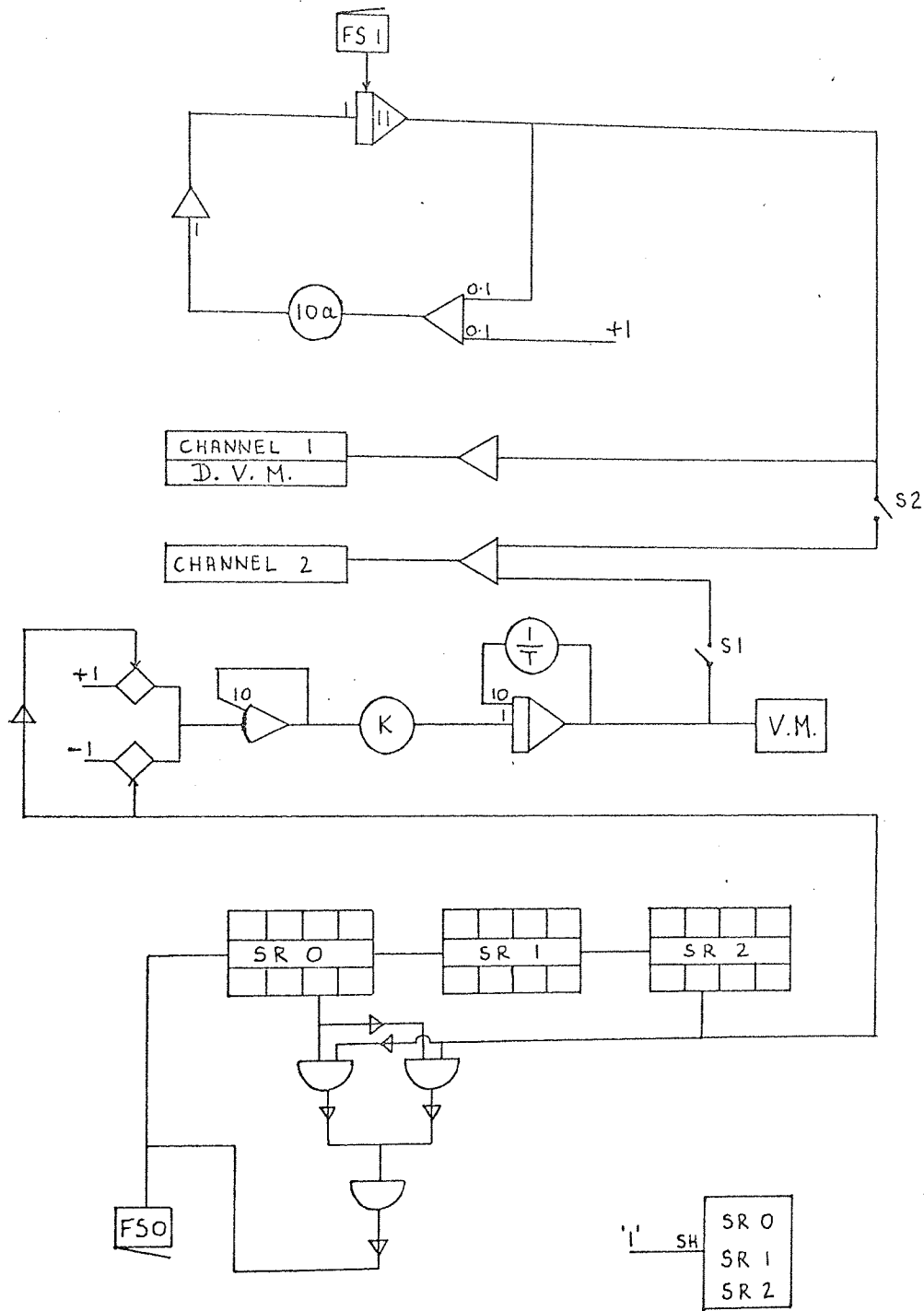


FIGURE 5.4.2

HYBRID CIRCUIT DIAGRAM (1)



CLOCK FREQUENCY SETTING : 10 c./s.

The HY-48 simulation.

This is shown in figure 5.4.2. The model simulation itself was comparatively small, as can be seen. It was generated round integrator 11, and initiated from a logic function switch FS1. The output of the model passed through an inverter to channel 20 on the logging system and also the HY-48 digital voltmeter.

It also passed through an analogue function switch, S2 to another inverter, where a pseudo-random noise signal was added through S1.

The pseudo-random noise generator consisted of a small filtering circuit of time constant T and input gain K. The input was driven by a plus or minus one reference voltage, depending on the state of the two complementary D/A switches.

These switches were controlled from a series of shift registers and AND gates connected as shown. The signal from this series was pseudo-random in form. The speed with which the signal was generated was controlled by the clock frequency setting on the HY-48 and was set at 10 c/s.

Results from these programs are shown in Appendix IIc.

5.5. Single-cycle identification programs with off-line processing.

These programs consisted of an on-line monitoring program for the PDS. 1020 and an off-line processing program for the ICL. 1905. The HY-48 simulation used was identical to that discussed in the previous section and shown in figure 5.4.2.

The PDS. 1020 on-line monitor program.

This program constituted 6 separate discrete operations, each operation initiated from a macro switch. The operations are summarised in the block diagram shown in figure 5.5.1.

Initially information is input concerning the number of scans to be taken on each channel, the number of channels to be scanned and the number of the first channel to be scanned.

The data tape is headed with information for the ICL. 1905

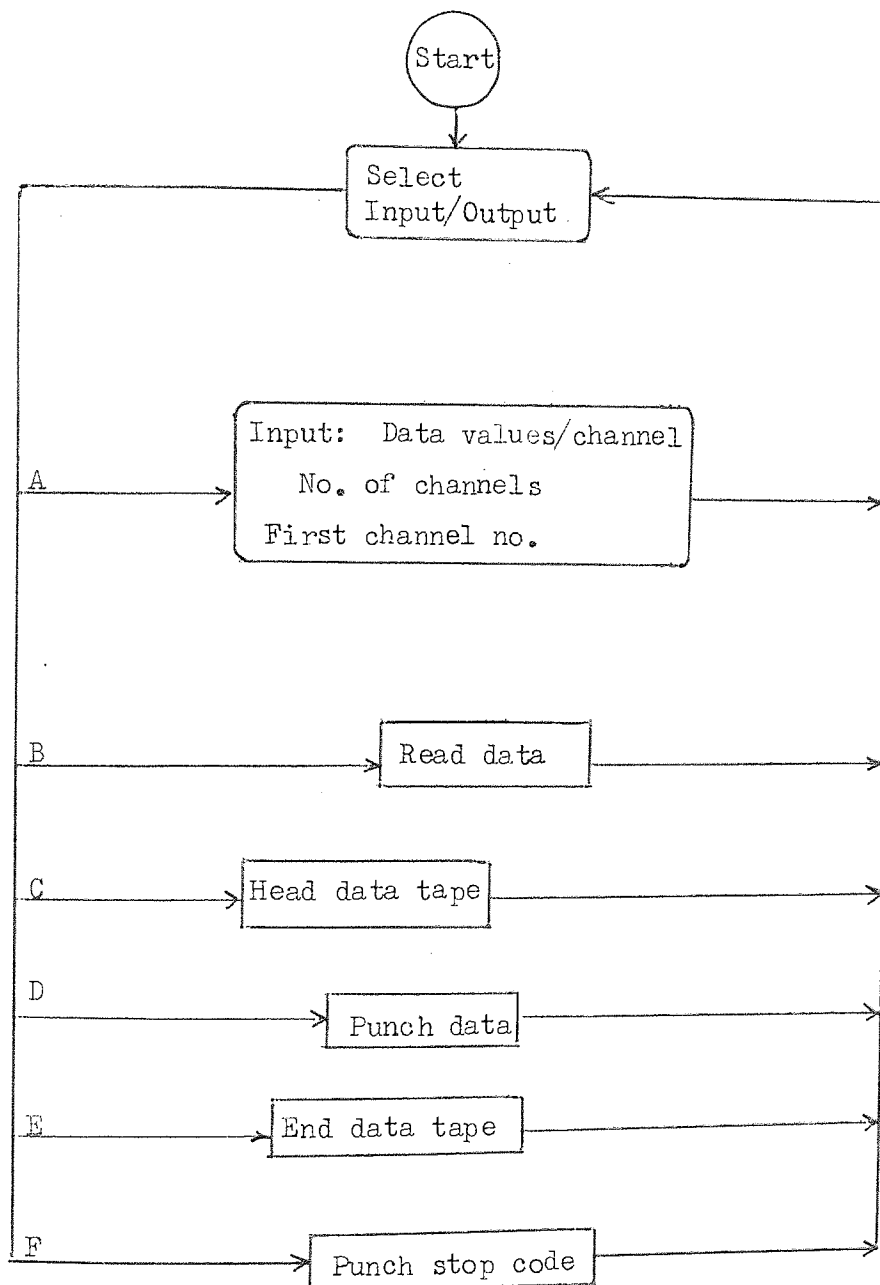
operating system from macro switch C.

On depressing macro switch B the program cycles on the first channel to be scanned until its value changes by more than 10 mV. Channels are then scanned repetitively under control of the clock on the logging system until all the required samples have been taken. The samples are stored in the PDS. 1020 memory.

These samples are then punched onto tape by depressing macro switch D. The stop code is to inform the ICL. 1905 operating system that a particular data tape has been read in, and the End data tape code informs it that all data tapes have been read in.

Figure 5.5.1.

Block diagram of the PDS. 1020 on-line monitor program. (Single cycle).



Off-line parameter estimation program.

This was an Algol program, written to process the data tape produced by the PDS. 1020 monitor program. The program is listed in figure 5.5.2., while a variable reference table and the input data format are given in tables 5.5.2(a) and 5.5.2(b) respectively.

Values of $w_i r_i^{s-1}$ and t_i are read in for sample sizes of 3, 6, 9, 12 and 15. This is followed by input data consisting of the run number, logging system timer setting, number of channels scanned and the number of scans per channel.

The data tape is then read into the ICL. 1905 memory. The data is sorted so that all possible sampling intervals for all possible sample sizes (3,6,9,12 and 15) are covered.

Parameter estimations are made in a procedure EVALUATE after the numerical computation of the Laplace transforms required.

Results from runs with these programs are shown in Appendix II e.

Table 5.5.2(a)

Variable Reference Table.

Variable Name	Reference
I,J,K,L,S	General counters.
NN	Data values per channel.
NO	Number of channels scanned .
RN	Run number.
SI	Sampling interval.
TMP	Clock timer setting on the logging system.
CF	Time scale factor
BU	CF * TMP
FCOUNT	Real subscript estimate.
SUB	Integer subscripts.
SS	Time scaled Laplace operator.

Variable Name	Reference
A	Model parameters.
ABOVE, BELOW	Buffer stores.
M	$w_i r_i^{s-1}$
X	Values of $x(t)$ from tape.
T	t_i
F	Laplace Transforms.

Table 5.5.2(b)

Input data format.

Data from cards.

For sample sizes of 3,6,9,12 and 15, read consecutively:

M, row by row

T

RN

TMP

NO

NN

Data from tape.

Data tape from PDS.1020 monitor program.

X

Data from cards.

RN

If RN = 0 computation stops, otherwise the above process is repeated.

NOTE

Input of M and T is in the order

$w_i r_i^{s-1}$ $i = N, N - 1, \dots, 1$

S = 1, 2, ..., N

t_i $i = N, N-1, \dots, 1$

Figure S.5.2

Off-line processing program. (Single cycle case)

```
'BEGIN' 'COMMENT' ZLOGANAL, PRICE, CESTF109;
'INTEGER' I, J, K, S, NN, NO, RN;
'REAL' SI, CF, BU, FCOUNT, TMP;
'REAL' 'ARRAY' A[1:5], T[1: 15, 1:15], F[1:15, 1:5], M[1:15, 1:15, 1:15];
'PROCEDURE' EVALUATE;
'BEGIN' 'INTEGER' L;
'REAL' ABOVE, BELOW, SS;
'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
'BEGIN' ABOVE:BELOW:=SS:=0;
'FOR' L:=1 'STEP' 1 'UNTIL' K 'DO'
'BEGIN' SS:=SS+CF;
ABOVE:ABOVE-SS2*F[L, J]*(SS*F[L, J]-1);
BELOW:=BELOW+(SS*F[L, J]-1)2;
'END';
A[J]:=ABOVE/BELOW;
NEWLINE(4);
WRITETEXT ('(' CHANNEL%NUMBER=%)');
PRINT(J, 2, 0);
NEWLINE(2);
WRITETEXT ('(' TIME%CONSTANT=%)');
OUTPUT(A[J]);
'END';
'END';
NEWLINE(1);
WRITETEXT ('(' DATA%ANALYSIS%PROGRAM.)');
WRITETEXT ('(' ('1C')-----)');
NEWLINE(2);
SELECTINPUT(0);
SELECTOUTPUT(0);
'FOR' K:=3 'STEP' 3 'UNTIL' 15 'DO'
'BEGIN' 'FOR' I=1 'STEP' 1 'UNTIL' K 'DO'
'FOR' J=1 'STEP' 1 'UNTIL' K 'DO'
M[I, J, K]:=READ;
'FOR' I:=1 'STEP' 1 'UNTIL' K 'DO'
T[I, K]: = READ;
'END';
START: SELECTINPUT(0);
RN:=READ;
'IF' RN=0 'THEN' 'GOTO' FINISH;
TMP:READ;
NO:=READ;
NN:=READ;
NEWLINE(4);
WRITETEXT ('(' RUN%NUMBER=%)');
PRINT(RN, 2, 0);
WRITE TEXT ('(' ('1C')-----)');
NEWLINE(1);
WRITETEXT ('(' TIME%MARKER%PULSE%SETTING=%)');
PRINT(TMP, 2, 1);
NEWLINE(1);
WRITETEXT ('(' NUMBER%OF%CHANNELS=%)');
PRINT(NO, 2, 0);
NEWLINE(1);
WRITETEXT ('(' DATA%VALUES%PER%CHANNEL=%)');
PRINT(NN, 3, 0);
SELECTINPUT(3);
'BEGIN' 'REAL' 'ARRAY' X[1:NN, 1:5];
'INTEGER' 'ARRAY' SUB[1:NN];
'FOR' I:=1 'STEP' 1 'UNTIL' NN 'DO'
```

```

'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
XI I,J]:=READ;
'FOR' K:=3 'STEP' 3 'UNTIL' 15 'DO'
'BEGIN' SI:=0;
NEWLINE (5);
WRITETEXT('('QUADRATURE%SIZE=%)');
PRINT(K,2,0);
WRITETEXT('('('LC')'-----)');
RETURN:SI:=SI+TMP;
CF:=T[I,K]/SI;
BU:=CF*TMP;
'IF' T[K,K]/BU > NN 'THEN' 'GOTO' CONTINUE;
NEWLINE(2);
WRITETEXT('('SAMPLING%INTERVAL=%)');
PRINT(SI,2,1);
SUB[I]:=ENTIER(SI/TMP+0.01);
'FOR' I:=2 'STEP' 1 'UNTIL' K 'DO'
'BEGIN'
FCOUNT:=T[I,K]/BU;
'IF' (FCOUNT-ENTIER(FCOUNT)) 'GE' 0.5 'THEN' SUB[I]:=ENTIER(FCOUNT)+1
'ELSE' SUB[I]:=ENTIER(FCOUNT);
'END';
'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
'FOR' S:=1 'STEP' 1 'UNTIL' K 'DO'
'BEGIN' F[S,J]:=0;
'FOR' I:=1 'STEP' 1 'UNTIL' K 'DO'
F[S,J]:=F[S,J]+M[S,I,K]*X[SUB[I],J]/CF;
'END';
EVALUATE;
'GOTO' RETURN;
CONTINUE: 'END';
'END';
'GOTO' START;
FINISH: 'END';

```

5.6 Repetitive-Operation identification programs with off-line processing.

These programs included a monitor program for the PDS. 1020 which was controlled from the digital clock on the HY-48. By slaving the PDS. 1020 to the HY-48 in this way, fixed numbers of runs could be monitored and punched without operator interference.

The PDS. 1020 sorted the data prior to punching it onto tape, which reduced the tape consumption considerably.

The off-line Algol program computed the means and standard deviations of the resulting model parameter estimations from all the runs.

The HY-48 Simulation.

The simulation was similar to that shown in figure 5.4.2 with the addition of a timing circuit to operate the model and an analogue logic signal to control operation of the PDS. 1020 monitor program. The circuit is shown in figure 5.6.1(a).

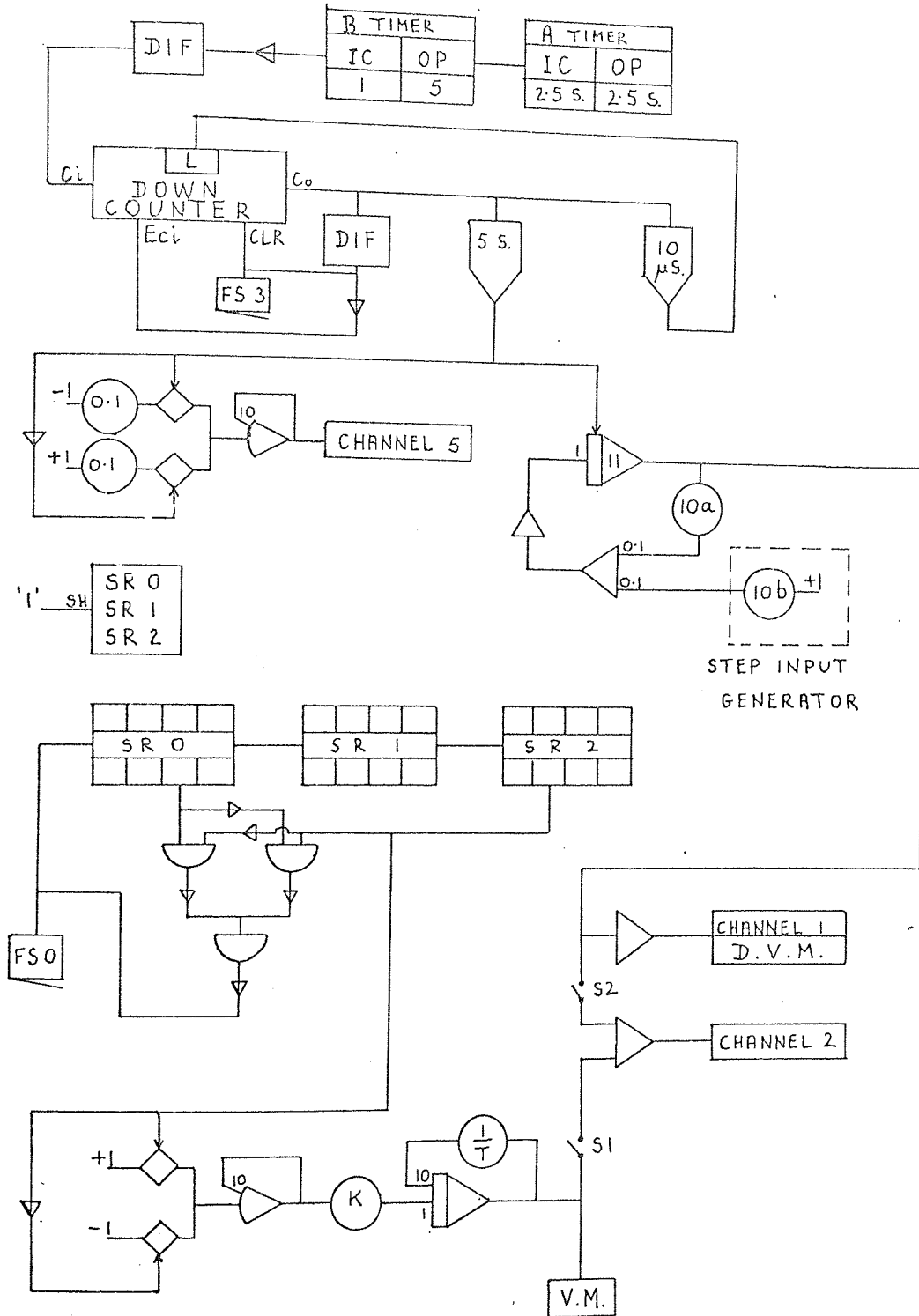
The timing signal was generated from two timers in series with the settings as shown. The output of the second timer gave a logic '1' signal to the differentiator every 30 secs. The pulse from the differentiator activated a down counter which was initially set by digi-switches on the logic control panel. At the end of the down counter sequence, i.e., when the down counter had decremented to zero, a pulse was produced on the Co line from the down counter. This signal temporarily disabled the down counter input by setting EC_i to logic '0', reloaded the down counter to the value set up on the digi-switches through a monostable with a $10\mu s$ setting and reset the analogue simulation for a period of about 5 secs. through a monostable. This latter signal also set a logic signal to -IV for about 5 seconds. At all other times this signal was at + IV. The signal was monitored from the PDS. 1020 through channel 5.

The model simulated was a first order lag with a step input, given as:

$$\frac{dx}{dt} + ax = b, \quad x(0) = 0.$$

FIGURE 5.6.1(a)

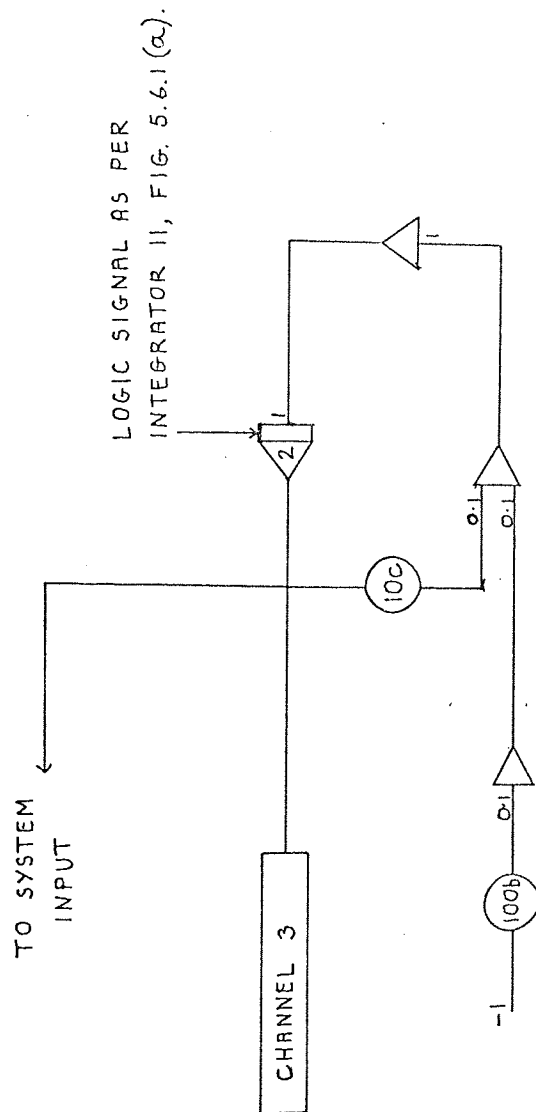
HYBRID CIRCUIT DIAGRAM (2)



CLOCK FREQUENCY SETTING : 10 c./s.

FIGURE 5.6.1 (b).

HYBRID CIRCUIT DIAGRAM (3)



FORCING FUNCTION GENERATOR

The solution of this equation is:

$$x = \frac{b}{a} (1 - e^{-at})$$

Hence b was always set less than a to keep the final response below 1 machine unit.

Figure 5.6.1 (b) shows the circuit modification for the forcing function of unknown form.

The P.D.S. 1020 monitoring program.

This program was similar to the monitor program described previously, with the addition of two further operations. A block diagram of the program is shown in figure 5.6.2.

The first, under the control of macro F, generated counters giving the maximum number of samples possible with the given number of scans to be taken, for each possible sample size. This was obtained by rounding down to the nearest integer the value of $\frac{N}{T}$, where N is the number of scans to be taken per channel, and T is the largest value of t_i for a particular sample size.

Macro E controlled a small executive program, which, once initiated, placed the PDS. 1020 under control of the HY-48 until all runs had been completed.

The number of runs to be carried out was first input. The program then cycled on channel 5 until the logic signal went negative. This showed that the simulation had been reset, and the read data routine proceeded to cycle on the first channel to be scanned until it changed by more than 10 mV, showing the simulation to be again operating. Data was then read in under control of the logging system clock.

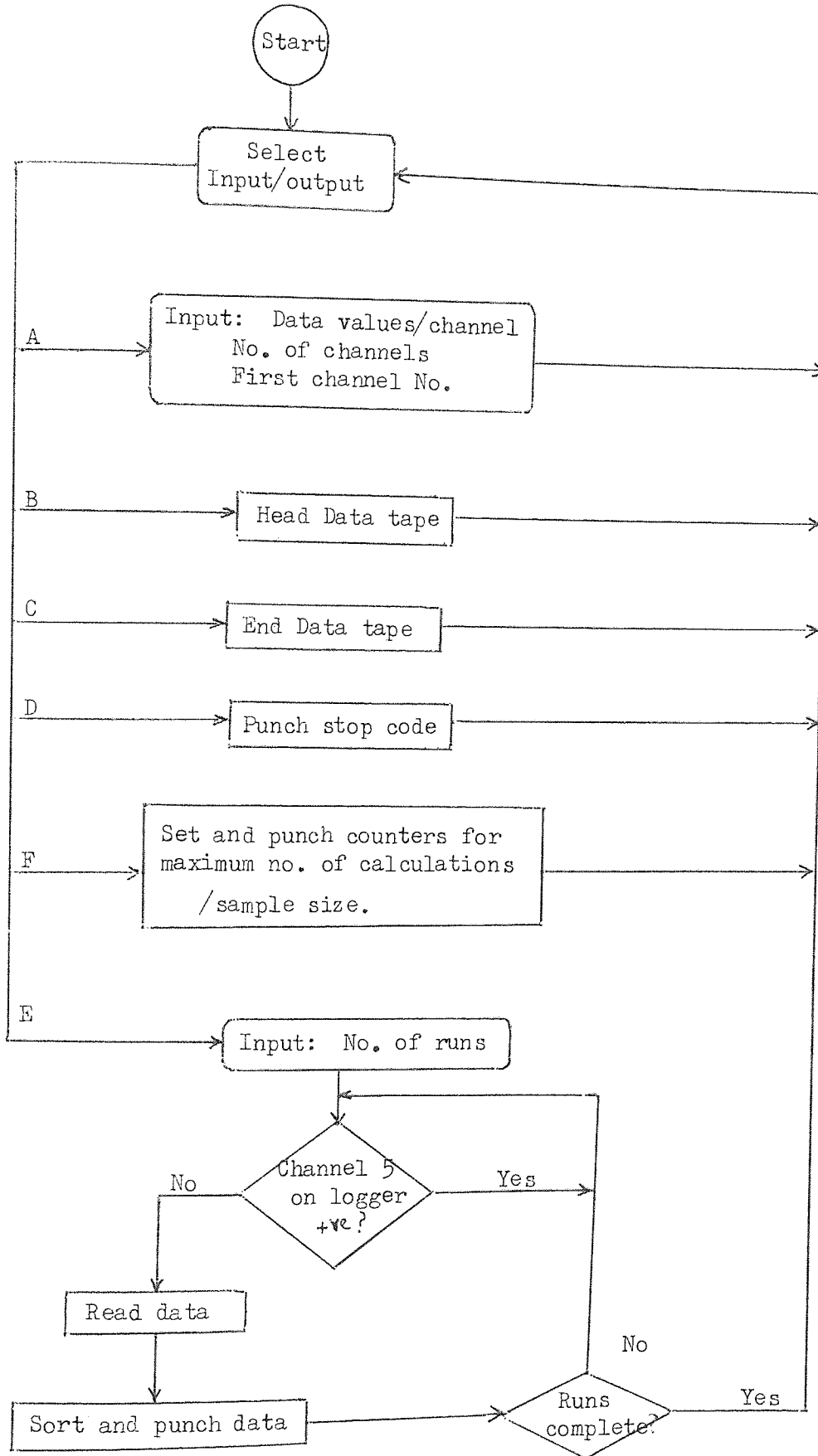
When the data had been read in, it was sorted by the program and then punched onto tape. The data was sorted into samples so that direct calculation of the numerical Laplace Transform could be made in the Algol program, and hence the model parameters predicted.

If all runs had been completed at this time, the program halted.

Otherwise it again cycled on channel 5 until it went negative and the process was repeated. It may be noted here that HY-48 was operating under the control of the timing circuit during the operation of the monitor program.

Figure 5.6.2

Block diagram of the PDS.1020 monitor program. (Repetitive operation).



Off-line processing program.

This program is very similar to the previous off-line processing program except in this case the model parameters are not printed out but are stored for the computation of the means and standard deviations at the termination of all the parameter estimations. These means and standard deviations are printed out, together with the related sampling intervals and overall sampling periods. The overall sampling periods were taken as the time between the initiation of a run and the time at which the last channel reading used by the identification technique was read.

The program is listed in figure 5.6.3, while a variable reference table and the input data format are shown in tables 5.6.3(a) and 5.6.3(b) respectively.

Results from this program are given in Appendix III. The procedure EVALUATE is shown for the known forcing function case and has to be slightly modified for the case of the unknown forcing function.

Table 5.6.3 (a).Variable Reference table

Variable Name	Reference
I,J,K,KK,N,M,L,S	General counters.
NN	Data values per channel.
NO	Number of channels.
RN	Run number.
N1	Number of sets of readings.
FCOUNT	Real subscript counter.
SUB	Integer subscript.
RSI	Sampling interval counter.
SI	Sampling interval.
CF	Time scale factor.
TMP	Timer setting on logging system.

A1, A2, A3	Buffer stores.
SS	Time scaled Laplace operator.
A, B	Model parameters.
STAN	Standard deviation.
MEAN	Mean.
MM	$w_i^{r_i s-1}$
T	t_i
F	$x(s)$
X	$x(t)$ from PDS. tape.
SP	Sampling period.
C	Number of samples per sample size.

Table 5.6.3(b).

Input data format.

Data from cards.

For sample sizes of 3,6,9,12 and 15, read consecutively:

MM, row by row

T

RN

TMP

NO

NN

N1

Data from tape

Data tape from PDS. 1020 repetitive-operation monitor program.

C }
X }

Sets of data from tape controlled by N1

NOTE.

Input of MM and T is in the order:

$$s-1$$

$$w_i^r \quad i = N, N-1, \dots, 1$$

$$s = 1, 2, \dots, N$$

$$t_i \quad i = N, N-1, \dots, 1$$

where N = sample size.

Figure 5.6.3

Off-line processing program (Repetitive operation case)

```
'BEGIN' 'COMMENT' ZLOGANALO2,PRICE,CSTF109;
'INTEGER' I,J,K,KK,S,N,NN,NO,RN,M,N1;
'REAL' FCOUNT,TMP;
'REAL' 'ARRAY' STAN,MEAN [1:2:1:5,160,1:2],MM [1:15,1:15,1:5],
T,F[1:15,1:5],SI,CF[1:5,1:60],A,B[1:5];
'INTEGER' 'ARRAY' SP[1:5,1:60],CL[5];
'PROCEDURE' EVALUATE;
'BEGIN' 'INTEGER' L;
'REAL' A1,A2,A3,A4,SS;
'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
'BEGIN' A1:=A2:=A3:=A4:=SS:=0;
'FOR' L:=1 'STEP' 1 'UNTIL' KK 'DO'
'BEGIN' SS:=SS+CF[L,M];
A1:=A1+SS*F[L,J];
A2:=A2+SS↑2*F[L,J];
A3:=A3+SS↑3 *F[L,J]↑2;
A4:=A4+SS↑2*F[L,J]↑2;
'END';
ALJ]:=(A1*A2/KK-A3)/(A4-A1↑2/KK);
BJ]:=(A2+ALJJ*A1)/KK;
'END';
'END';
SELECTINPUT (0);
SELECTOUTPUT(0);
NEWLINE(1);
WRITETEXT (('DATA%ANALYSIS%PROGRAM'));
WRITETEXT (('('LC')'-----'));
'FOR' K:=1 'STEP' 1 'UNTIL' 5 'DO'
'BEGIN' KK:=K*3;
'FOR' I:=1 'STEP' 1 'UNTIL' KK 'DO'
'FOR' J:=1 'STEP' 1 'UNTIL' KK 'DO'
MM[I,J,K]:=READ;
'FOR' I:=1 'STEP' 1 'UNTIL' KK 'DO'
T[I,K] := READ;
'END';
RN:=READ;
TMP:=READ;
NO:=READ;
NN:=READ;
N1:=READ;
NEWLINE(4);
WRITETEXT (('RUN%NUMBER=%'));
PRINT (RN,3,0);
```



```

WRITETEXT('('('LC')'-----'))';
NEWLINE(2);
WRITETEXT('('TIME%MARKER%PULSE%SETTING=%')');
PRINT(TMP,2,1);
NEWLINE(1);
WRITETEXT('('NUMBER%OF%CHANNELS=%')');
PRINT(NO,2,0);
NEWLINE(1);
WRITETEXT('('DATA%VALUES%PER%CHANNEL=%')');
PRINT(NN,3,0);
NEWLINE(1);
WRITETEXT('('SETS%OF%READINGS=%')');
PRINT(N1,2,0);
SELECTINPUT(3);
'BEGIN' 'REAL' 'ARRAY' XL1:15,1:NO1;
'REAL' RSI;
'FOR' K:=1 'STEP' 1 'UNTIL' 5 'DO'
'BEGIN'
C[K]:=READ;
'IF' C[K]=0 'THEN' 'GOTO' CONTINUE;
KK:=K*3;
RSI:=0;
'FOR' M:=1 'STEP' 1 'UNTIL' C[K]'DO'
'BEGIN'
RSI:=RSI+TMP;
SILK,M]:=RSI;
CF[K,M]:=T[1,K]/SILK,M];
SP[K,M]:=ENTIER((T[KK,K]/T[1,K])*SILK,M]);
'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
'BEGIN'
STAN[1,K,M,J]:=STAN[2,K,M,J]:=0;
MEAN[1,K,M,J]:=MEAN[2,K,M,J]:=0;
'END';
'END';
CONTINUE:'END';
'FOR' N:=1 'STEP' 1 'UNTIL' N1 'DO'
'BEGIN'
'FOR' K:=1 'STEP' 1 'UNTIL' 5 'DO'
'BEGIN' KK:=K*3;
'FOR' M:=1 'STEP' 1 'UNTIL' CLKJ 'DO'
'BEGIN' 'FOR' I:=1 'STEP' 1 'UNTIL' KK 'DO'
'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
X[I,J]:=READ;
'FOR' J:=1 'STEP' 1 'UNTIL' NO'DO'
'FOR' S:=1 'STEP' 1 'UNTIL' KK 'DO'
'BEGIN' F[S,J]:=0;
'FOR' I:=1 'STEP' 1 'UNTIL' KK 'DO'
F[S,J]:=F[S,J]+MM[S,I,K]*X[I,J]/CF[K,M];
'END';
EVALUATE;
'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
'BEGIN'
MEAN[1,K,M,J]:=MEAN[1,K,M,J]+A[J];
MEAN[2,K,M,J]:=MEAN[2,K,M,J]+B[J];
STAN[1,K,M,J]:=STAN[1,K,M,J]+A[J]2;
STAN[2,K,M,J]:=STAN[2,K,M,J]+B[J]2;
'END';
'END';
'END';
'END';
'FOR' N:=1 'STEP' 1 'UNTIL' 2 'DO'

```

```

'BEGIN'
NEWLINE(4);
WRITETEXT ('('TIME%CONSTANT%')');
PRINT(N,1,0);
WRITETEXT ('('('1C')'-----')');
NEWLINE(3);
'FOR' K:=1 'STEP' 1 'UNTIL' 5 'DO'
'BEGIN' KK:= K*3;
WRITETEXT ('('QUADRATURE%SIZE=%')');
PRINT(KK,2,0);
WRITETEXT ('('('1C')'-----')');
NEWLINE(2);
SPACE (25);
WRITETEXT ('('CHANNEL%1('10S')'CHANNEL%2')');
NEWLINE (1);
SPACE(25);
WRITETEXT ('('-----'('10S')'-----')');
NEWLINE(1);
WRITETEXT ('(%%SP%%SI%%MEAN%%STD.DEV.
%%MEAN%%STD.DEV.')');
NEWLINE(2);
'FOR' M:=1 'STEP' 1 'UNTIL' C[K]'DO'
'BEGIN'
PRINT(SPI[K,M],3,0);
PRINT(SII[K,M],2,1);
'FOR' J:=1 'STEP' 1 'UNTIL' NO 'DO'
'BEGIN'
STAN[N,K,M,J]:=SQRT (STAN[N,K,M,J]-MEAN[N,K,M,J]2/N1)/(N1-1);
MEAN[N,K,M,J]:=MEAN[N,K,M,J]/N1;
PRINT(MEAN[N,K,M,J],1,5);
PRINT(STAN[N,K,M,J],0,5);
SPACE(3);
'END';
NEWLINE(1);
'END';
NEWLINE(2);
'END';
'END';
NEWLINE(6);
WRITETEXT ('('('6S')'-----')');
'END';
'END';

```

5.7 Support programs.

An on-line statistical program was written to evaluate the mean and standard deviation of the added noise from the pseudo-random noise generator. Its operation was very simple and can be understood by inspection of the block diagram shown in figure 5.7.1. Results are shown in Appendix II d.

A small Algol program was written to test the tape interface between the PDS. 1020 and the ICL. 1905. Known numbers were punched onto tape from the PDS. 1020; the tape was read and the numbers printed out by the ICL. 1905. The program is self-explanatory and is listed in figure 5.7.2. A variable reference table and the input data format are shown in tables 5.7.2 (a) and 5.7.2(b). Results are shown in Appendix II e.

Figure 5.7.1.

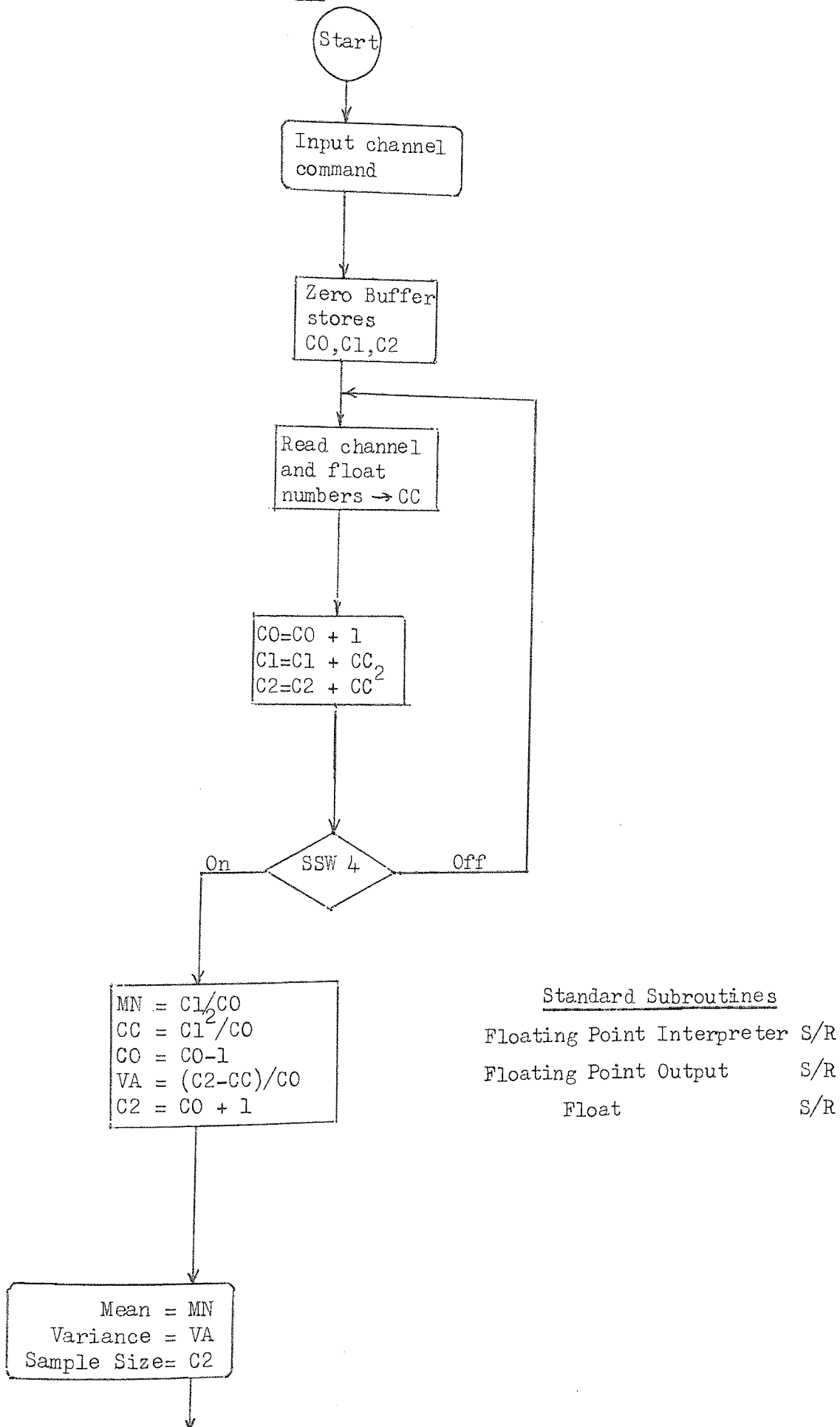
On-line statistical program.

Table 5.7.2 (a).Variable Reference table - READERTEST.

Variable Name	Reference
I,K	General counters
NUMBER	Numbers read from PDS. 1020 tape.

Table 5.7.2 (b).Data input format - READERTESTData from tape.

PDS. 1020	output tape.
NUMBER	twenty times.

Figure 5.7.2.Interface Test program.

```
'BEGIN' 'COMMENT' READERTEST, PRICE, CESTF109;
'REAL' 'ARRAY' NUMBER[1:100];
'INTEGER' I, K;
SELECTOUTPUT (0);
K:= 20;
NEWLINE (2);
SELECTINPUT(3);
'FOR' I=1 'STEP' 1 'UNTIL' K 'DO'
'BEGIN'
NUMBER[I]:= READ;
PRINT(NUMBER[I],1,4);
NEWLINE(1);
'END';
NEWLINE(2);
'END';
```

Chapter 6

In this chapter the results from the various programs are discussed, together with the methods of analysis, where relevant. An overall analysis of the work, in the light of its possible application to real problems, is made and the direction further work should take discussed.

6.1 The general logging program.

This program was written primarily to assist with the commissioning and calibration of on-line instruments on the evaporator. Its other uses were for monitoring the dynamic response of the evaporator, or logging steady state values.

A typical print out is shown in Appendix II a.

6.2 Support programs.

Before discussing the on-line identification program results, some support program results will be briefly mentioned.

6.2.1 Off-line identification programs:

These were primarily written to test, under ideal conditions, the identification technique for values of the parameters to be used in the on-line identification work. They were also particularly useful in aiding the debugging of on-line programs for the PDS. 1020, which were written in Assembler language. Some results are shown in Appendix II b.

6.2.2 On-line statistical analysis program:

This program was used to evaluate the statistical characteristics of the pseudo-random noise generated on the HY-48. The results are shown in Appendix II d and are tabulated against the required noise generator parameter settings.

6.2.3 Tape interface test routine:

This was used to verify that the tape code conversion routine in PDS. 1020 monitor program was working satisfactorily. Results agreed with the numbers stored in the PDS. 1020 memory.

6.3 The on-line identification program.

This was the first program used to study the identification technique. Six specimen sets of results are shown in Appendix IIc, together with their associated mean and standard deviations.

The NUMBER OF QUADRATURE POINTS refers to the sample size. TIME FACTOR converts Bellman's time units to seconds for the numerical estimation of the Laplace transform, while TIME CORRECTION FACTOR does the equivalent conversion for the system's mathematical model. The CONTROL SIGNAL INITIATE AMPLITUDE gives the required size of the disturbance on the control channel in mV which will initiate the identification routine.

Notice that the results are printed in pairs. The first number of each pair is the parameter estimate from the control channel readings and the second number is the parameter estimate from channel 21, readings which can be corrupted by noise. The parameter settings for which runs were carried out are tabulated together with the results in Appendix II c.

Considering run 1, when neither channel has any added noise, it can be seen that the second results are about 2.5% higher than the first, overall. This difference is due to the time lag between scanning the first channel and the second, and is a consequence of the low scanning speed of the logging system combined with the slowness of the PDS. 1020 cycle time.

Later results will show that considerably higher sampling periods are preferred for more accurate parameter estimation and so the effect of scanning speed will be minimised. It would certainly be an important factor, however, where several channels are going to be scanned simultaneously.

Runs 2-6 show the effect of increasing the added noise levels at a set sampling period and the effect of varying the sampling period,

the added noise levels being kept constant.

The effect of increasing the noise levels is to increase the value of the standard deviation of the results, showing increased spread of the parameter estimation results. Increasing the sampling period decreases the standard deviation of the results, showing increased accuracy of estimation. The means of the parameter estimates are reasonably accurate in all cases.

A point to be considered concerns the setting of the logging system clock timer. In the author's work it was set invariably to 1 second. However, there is no reason why this setting should not be made smaller or larger. Obviously, the larger the setting the less accurate the approximation for t_1 and vice versa. The choice made by the author was arbitrary but made under the limitations of computing speed of the PDS. 1020 and the scanning speed of the logging system.

If the clock timer setting is set too low, the program may miss the clock timer increment. About $\frac{1}{2}$ second is required for the program to scan two channels and carry out the associated computation for the numerical transformation of the results, hence 1 second is a reasonable choice.

Another point to consider and which is connected to what has already been said, is the initiation of the identification routine. The identification routine can be initiated at any time during a sampling interval and the clock timer count will commence from the clock timer pulse immediately following the initiation signal. This means that the timer pulse count routine can be delayed anything up to the value of the sampling interval. Thus further inaccuracies are introduced.

From the point of view of identifying chemical plant models, this is not too serious, as the time constants are generally large and, as mentioned already, identification is more accurate with large sampling periods, where the effect of this error is minimised. However, the larger the clock timer setting, the greater the errors that are introduced.

Despite the errors induced by limitations on the sampling time accuracy, the results of this program are excellent. They show that the identification technique can be used accurately in on-line work with computation time down to a minimum.

However, the amount of data that this particular computer can process on-line is limited, due to the lack of a proper interrupt facility and the slow cycle-time. Having proved that the technique can be applied under realistic conditions, this computer was hence used only as a sampling computer, the data being punched onto tape. Processing of this tape was carried out off-line.

The remainder of the work done by the author is concerned with the characteristics of the identification technique under differing conditions. However, the limitations on sampling time accuracy and scanning rate are adhered to, such that the aim of providing information about the applicability of the technique under real conditions is not lost sight of.

6.4 On-line monitoring, off-line processing programs.

The single-cycle program results are of academic interest only, the repetitive-operation programs giving more valuable results. However, the program and results (Appendix II e) are shown as an indication of how the final configuration developed from the initial on-line program.

Results from the repetitive-operation program are shown in Appendix III. These results will be discussed in the following pages.

6.4.1 Method of analysis:

Given the results in Appendix III, the problem then arises as to how best analyse the large amount of data available.

First consideration was given to the means of the parameter estimates under different conditions and graphs were drawn showing these means against the sampling period expressed in terms of the system time constant, $\tau = \frac{1}{a}$. The means were plotted as percentage deviations from the true parameter setting. Only a sample size of 3 was considered, as

there were insufficient data from the other sample sizes for reasonable analysis due to equipment limitations.

These graphs are shown in Appendix IV, graphs 22-33. Graphs 22-30 show the results of the estimation of a for the model with a known forcing function, whilst graphs 31-33 show those for the model with an unknown forcing function.

To facilitate the interpretation of the results in terms of noise levels, sampling periods, system parameters, forcing function amplitude and sample sizes, graphs were drawn of the standard deviation of the estimated value of the parameter under consideration against the standard deviation of the added noise for various sampling period lengths and differing sample sizes. These graphs are shown in Appendix IV, graphs 1-21.

Two sets of confidence limits were drawn on the graphs. Specimen calculations for these confidence limits are shown in Appendix I b. The first set, designated C.L.¹, referred to the confidence with which it could be assumed that the mean of the sets of parameter estimations under the particular conditions operating was within 10% of the true population mean. These confidence limits were used as a check on the estimated means for each noise level.

The second set of confidence limits, designated C.L.², referred to the confidence with which it could be assumed that a single parameter estimation under the particular conditions operating was within 10% of the population mean.

The value of 10% was chosen since a sensitivity analysis showed that a 10% error in the estimation of a or b was equivalent to a 10% error in system response to a step input (Appendix I a). The figure of 10% limit on response accuracy was chosen arbitrarily after discussion with workers on related problems in industry.

Note that the amplitude of the forcing function and the model

parameter are being estimated simultaneously.

Reproducibility of the results can be assessed by comparing runs 105 and 106, both run under identical conditions. The two sets of results showed similar trends.

6.4.2 Discussion of results:

By inspection of the graphs showing means plotted against sampling period in terms of system time constant, τ (graphs 22-33), the following points may be noted.

Known forcing function.

(1) The results for the noise-free channel show regularly shaped curves with common characteristics.

(2) These characteristics show a gradual increase in accuracy of estimation with increasing sampling period. The curves show a turning point or point of inflection at a sampling period of about 7τ , after which the rate of change of slope of the curve begins to increase again.

(3) The accuracy of the estimations at this point is not 100% but show deviations of between 1% and 8%.

(4) The results for the noisy channel show that the spread of the results increases with a decrease in forcing function amplitude and also with a decrease in model parameter size.

Unknown forcing function.

(1) These results showed a greater spread than those for the known forcing function. This increased spread was probably due to the fact that both the input and output functions were approximated in the Laplace domain, whereas with the forcing function of known form only the output function was approximated in the Laplace domain.

(2) Results were more accurate for lower forcing function amplitudes, however, for more accurate assessment, results for larger

sampling periods are required.

From the above observations for the known forcing function case it may reasonably be concluded that the errors in estimation at the points of inflection of the curves are due to equipment and sampling limitations and that these points in fact show the sampling periods at which estimation is at its most accurate. From the off-line support programs, (Appendix II b), it may be shown that the results of estimations in the ideal case are accurate to within 1%. It can be seen from the graphs that reasonably accurate results may be obtained with sampling periods in the range 3-12%.

Notice that for the case of the unknown forcing function, actual monitoring of the input and output signals was delayed for about 5 seconds due to the time taken for the system under identification to respond to the forcing function. This may have affected the accuracy of the results obtained, however, further work needs to be done in this area before any final conclusion can be reached.

Further, the forcing function final amplitude was chosen to give three distinct final response amplitudes for each model, these amplitudes being 0.1, 0.4 and 0.7.

Attention will now be turned to the analysis of the graphs of standard deviation of the estimates against noise level standard deviation. (Graphs 1-21). Discussion of these graphs may be separated into three sections: estimation of the model parameter for the model with known forcing function; estimation of the step amplitude in this case; and estimation of the model parameter where the forcing function has unknown form.

(a) Estimation of the model parameter, a, where the form of the forcing function is known. (Graphs 1 - 9).

Consideration of the graphs showed that the optimum sampling period appeared to be in the order of 7-7.5% , which compares well with

that estimated from the graphs of the means. Around this sampling period the standard deviations were lower than at other sampling periods.

The effect of sampling period length appeared to vary in a cyclic fashion, other reasonable sampling periods being 3-3.5 and 11-11.5.

This effect of sampling period length was accentuated by an increase in sample size. This was particularly the case with a sample size of 9, the standard deviations of the estimated values being much greater at sampling period lengths other than 7-7.5.

Generally, forcing functions generating larger final response amplitudes gave more accurate results than those for smaller response amplitudes. The exception was the case for a sample size of 3, where the converse appeared to hold. This exception is probably due to numerical rounding error occurring in the calculation of the parameter caused by the large time scaling factors encountered for this sample size.

The C.L.¹ lines showed that an insufficient number of estimates per point had been taken for the computed means to have any real significance, except for the low noise level or noise-free cases. Similarly, the C.L.² lines showed that too wide a range of noise levels had been used for a parameter estimate from a single sample to be within 10% of the true parameter value. The upper bound on the noise level should have been that with a standard deviation of about 0.025.

However, some general information could be deduced from the results. Table 6.1 gives the approximate maximum noise levels that can be tolerated for small sample sizes with particular values of the final response, $\frac{b}{a}$. These values were obtained by inspection of the graphs.

(b) Estimation of the step forcing function amplitude for the case where the form of the forcing function is known. (Graphs 10-18).

The characteristics of the estimation of the step forcing function amplitude were similar to those of the estimation of the model parameter, a , however the standard deviations of the results were much

more dependent on the size of the final response, $\frac{b}{a}$.

For small values of $\frac{b}{a}$ the standard deviations varied widely with sampling period, while at large values the standard deviation was smaller and practically constant. From these results it appeared that the optimum sampling period for small values of $\frac{b}{a}$ was nearer 4τ .

Table 6.1 gives approximate allowable standard deviation limits for the added noise levels for the estimation of b , deduced by inspection of the graphs.

(c) Estimation of the model parameter, a , in the case of an unknown forcing function. (Graph 19-27).

Results were only obtained in this case for $a = 0.01$, i.e. sampling periods of up to 4τ . The effects of sampling period length within this range, however, appeared to be similar to those in the case of the known forcing function.

Again, the graphs showed that the range of noise levels considered was too wide. However, it appeared from the results that the noise levels that could be tolerated for a value of $\frac{b}{a} = 0.1$ were higher than those for higher values of $\frac{b}{a}$. The standard deviation of the noise levels that could be tolerated for values of $\frac{b}{a} = 0.7$ and 0.4 was approximately 0.002 , whilst that for $\frac{b}{a} = 0.1$ was approximately 0.006 .

Table 6.1

Known forcing function, estimation of a .

$\frac{b}{a}$	Maximum allowable noise level standard deviation
0.7	0.1
0.4	0.007
0.1	0.002

Known forcing function, estimation of b.

$\frac{b}{a}$	Maximum allowable noise level standard deviation
0.7	0.01
0.4	0.008
0.1	0.006

6.5 Further work

The work done by the author has been concerned with the identification of two very simple models, however a considerable amount of information has been gained about the operation of the identification technique. The main advance of the work has been the development of an approach to the study of non-sequential identification techniques in general.

The programs developed can be very easily modified to study the identification technique for a variety of models under widely varying conditions and the identification of particular models can be studied in considerable depth under very realistic conditions.

It is apparent that the technique's only drawback is the limitation on the noise levels. This, it is considered, would not be a serious limitation in many cases. The unequal interval sampling period would not be a problem on chemical plant models where the system time constants are large.

One possible way of dealing with a system containing severe noise would be the combination of this technique with correlation analysis techniques, system parameters being identified from a knowledge of the impulse response curve using the convolution integral and the numerical Laplace Transform technique. This method would probably be very accurate.

The next stage in the study of the

usefulness of the identification technique would be its application to a real process problem. The plant used will obviously be the double-effect evaporator. As it is a pilot-scale plant, it is ideal for the purposes of this study.

A simulated model would be set up on the HY-48 with time constants set in the region of the true time constants, and the identification of this model tested using the already prepared software. Having assessed the optimum conditions for the operation of the identification technique under conditions similar to those on the evaporator, the technique could be used for system modelling with considerable confidence.

The technique is, of course, applicable only to linearised models, these being set up around the operating region. The use of approximate models for non-linear systems introduces another problem, that of the choice of the form of the approximating model. This could be done by choosing the model whose sum of squares of the residuals is least.

In the author's work all models were run at their real-time speeds, no time-scaling of the models or monitor scanrate being attempted. This was due to the slow cycle time of the PDS. 1020 and also, more important, to the limited scanning speed of the MDP. 200 logging system. Neither could a true on-line program be written due to the lack of interrupt system on the PDS. 1020. A more modern computer with full interrupt capability and a more rapid cycle time would alleviate the first problem and eliminate the second. Time-scaling capability would still be limited by the logging system scanning rate.

Given a high speed logging system and also some interfacing between the HY-48 and the digital computer, the results so laboriously obtained by the author could be carried in a matter of seconds. Results from the monitor program could be stored on a disc until a large number

of runs had been carried out, and then processed by a separate program.

Despite all the drawbacks, however, meaningful results have been obtained which should prove useful to anyone intent on using this particular non-sequential identification technique.

1954-1955

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Appendices

Appendix 1(a) Specimen derivation of the sensitivity of the response of a first order system to system parameter variations

Given a first order system,

$$\frac{dx}{dt} + ax = b, \quad x(0) = 0,$$

where x is the state variable and a and b are system parameters,

the solution is given as

$$x = \frac{b}{a} (1 - e^{-at})$$

Now,

$$\frac{\partial x}{\partial a} = \frac{b}{a} \left[t e^{-at} - \frac{1}{a} (1 - e^{-at}) \right]$$

$$\text{and } \Delta x = \frac{\partial x}{\partial a} \Delta a$$

$$\text{or } \frac{\Delta x}{x} = \frac{\partial x}{\partial a} \frac{\Delta a}{x}$$

$$= \frac{\frac{b}{a} \left[t e^{-at} - \frac{1}{a} (1 - e^{-at}) \right] \Delta a}{\frac{b}{a} (1 - e^{-at})}$$

$$= \left[\frac{(1+at)e^{-at} - 1}{1 - e^{-at}} \right] \frac{\Delta a}{a} \dots\dots\dots(1)$$

$$\text{Now } \frac{\partial}{\partial t} \left(\frac{\Delta x}{x} \right) = \Delta a \left[\frac{at(at-1)e^{-3at}}{1 - e^{-at}} \right]$$

At the turning points,

$$\frac{\partial}{\partial t} \left(\frac{\Delta x}{x} \right) = 0$$

Solving the above, the turning points are found to be at

$$t = 0$$

$$t = \infty$$

$$t = \frac{1}{a}$$

Equation (1) will now be solved for these values of t.

$$\text{At } t = \frac{1}{a}, \quad \frac{\Delta x}{x} = -0.4179 \quad \frac{\Delta a}{a}$$

$$\text{At } t = 0, \quad \frac{\Delta x}{x} = 0$$

$$\text{At } t = \infty, \quad \frac{\Delta x}{x} = -\frac{\Delta a}{a}$$

By inspection it can be seen that the maximum fractional variation in x for a given variation in a will be given by:

$$\frac{\Delta x}{x} = -\frac{\Delta a}{a}$$

Similarly, it may be shown for variation in parameter b,

$$\frac{\Delta x}{x} = \frac{\Delta b}{b}$$

(b) Specimen calculation of the standard deviation limit for confidence limits of 95%, given a permissible error of 10% in the result

From Brownlee (54),

$$u_{0.975} = 1.96$$

$$u_{0.025} = -1.96$$

Given a 10% allowable error on a parameter value of 0.01,

then

$$0.001 = 1.96 \frac{\sigma}{\sqrt{N}}$$

where σ = standard deviation

N = No. of results

For $N = 15$,

$$0.001 = 1.96 \frac{\bar{\sigma}}{\sqrt{15}}$$

$$\text{and } \bar{\sigma} = 2 \times 10^{-3}$$

(c) Specimen derivation of the unknown model parameter for a simple model

Given a model,

$$\frac{dx}{dt} + ax = a, \quad x(0) = 0$$

where a is unknown.

Transforming this equation,

$$s x(s) + ax(s) = \frac{a}{s}$$

If \bar{x} is obtained from numerical transformation of values of $x(t)$, the sum of the squares of the residuals may be written:

$$S = \sum_{s=1}^N \left\{ s^2 x(s) + a s x(s) - a \right\}^2$$

Hence,

$$\begin{aligned} \frac{\partial S}{\partial a} &= \sum_{s=1}^N 2 \left\{ s^2 x(s) + a s x(s) - a \right\} (s x(s) - 1) \\ &= 0 \end{aligned}$$

Simplifying,

$$\underline{a = \sum_{s=1}^N \frac{s^2 x(s) \{ s x(s) - 1 \}}{(s x(s) - 1)^2}}$$

(d) Specimen calculation to show the effect of rounding of the sampling time on the accuracy of the measured value of x

Consider the model,

$$\frac{dx}{dt} + ax = b, \quad x(0) = 0.$$

The rate of change of x with time is a maximum at $t = 0$,

and falls off thereafter. It can be expected that the worst error in the measured value of x will be at the second sampling point, where rounding of the sampling time first takes place, and where b is large.

The value of x will be computed for the true and rounded values of t_2 for the model above, given a sample size of 3, $\frac{b}{a} = 0.7$, and $a = 0.1$ and 0.3 . The percentage error in x can then be calculated.

$$(I) \frac{dx}{dt} + 0.01 x = 0.007$$

From Bellman (1), for a sample size of 3,

$$t_1 = 0.119574$$

$$t_2 = 0.693147$$

Hence, if t_1 is scaled to 1 second, t_2 will be scaled to $0.693147 / 0.119574 = 5.7968$ seconds. The rounded value of t_2 will then be 6 seconds.

The solution of the model, given $a = 0.01$, is:

$$x = 0.7 (1 - e^{-0.01t})$$

Substituting for t with both the true and rounded values of t_2 ,

$$x = 0.039424 \quad (t_2 \text{ true})$$

$$x = 0.040765 \quad (t_2 \text{ rounded})$$

The percentage error in x is 3.4%. This is with the minimum time-scaling factor possible.

For $a = 0.3$,

$$x = 0.111736 \quad (t_2 \text{ true})$$

$$x = 0.115311 \quad (t_2 \text{ rounded})$$

The percentage error in x is 3.2%

This can be considered negligible in both cases, as considerably larger time-scaling factors are used in practice, giving sampling intervals of 10 - 20 seconds.

Appendix II(a) Specimen printout for general logging program

This printout shows the operation of the general logging program, initially taking scaled voltage readings for 8 thermocouples on the double-effect evaporator, and then inputting calibration factors and logging the true temperatures ($^{\circ}\text{F}$)

 General Logging Program

Filter (In or No)?: No

Input from Scan or K/bd?: K/bd

First Channel No.: 20

Last Channel No.: 27

GAINS

20	21	22	23	24	25
26	27				
1000	1000	1000	1000	1000	1000
1000	1000				

CHANNEL READINGS

20	21	22	23	24	25
26	27				
0.600	1.139	0.647	1.824	1.480	1.489
1.787	1.144				
0.600	1.133	0.638	1.800	1.430	1.459
1.764	1.157				
0.594	1.147	0.644	1.826	1.450	1.457
1.780	1.199				
0.599	1.150	0.670	1.846	1.467	1.500
1.818	1.160				
0.599	1.150	0.671	1.841	1.428	1.470
1.848	1.230				
0.600	1.148	0.603	1.841	1.452	1.590
1.853	1.216				

0.600	1.152	0.663	1.838	1.409	1.408
1.750	1.145				
0.600	1.157	5.959	1.830	1.417	1.413
1.720	1.067				

CALIBRATION FACTORS (INPUT BASES, THEN GRADIENTS).

20	21	22	23	24	25
26	27				
32.	32.	32.	32.	32.	32.
32.	32.				
45.	45.	45.	45.	45.	45.
45.	45.				

First Channel No.: 20

Last Channel No.: 27

GAINS

20	21	22	23	24	25
26	27				
1000	1000	1000	1000	1000	1000
1000	1000				

CHANNEL READINGS

20	21	22	23	24	25
26	27				
58.955	83.165	61.655	112.37	96.17	99.905
115.205	85.685				
59.	83.615	61.43	114.305	97.88	98.6
111.74	83.3				
58.91	83.3	61.97	113.36	97.205	101.435
116.6	86.855				
58.955	83.3	61.745	113.9	98.33	98.285
112.685	85.955				
58.505	83.525	60.665	112.865	97.835	100.22
116.015	88.43				
58.505	83.165	61.835	113.72	96.485	96.8
110.66	83.75				
58.91	83.39	62.06	113.495	96.08	96.8
111.2	83.66				
58.955	83.57	61.7	113.855	98.465	98.555
113.	86.855				

58.46 110.3	83.435 83.3	62.195	113.81	96.305	96.305
59. 112.145	82.58 85.1	61.07	113.045	95.72	96.8
58.685 113.	83.705 85.415	60.8	113.45	98.51	99.365

(b) Off-line parameter estimation results

(I) Model with known forcing function

NOTE: The values of time scale used refer to initial sampling interval values as shown in the following table.

Time Scale	Sampling Interval
41.8151	5
83.6302	10
167.2604	20

Modelling Technique Test Program

No. of Quadrature Points: 03

Time Scale: .83630200+ 2+

Input Time Constants!

True Time Constants:

.10000000+ 1-

.70000000+ 2-

Estimated Time Constants:

.10041194+ 1-

.70073393+ 2-

Input Time Constants!

True Time Constants:

.10000000+ 1-

.40000000+ 2-

Estimated Time Constants:

.10040775+ 1-

.40041370+ 2-

Input Time Constants!

True Time Constants:

.10000000+ 1-
.10000000+ 2-

Estimated Time Constants:

.10048921+ 1-
.10012953+ 2-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.14000000+ 1-

Estimated Time Constants:

.19992566+ 1-
.13998410+ 1-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.80000000+ 2-

Estimated Time Constants:

.19993697+ 1-
.79993086+ 2-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.20000000+ 2-

Estimated Time Constants:

.19993650+ 1-
.19998249+ 2-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.21000000+ 1-

Estimated Time Constants:

.29991335+ 1-
.20995507+ 1-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.12000000+ 1-

Estimated Time Constants:

.29992992+ 1-
.11997814+ 1-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.30000000+ 2-

Estimated Time Constants:

.30004058+ 1-
.30000905+ 2-

Time Scale: .16726040+ 3+

Input Time Constants!

True Time Constants:

.10000000+ 1-
.70000000+ 2-

Estimated Time Constants:

.99966216+ 2-
.69993203+ 2-

Input Time Constants!

True Time Constants:

.10000000+ 1-
.40000000+ 2-

Estimated Time Constants:

.99968740+ 2-
.39996593+ 2-

Input Time Constants!

True Time Constants:

.10000000+ 1-
.10000000+ 2-

Estimated Time Constants:

.10009785+ 1-
.10005325+ 2-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.14000000+ 1-

Estimated Time Constants:

.20027238+ 1-
.14013866+ 1-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.80000000+ 2-

Estimated Time Constants:

.20028408+ 1-
.80082236+ 2-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.20000000+ 2-

Estimated Time Constants:

.20048178+ 1-
.20033208+ 2-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.21000000+ 1-

Estimated Time Constants:

.30857521+ 1-
.21485905+ 1-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.12000000+ 1-

Estimated Time Constants:

.30856376+ 1-
.12277325+ 1-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.30000000+ 2-

Estimated Time Constants:

.30895676+ 1-
.30721859+ 2-

Time Scale: .41815100+ 2+

Input Time Constants!

True Time Constants:

.10000000+ 1-
.70000000+ 2-

Estimated Time Constants:

.10676026+ 1-
.70706946+ 2-

Input Time Constants!

True Time Constants:

.10000000+ 1-
.40000000+ 2-

Estimated Time Constants:

.10678489+ 1-
.40405910+ 2-

Input Time Constants!

True Time Constants:

.10000000+ 1-
.10000000+ 2-

Estimated Time Constants:

.10694771+ 1-
.10104647+ 2-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.14000000+ 1-

Estimated Time Constants:

.20081711+ 1-
.14014526+ 1-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.80000000+ 2-

Estimated Time Constants:

.20082154+ 1-
.80083590+ 2-

Input Time Constants!

True Time Constants:

.20000000+ 1-
.20000000+ 2-

Estimated Time Constants:

.20098957+ 1-
.20026302+ 2-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.21000000+ 1-

Estimated Time Constants:

.29961091+ 1-
.20991337+ 1-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.12000000+ 1-

Estimated Time Constants:

.29961288+ 1-
.11995081+ 1-

Input Time Constants!

True Time Constants:

.30000000+ 1-
.30000000+ 2-

Estimated Time Constants:

.29975366+ 1-
.29993499+ 2-

(II) Model with unknown forcing function

Input Signal Final Amplitude = 3.50000& -4

Input Signal Time Constant = 5.00000& -2

System Time Constant = 1.00000& -2

Time Scale		Estimate	
8.36302&	0	2.05623&	-2
1.67260&	1	1.34435&	-2
2.50891&	1	1.15021&	-2
3.34521&	1	1.07446&	-2
4.18151&	1	1.03965&	-2
5.01781&	1	1.02198&	-2
5.85412&	1	1.01255&	-2
6.69042&	1	1.00763&	-2
7.52672&	1	1.00548&	-2

INPUT	OUTPUT
0.00275	0.01441
0.00661	0.21958
0.00700	0.55905

8.36302&	1	1.00523&	-2
9.19932&	1	1.00634&	-2
1.00356&	2	1.00847&	-2
1.08719&	2	1.01137&	-2
1.17082&	2	1.01484&	-2
1.25445&	2	1.01870&	-2
1.33808&	2	1.02284&	-2
1.42171&	2	1.02713&	-2
1.50534&	2	1.03150&	-2
1.58897&	2	1.03588&	-2

INPUT	OUTPUT
0.00442	0.04799
0.00698	0.42606
0.00700	0.67729

1.67260&	2	1.04019&	-2
1.75623&	2	1.04441&	-2

Input Signal Final Amplitude = 2.00000& -4

Input Signal Time Constant = 5.00000& -2

System Time Constant = 1.00000& -2

Time Scale		Estimate
8.36302&	0	2.05623& -2
1.67260&	1	1.34435& -2
2.50891&	1	1.15021& -2
3.34521&	1	1.07446& -2
4.18151&	1	1.03965& -2
5.01781&	1	1.02198& -2
5.85412&	1	1.01255& -2
6.69042&	1	1.00763& -2
7.52672&	1	1.00548& -2

INPUT

OUTPUT

0.00157
0.00378
0.00400

0.00823
0.12547
0.31945

8.36302&	1	1.00523& -2
9.19932&	1	1.00634& -2
1.00356&	2	1.00847& -2
1.08719&	2	1.01137& -2
1.17082&	2	1.01484& -2
1.25445&	2	1.01870& -2
1.33808&	2	1.02284& -2
1.42171&	2	1.02713& -2
1.50534&	2	1.03150& -2
1.58897&	2	1.03588& -2

INPUT

OUTPUT

0.00253
0.00399
0.00400

0.02742
0.24346
0.38702

1.67260&	2	1.04019& -2
1.75623&	2	1.04441& -2

Input Signal Final Amplitude = 5.00000& -5

Input Signal Time Constant = 5.00000& -2

System Time Constant = 1.00000& -2

Time Scale		Estimate
8.36302&	0	2.05623& -2
1.67260&	1	1.34435& -2
2.50891&	1	1.15021& -2
3.34521&	1	1.07446& -2
4.18151&	1	1.03965& -2
5.01781&	1	1.02198& -2
6.69042&	1	1.00763& -2
7.52672&	1	1.00548& -2

INPUT		OUTPUT
0.00039		0.00206
0.00094		0.03137
0.00100		0.07986
8.36302&	1	1.00523& -2
9.19932&	1	1.00634& -2
1.00356&	2	1.00847& -2
1.08719&	2	1.01137& -2
1.17082&	2	1.01484& -2
1.25445&	2	1.01870& -2
1.33808&	2	1.02284& -2
1.42171&	2	1.02713& -2
1.50534&	2	1.03150& -2
1.58897&	2	1.03588& -2

INPUT		OUTPUT
0.00063		0.00686
0.00100		0.06087
0.00100		0.09676
1.67260&	2	1.04019& -2
1.75623&	2	1.04441& -2

(c) On-line parameter estimation results

The following table gives the parameter settings used for the runs shown for the on-line identification program.

Parameter/Run Number	1	2	3	4	5	6
a	0.01	0.01	0.01	0.01	0.01	0.01
Logging System timer setting	1 sec.	1 sec.	1 sec.	1 sec.	1 sec.	1 sec.
Sampling interval	1 sec.	1 sec.	1 sec.	1 sec.	2 sec.	3 sec.
Sampling period in terms of τ , the system time constant	0.98	0.98	0.98	0.98	1.97	2.95
Time Scale(s domain)	29.114	29.114	29.114	29.114	58.228	87.342
Sample size	6	6	6	6	6	6
Standard deviation of noise level added to output signal	-	0.022	0.061	0.102	0.022	0.022
Control signal initiate amplitude	10mV	10mV	10mV	10mV	10mV	10mV

Below are tabulated the means and standard deviations of the results for each run.

Run No.	Control Channel		Channel with added noise	
	Mean	Std. Dev.	Mean	Std. Dev.
1	0.009230	0.3762×10^{-3}	0.009467	0.3518×10^{-3}
2	0.009498	0.3340×10^{-3}	0.009819	0.1768×10^{-2}
3	0.009515	0.4305×10^{-3}	0.009629	0.3863×10^{-2}
4	0.009788	0.4434×10^{-3}	0.012055	0.9520×10^{-2}
5	0.010202	0.2358×10^{-3}	0.010221	0.1382×10^{-2}
6	0.009975	0.2168×10^{-3}	0.009940	0.6429×10^{-3}

RUN 1

Model Prediction Program

No. of Quadrature Points: 6

First Channel No.: 20

Last Channel No.: 21

Time Factor: 29.114000

Time Correction Factor: 1.000000

Control Channel No.: 20

Control Signal Initiate Amplitude: 10

.93145471+ 2-
.96116927+ 2-

.97284775+ 2-
.98799628+ 2-

.88418877+ 2-
.90448345+ 2-

.96685988+ 2-
.98484331+ 2-

.93376397+ 2-
.96031080+ 2-

.91293358+ 2-
.94943949+ 2-

.88013756+ 2-
.90039026+ 2-

.95914662+ 2-
.97453907+ 2-

.92390656+ 2-
.95096152+ 2-

.86475051+ 2-
.89282127+ 2-

RUN 2

.96118984+ 2-
.12137147+ 1-

.96946659+ 2-
.10435789+ 1-

.96497135+ 2-
.97871255+ 2-

.94598714+ 2-
.10298429+ 1-

.99560235+ 2-
.10542517+ 1-

.95896004+ 2-
.98640466+ 2-

.88785248+ 2-
.11974697+ 1-

.95314616+ 2-
.93659491+ 2-

.96692325+ 2-
.99564119+ 2-

.99151255+ 2-
.11914341+ 1-

.93962476+ 2-
.72296875+ 2-

.98354502+ 2-
.11555172+ 1-

.89994342+ 2-
.79654233+ 2-

.89643365+ 2-
.66833690+ 2-

.93246358+ 2-
.75770344+ 2-

RUN 3

.96212466+ 2-
.99696851+ 2-

.99423444+ 2-
.29333094+ 2-

.90452589+ 2-
.58543011+ 2-

.10032761+ 1-
.11233868+ 1-

.10065765+ 1-
.12654260+ 1-

.99321944+ 2-
.49173272+ 2-

.99280172+ 2-
.91185641+ 2-

.88827597+ 2-
.38082822+ 2-

.93293658+ 2-
.14841365+ 1-

.98345239+ 2-
.86629673+ 2-

.96463328+ 2-
.14281872+ 1-

.90148447+ 2-
.10578705+ 1-

.92913917+ 2-
.93621794+ 2-

.92214306+ 2-
.14945129+ 1-

.89383681+ 2-
.11274339+ 1-

RUN 4

.10123912+ 1-
.15028621+ 1-

.10125536+ 1-
.13300159+ 2-

.98101632+ 2-
.24621217+ 1-

.10061809+ 1-
.24718807+ 2-

.10268810+ 1-
.32696825+ 2-

.10503459+ 1-
.27194538+ 1-

.94338120+ 2-
.10251580+ 2-

.93419606+ 2-
.22112171+ 1-

.96665357+ 2-
.95116136+ 2-

.10074493+ 1-
.26559669- 2-

.91541857+ 2-
.15316400+ 1-

.99385890+ 2-
.13507531+ 1-

.89107664+ 2-
.98507384+ 2-

.98984413+ 2-
.15525824+ 1-

.95001057+ 2-
.22712085+ 1-

RUN 5

.99413214+ 2-
.11240015+ 1-

.10121732+ 1-
.93597143+ 2-

.10253683+ 1-
.91092300+ 2-

.10313011+ 1-
.11565080+ 1-

.10346159+ 1-
.11309642+ 1-

.10345173+ 1-
.11778555+ 1-

.10494682+ 1-
.10885906+ 1-

.10528091+ 1-
.94101922+ 2-

.97391199+ 2-
.76579530+ 2-

.99603497+ 2-
.11904252+ 1-

.10076720+ 1-
.94218161+ 2-

.10303443+ 1-
.90151194+ 2-

RUN 6

.97569615+ 2-
.94133644+ 2-

.98012787+ 2-
.10638204+ 1-

.96068039+ 2-
.99104217+ 2-

.98770757+ 2-
.98876236+ 2-

.97612296+ 2-
.96214486+ 2-

.98441511+ 2-
.10878114+ 1-

.10004658+ 1-
.97824053+ 2-

.98091048+ 2-
.92933810+ 2-

.10047882+ 1-
.94174036+ 2-

.10283155+ 1-
.97118834+ 2-

.10138201+ 1-
.94805277+ 2-

.10036719+ 1-
.97291849+ 2-

.10380806+ 1-
.10047422+ 1-

.10128422+ 1-
.96411920+ 2-

.10155764+ 1-
.11646678+ 1-

(d) Noise level calibrations

This table shows HY-48 pseudo-random noise generator settings against standard deviation of resultant noise, calculated by the on-line statistical analysis program. The mean of the noise was assumed zero. Specimen results are shown overleaf. The HY-48 digital clock speed was set at 10 cps.

K	$\frac{1}{T}$	Resultant Standard Deviation
0.1	0.1	0.022
0.3	0.1	0.061
0.5	0.1	0.106

Statistical Check.

Channel Command?

Mean: .35420560- 3-

Standard Deviation: .23203302+ 1-

Sample Size: .21300000+ 3+

Statistical Check.

Channel Command?

Mean: .30954166+ 2-

Standard Deviation: .62849814+ 1-

Sample Size: .23900000+ 3+

Statistical Check.

Channel Command?

Mean: .93748898+ 2-

Standard Deviation: .10695780+ 0-

Sample Size: .22600000+ 3+

Statistical Check.

Channel Command?

Mean: .13113861+ 2-

Standard Deviation: .21403573+ 1-

Sample Size: .20100000+ 3+

Statistical Check.

Channel Command?

Mean: .10136986- 2-

Standard Deviation: .61305706+ 1-

Sample Size: .21800000+ 3+

Statistical Check.

Channel Command?

Mean: .15348837+ 3-

Standard Deviation: .10552279+ 0-

Sample Size: .21400000+ 3+

Statistical Check.

Channel Command?

Mean: .12301369+ 3-

Standard Deviation: .22903727+ 1-

Sample Size: .36400000+ 3+

Statistical Check.

Channel Command?

Mean: .24996655+ 2-

Standard Deviation: .58575494+ 1-

Sample Size: .29800000+ 3+

Statistical Check.

Channel Command?

Mean: .36171641+ 2-

Standard Deviation: .10695318+ 0-

Sample Size: .26700000+ 3+

(e) Results from single-cycle monitoring, off-line processing runsData Analysis ProgramRun Number = 19

Time marker pulse setting = 1.0

Number of channels = 2

Data values per channel = 400

Quadrature Size = 3

Sampling interval = 1.0

Channel number = 1

Time constant = 1.0244404266& -2:

Channel number = 2

Time constant = 6.7807126652& -3:

Sampling interval = 2.0

Channel number = 1

Time constant = 9.9813990807& -3:

Channel number = 2

Time constant = 1.3407521522& -2:

Sampling interval = 3.0

Channel number = 1

Time constant = 9.6999498829& -3:

Channel number = 2

Time constant = 1.1111033625& -2:

Sampling interval = 4.0

Channel number = 1

Time constant = 9.6719828306& -3:

Channel number = 2

Time constant = 8.6923691390& -3:

Sampling interval = 5.0

Channel number = 1

Time constant = 9.5969425987& -3:

Channel number = 2

Time constant = 7.9248990106& -3:

Sampling interval = 6.0

Channel number = 1

Time constant = 9.7445181079& -3:

Channel number = 2

Time constant = 9.1065439723& -3:

Sampling interval = 7.0

Channel number = 1

Time constant = 9.7563931284& -3:

Channel number = 2

Time constant = 1.0405835235& -2:

Sampling interval = 8.0

Channel number = 1

Time constant = 9.6503165722& -3:

Channel number = 2

Time constant = 1.0296432091& -2:

Sampling interval = 9.0

Channel number = 1

Time constant = 9.6666874492& -3:

Channel number = 2

Time constant = 9.8737959902& -3:

Sampling interval = 10.0

Channel number = 1

Time constant = 9.6636317177& -3:

Channel number = 2

Time constant = 9.3590941637& -3:

Sampling interval = 11.0

Channel number = 1

Time constant = 9.7017090654& -3:

Channel number = 2

Time constant = 9.2360758072& -3:

Sampling interval = 12.0

Channel number = 1

Time constant = 9.6826441280& -3:

Channel number = 2

Time constant = 8.9994727904& -3:

Sampling interval = 13.0

Channel number = 1

Time constant = 9.6260279660& -3:

Channel number = 2

Time constant = 8.7810457861& -3:

Sampling interval = 14.0

Channel number = 1

Time constant = 9.6165651812& -3:

Channel number = 2

Time constant = 9.1427579415& -3:

Sampling interval = 15.0

Channel number = 1

Time constant = 9.6407721994& -3:

Channel number = 2

Time constant = 9.1969696751& -3:

Sampling interval = 16.0

Channel number = 1

Time constant = 9.7081546145& -3:

Channel number = 2

Time constant = 1.016601215& -2:

Sampling interval = 17.0

Channel number = 1

Time constant = 9.7609766552& -3:

Channel number = 2

Time constant = 1.0287377151& -2:

Sampling interval = 18.0

Channel number = 1

Time constant = 9.6818327109& -3:

Channel number = 2

Time constant = 1.0641089805& -2:

Sampling interval = 19.0

Channel number = 1

Time constant = 9.7431351973& -3:

Channel number = 2

Time constant = 1.0238710134& -2:

Sampling interval = 20.0

Channel number = 1

Time constant = 9.7222698715& -3:

Channel number = 2

Time constant = 9.9596100194& -3:

Sampling interval = 21.0

Channel number = 1

Time constant = 9.7338619226& -3:

Channel number = 2

Time constant = 1.0233836267& -2:

Quadrature Size = 6

Sampling interval = 1.0

Channel number = 1

Time constant = 9.6601770848& -3:

Channel number = 2

Time constant = 6.8803824741& -3:

Sampling interval = 2.0

Channel number = 1

Time constant = 9.8083157230& -3:

Channel number = 2

Time constant = 1.0174617175& -2:

Sampling interval = 3.0

Channel number = 1

Time constant = 9.6610864479& -3:

Channel number = 2

Time constant = 1.0250291324& -2:

Sampling interval = 4.0

Channel number = 1

Time constant = 9.8299226174& -3:

Channel number = 2

Time constant = 9.4752872126& -3:

Quadrature Size = 9

Sampling interval = 1.0

Channel number = 1

Time constant = 9.6390480131& -3:

Channel number = 2

Time constant = 7.6905514897& -3:

(f) Tape interface test results

0.0000

0.0000

0.1111

-0.1111

0.2222

-0.2222

0.3333

-0.3333

0.4444

-0.4444

0.5555

-0.5555

0.6666

-0.6666

0.7777

-0.7777

0.8888

-0.8888

0.9999

-0.9999

Appendix III

This table gives the parameter settings for individual sets of runs using the repetitive operation program system. Runs 102 - 130 apply to the model with an *unknown* step forcing function, while runs 200 - 208 apply to the model with unknown forcing function. The logging system clock timer was set at 1 sec. for all these runs. Actual parameter settings used on the HY-48 are given in the table following this one. For runs 102-130 'Time Constant 1' is the parameter 'a', and 'Time Constant 2' parameter 'b'.

Run No.	Model Parameter a	Forcing function final amplitude	Noise Level standard deviation
102	0.01	0.007	0.022
103	0.01	0.007	0.061
104	0.01	0.007	0.106
105, 106	0.01	0.004	0.022
107	0.01	0.004	0.061
108	0.01	0.004	0.106
109	0.01	0.001	0.022
110	0.01	0.001	0.061
111	0.01	0.001	0.106
113	0.02	0.007	0.022
114	0.02	0.007	0.061
115	0.02	0.007	0.106
116	0.02	0.004	0.022
117	0.02	0.004	0.061
118	0.02	0.004	0.106
119	0.02	0.001	0.022
120	0.02	0.001	0.061
121	0.02	0.001	0.106
122	0.03	0.007	0.022
123	0.03	0.007	0.061
124	0.03	0.007	0.106
125	0.03	0.004	0.022
126	0.03	0.004	0.061
127	0.03	0.004	0.106
128	0.03	0.001	0.022
129	0.03	0.001	0.061
130	0.03	0.001	0.106
200	0.01	0.007	0.022
201	0.01	0.007	0.061
202	0.01	0.007	0.106
203	0.01	0.004	0.022
204	0.01	0.004	0.061
205	0.01	0.004	0.106
206	0.01	0.001	0.022
207	0.01	0.001	0.061
208	0.01	0.001	0.106

Potentiometer settings

Run No.	Model parameters			Noise level parameters	
	a	b	c	k	$\frac{1}{T}$
102	0.01	0.007	-	0.1	0.1
103	0.01	0.007	-	0.3	0.1
104	0.01	0.007	-	0.5	0.1
105	0.01	0.004	-	0.1	0.1
106	0.01	0.004	-	0.1	0.1
107	0.01	0.004	-	0.3	0.1
108	0.01	0.004	-	0.5	0.1
109	0.01	0.001	-	0.1	0.1
110	0.01	0.001	-	0.3	0.1
111	0.01	0.001	-	0.5	0.1
113	0.02	0.014	-	0.1	0.1
114	0.02	0.014	-	0.3	0.1
115	0.02	0.014	-	0.5	0.1
116	0.02	0.008	-	0.1	0.1
117	0.02	0.008	-	0.3	0.1
118	0.02	0.008	-	0.5	0.1
119	0.02	0.002	-	0.1	0.1
120	0.02	0.002	-	0.3	0.1
121	0.02	0.002	-	0.5	0.1
122	0.03	0.021	-	0.1	0.1
123	0.03	0.021	-	0.3	0.1
124	0.03	0.021	-	0.5	0.1
125	0.03	0.012	-	0.1	0.1
126	0.03	0.012	-	0.3	0.1
127	0.03	0.012	-	0.5	0.1
128	0.03	0.003	-	0.1	0.1
129	0.03	0.003	-	0.3	0.1
130	0.03	0.003	-	0.5	0.1
200	0.01	0.0035	0.05	0.1	0.1
201	0.01	0.0035	0.05	0.3	0.1
202	0.01	0.0035	0.05	0.5	0.1
203	0.01	0.002	0.05	0.1	0.1
204	0.01	0.002	0.05	0.3	0.1
205	0.01	0.002	0.05	0.5	0.1
206	0.01	0.0005	0.05	0.1	0.1
207	0.01	0.0005	0.05	0.3	0.1
208	0.01	0.0005	0.05	0.5	0.1

Data Analysis Program

Run Number = 102

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.05487	1.42358&	-2	0.07547	2.03769& -1
36	2.0	0.02250	3.92147&	-3	0.02071	3.56213& -2
54	3.0	0.01525	1.84745&	-3	0.01292	2.15967& -2
73	4.0	0.01342	1.15155&	-3	0.01296	1.53718& -2
91	5.0	0.01245	7.84935&	-4	0.01555	6.81886& -3
109	6.0	0.01174	6.21509&	-4	0.01172	6.21795& -3
127	7.0	0.01143	4.65119&	-4	0.01410	5.73832& -3
146	8.0	0.01091	3.89018&	-4	0.01076	3.66374& -3
164	9.0	0.01083	3.01282&	-4	0.01225	2.92448& -3
182	10.0	0.01067	3.20532&	-4	0.01106	3.18554& -3
200	11.0	0.01059	2.68689&	-4	0.01023	1.97195& -3
219	12.0	0.01053	2.28434&	-4	0.01085	3.00276& -3
237	13.0	0.01042	2.03248&	-4	0.01039	2.33944& -3
255	14.0	0.01038	1.87355&	-4	0.00931	2.08095& -3
273	15.0	0.01035	1.67200&	-4	0.01174	6.31212& -3
292	16.0	0.01034	1.55655&	-4	0.00985	1.81278& -3
310	17.0	0.01033	1.44879&	-4	0.01067	1.81896& -3
328	18.0	0.01028	1.43209&	-4	0.00974	1.83792& -3
346	19.0	0.01027	1.35032&	-4	0.00985	2.33768& -3
365	20.0	0.01027	1.42069&	-4	0.00936	1.68587& -3
383	21.0	0.01027	1.34167&	-4	0.01013	2.19964& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01406	2.53438&	-3	0.01314	1.93854& -2
197	2.0	0.01219	8.73060&	-4	0.01175	4.58898& -3
295	3.0	0.01090	4.56448&	-4	0.00975	4.07619& -3
394	4.0	0.01090	3.13536&	-4	0.01059	2.80087& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01158	1.07909&	-3	0.01196	6.94431& -3

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00992	1.12493&	-3	0.01170	1.16383& -2
36	2.0	0.00857	5.42397&	-4	0.00856	4.27758& -3
54	3.0	0.00781	3.43672&	-4	0.00752	3.24458& -3
73	4.0	0.00769	2.65349&	-4	0.00747	2.67540& -3
91	5.0	0.00761	2.11291&	-4	0.00835	1.48526& -3
109	6.0	0.00755	1.86351&	-4	0.00764	1.77458& -3
127	7.0	0.00752	1.56592&	-4	0.00849	1.74500& -3
146	8.0	0.00735	1.38513&	-4	0.00741	1.21004& -3
164	9.0	0.00736	1.15038&	-4	0.00798	1.05209& -3
182	10.0	0.00734	1.27138&	-4	0.00763	1.12243& -3
200	11.0	0.00733	1.12757&	-4	0.00718	7.76792& -4
219	12.0	0.00732	1.00642&	-4	0.00734	1.20825& -3
237	13.0	0.00726	9.18342&	-5	0.00715	1.09153& -3
255	14.0	0.00725	8.83985&	-5	0.00689	9.48417& -4
273	15.0	0.00725	8.08099&	-5	0.00743	9.43666& -4
292	16.0	0.00725	7.68403&	-5	0.00703	8.36197& -4
310	17.0	0.00725	7.35638&	-5	0.00740	7.88695& -4
328	18.0	0.00721	7.35629&	-5	0.00701	8.72772& -4
346	19.0	0.00722	7.08424&	-5	0.00711	1.14745& -3
365	20.0	0.00722	7.53048&	-5	0.00673	7.95997& -4
383	21.0	0.00722	7.20475&	-5	0.00714	1.18524& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00779	4.42634&	-4	0.00778	2.94522& -3
197	2.0	0.00766	2.43974&	-4	0.00768	1.19901& -3
295	3.0	0.00739	1.60796&	-4	0.00713	1.26702& -3
394	4.0	0.00743	1.27637&	-4	0.00740	1.03349& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00751	2.81428&	-4	0.00767	1.57477& -3

Data Analysis ProgramRun Number = 103

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values Per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.05918	1.54260&	-2	-0.04070	1.16467& 0
36	2.0	0.02344	3.64968&	-3	-0.01567	7.00791& -2
54	3.0	0.02083	2.01363&	-2	0.06995	1.35510& -1
73	4.0	0.01377	1.06304&	-3	0.03580	4.95599& -2
91	5.0	0.01264	8.18400&	-4	0.01388	2.18293& -2
109	6.0	0.01326	5.79628&	-3	0.01563	1.04959& -2
127	7.0	0.01145	4.53524&	-4	0.02094	1.51875& -2
146	8.0	0.01033	2.45448&	-3	0.01759	1.00489& -2
164	9.0	0.01081	3.17130&	-4	0.01268	1.31493& -2
182	10.0	0.01071	2.57170&	-4	0.01321	1.18305& -2
200	11.0	0.01060	2.33773&	-4	0.01088	7.64671& -3
219	12.0	0.01055	2.22892&	-4	0.00820	6.63748& -3
237	13.0	0.01042	1.90878&	-4	0.00874	7.54863& -3
255	14.0	0.01038	1.83057&	-4	0.01235	9.66654& -3
273	15.0	0.01036	1.68297&	-4	0.01101	5.18082& -3
292	16.0	0.01034	1.60833&	-4	0.01124	5.27422& -3
310	17.0	0.01033	1.61835&	-4	0.00792	5.92433& -3
328	18.0	0.01028	1.46576&	-4	0.01001	3.51862& -3
346	19.0	0.00964	2.37163&	-3	0.01039	4.26881& -3
365	20.0	0.01026	1.23202&	-4	0.00937	5.96049& -3
383	21.0	0.01025	1.19702&	-4	0.01277	5.26358& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01476	2.63232&	-3	0.04055	5.59313& -2
197	2.0	0.01233	7.93706&	-4	0.00832	1.69143& -2
295	3.0	0.01096	4.52278&	-4	0.01668	1.48986& -2
394	4.0	0.01094	2.91773&	-4	0.01618	1.17781& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01183	1.09857&	-3	0.01428	2.09945& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01022	1.20903&	-3	0.00850	9.99003& -2
36	2.0	0.00866	5.11150&	-4	0.00708	7.00613& -3
54	3.0	0.00801	6.84664&	-4	0.01642	1.92458& -2
73	4.0	0.00774	2.51416&	-4	0.01273	1.05757& -2
91	5.0	0.00764	2.16584&	-4	0.00791	4.93962& -3
109	6.0	0.00758	2.27268&	-4	0.00948	3.07227& -3
127	7.0	0.00750	1.50978&	-4	0.01035	4.85839& -3
146	8.0	0.00716	7.47616&	-4	0.00929	3.21584& -3
164	9.0	0.00734	1.19495&	-4	0.00835	4.74252& -3
182	10.0	0.00734	1.03912&	-4	0.00830	3.22613& -3
200	11.0	0.00732	9.85918&	-5	0.00763	3.05104& -3
219	12.0	0.00731	9.67488&	-5	0.00644	2.56855& -3
237	13.0	0.00724	8.67606&	-5	0.00650	2.94517& -3
255	14.0	0.00724	8.46968&	-5	0.00842	4.49904& -3
273	15.0	0.00724	8.03889&	-5	0.00744	2.40808& -3
292	16.0	0.00724	7.86252&	-5	0.00746	2.08134& -3
310	17.0	0.00724	7.99185&	-5	0.00637	2.93446& -3
328	18.0	0.00720	7.35509&	-5	0.00673	1.46034& -3
346	19.0	0.00683	1.43519&	-3	0.00780	2.48569& -3
365	20.0	0.00720	6.47789&	-5	0.00677	3.01326& -3
383	21.0	0.00720	6.37240&	-5	0.00825	2.56903& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00788	4.52841&	-4	0.01228	9.73088& -3
197	2.0	0.00768	2.23837&	-4	0.00718	4.55252& -3
295	3.0	0.00739	1.58827&	-4	0.00935	4.77750& -3
394	4.0	0.00743	1.18188&	-4	0.00910	3.90363& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00755	2.84719&	-4	0.00833	5.27547& -3

Data Analysis ProgramRun Number = 104

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.01678	1.08802& -1	-0.19254	7.47352& -1
36	2.0	0.01973	1.06623& -2	0.10411	2.98615& -1
54	3.0	0.01354	6.41205& -3	0.03000	1.41179& -1
73	4.0	0.01220	4.67282& -3	0.00030	4.74179& -2
91	5.0	0.01164	3.03660& -3	0.01321	4.65548& -2
109	6.0	0.00980	5.25808& -3	0.01686	4.52864& -2
127	7.0	0.01089	1.79600& -3	0.01430	1.88047& -2
146	8.0	0.01050	1.48586& -3	0.02694	3.27081& -2
164	9.0	0.01043	1.26813& -3	0.01121	1.77754& -2
182	10.0	0.01153	4.77144& -3	0.01748	1.76994& -2
200	11.0	0.01030	9.68589& -4	0.01268	1.28108& -2
219	12.0	0.01028	8.70868& -4	0.02046	1.60655& -2
237	13.0	0.01018	7.92679& -4	0.01055	1.35379& -2
255	14.0	0.01016	7.23608& -4	0.01028	1.06773& -2
273	15.0	0.01016	6.70835& -4	0.01143	9.66625& -3
292	16.0	0.01017	6.23646& -4	0.01308	1.07931& -2
310	17.0	0.01015	5.81932& -4	0.01450	9.70304& -3
328	18.0	0.00960	1.98127& -3	0.01111	1.03183& -2
346	19.0	0.01011	5.22114& -4	0.01302	1.16633& -2
365	20.0	0.01012	4.95944& -4	0.01424	9.06500& -3
383	21.0	0.01011	4.74518& -4	0.01114	5.90144& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.01212	7.29837& -3	-0.00640	7.58248& -2
197	2.0	0.01146	2.66456& -3	0.01273	3.43205& -2
295	3.0	0.01044	1.66610& -3	0.01143	2.27648& -2
394	4.0	0.01054	1.28207& -3	0.01135	1.63220& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.01064	3.43151& -3	0.00837	4.07604& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00827	3.84267&	-3	0.01138	7.98593& -2
36	2.0	0.00817	1.37447&	-3	0.02737	4.38892& -2
54	3.0	0.00748	1.09026&	-3	0.01681	2.37415& -2
73	4.0	0.00740	9.76501&	-4	0.00771	1.01671& -2
91	5.0	0.00738	7.69264&	-4	0.00861	1.07753& -2
109	6.0	0.00694	1.56555&	-3	0.01105	1.53156& -2
127	7.0	0.00732	5.77084&	-4	0.00895	5.04496& -3
146	8.0	0.00718	5.15470&	-4	0.01280	9.11397& -3
164	9.0	0.00719	4.71458&	-4	0.00813	6.71750& -3
182	10.0	0.00726	5.24987&	-4	0.01032	6.86770& -3
200	11.0	0.00718	4.01777&	-4	0.00841	5.69286& -3
219	12.0	0.00718	3.76986&	-4	0.01121	6.51955& -3
237	13.0	0.00713	3.54921&	-4	0.00823	6.66461& -3
255	14.0	0.00713	3.35018&	-4	0.00738	4.21693& -3
273	15.0	0.00713	3.19565&	-4	0.00760	4.27154& -3
292	16.0	0.00714	3.05234&	-4	0.00898	5.07604& -3
310	17.0	0.00714	2.91523&	-4	0.00923	4.51676& -3
328	18.0	0.00687	9.09553&	-4	0.00773	4.91261& -3
346	19.0	0.00711	2.71773&	-4	0.00901	5.69919& -3
365	20.0	0.00712	2.62407&	-4	0.00856	4.01747& -3
383	21.0	0.00712	2.54827&	-4	0.00818	3.29407& -3

Quadrature Size = 6

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00743	1.21292&	-3	0.00674	1.21531& -2
197	2.0	0.00743	7.34434&	-4	0.00899	8.53873& -3
295	3.0	0.00720	5.73098&	-4	0.00855	8.03886& -3
394	4.0	0.00727	5.05610&	-4	0.00803	5.63376& -3

Quadrature Size = 9

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00724	8.75393&	-4	0.00781	1.04251& -2

Data Analysis ProgramRun Number = 105

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.05714	1.39629& -2	0.10983	2.08343& -1
36	2.0	0.02096	8.16174& -3	0.06555	1.80334& -1
54	3.0	0.01564	2.31902& -3	0.01351	2.20109& -2
73	4.0	0.01726	1.42208& -2	0.01143	1.85266& -2
91	5.0	0.01255	8.17655& -4	0.01178	8.91335& -3
109	6.0	0.01187	5.65255& -4	0.01341	8.76163& -3
127	7.0	0.01141	4.52376& -4	0.01214	7.18533& -3
146	8.0	0.01091	4.20179& -4	0.01043	7.85652& -3
164	9.0	0.01079	3.68561& -4	0.01193	5.47792& -3
182	10.0	0.01063	2.96072& -4	0.01259	6.75371& -3
200	11.0	0.01058	2.73346& -4	0.01016	4.45720& -3
219	12.0	0.01051	2.47030& -4	0.01024	5.20374& -3
237	13.0	0.01041	2.29332& -4	0.01116	4.32368& -3
255	14.0	0.01037	2.03805& -4	0.01060	4.37518& -3
273	15.0	0.01036	2.10996& -4	0.01102	6.66208& -3
292	16.0	0.01034	1.63155& -4	0.00981	2.66958& -3
310	17.0	0.01032	1.69718& -4	0.01101	3.72706& -3
328	18.0	0.01026	1.56014& -4	0.01135	2.88199& -3
346	19.0	0.01026	1.42391& -4	0.00912	2.73356& -3
365	20.0	0.01025	1.31959& -4	0.00968	3.04801& -3
383	21.0	0.01026	1.37841& -4	0.00969	3.40122& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.01437	2.59234& -3	0.01360	2.57561& -2
197	2.0	0.01197	1.32820& -3	0.01321	1.33564& -2
295	3.0	0.01215	4.90083& -3	0.01033	6.35640& -3
394	4.0	0.01093	3.75864& -4	0.00965	5.15895& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.01167	1.13590& -3	0.01190	1.28568& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00577	6.27594&	-4	0.00813	6.91110& -3
36	2.0	0.00481	5.58225&	-4	0.00746	9.48501& -3
54	3.0	0.00450	2.43297&	-4	0.00435	1.85056& -3
73	4.0	0.00450	3.70065&	-4	0.00408	2.08149& -3
91	5.0	0.00437	1.28433&	-4	0.00435	1.20327& -3
109	6.0	0.00434	9.92481&	-5	0.00462	1.50639& -3
127	7.0	0.00430	8.87852&	-5	0.00451	1.22485& -3
146	8.0	0.00421	8.64699&	-5	0.00411	1.50578& -3
164	9.0	0.00420	8.02502&	-5	0.00445	1.11607& -3
182	10.0	0.00419	7.12712&	-5	0.00469	1.40941& -3
200	11.0	0.00419	6.86669&	-5	0.00413	1.02342& -3
219	12.0	0.00418	6.34405&	-5	0.00411	1.08732& -3
237	13.0	0.00415	6.11840&	-5	0.00444	1.05226& -3
255	14.0	0.00415	5.57350&	-5	0.00424	1.07462& -3
273	15.0	0.00415	5.82781&	-5	0.00416	1.12991& -3
292	16.0	0.00415	4.69415&	-5	0.00408	7.73231& -4
310	17.0	0.00415	4.95774&	-5	0.00433	9.06825& -4
328	18.0	0.00412	4.62421&	-5	0.00432	7.31092& -4
346	19.0	0.00413	4.30079&	-5	0.00384	8.19646& -4
365	20.0	0.00413	4.09772&	-5	0.00401	8.83921& -4
383	21.0	0.00413	4.26238&	-5	0.00400	1.03113& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00448	2.61829&	-4	0.00456	2.20719& -3
197	2.0	0.00435	1.99313&	-4	0.00470	2.16320& -3
295	3.0	0.00431	3.66934&	-4	0.00416	1.17003& -3
394	4.0	0.00426	8.75545&	-5	0.00398	1.05852& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00430	1.71863&	-4	0.00445	1.72983& -3

Data Analysis ProgramRun Number = 106

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
18	1.0	0.05576	1.50160&	-2	-0.02027	2.74393&	-1
36	2.0	0.01939	1.38998&	-2	0.03516	7.17209&	-2
54	3.0	0.01541	2.02840&	-3	-0.01422	8.14872&	-2
73	4.0	0.01346	1.17873&	-3	-0.00131	7.15499&	-2
91	5.0	0.01101	5.78255&	-3	0.02010	1.00785&	-2
109	6.0	0.01178	5.71669&	-4	0.01426	8.85353&	-3
127	7.0	0.01145	4.45306&	-4	0.01577	9.23902&	-3
146	8.0	0.00989	4.01368&	-3	0.01444	6.39833&	-3
164	9.0	0.01019	2.30674&	-3	0.01144	5.73468&	-3
182	10.0	0.01066	2.75737&	-4	0.01074	7.26032&	-3
200	11.0	0.01061	2.83249&	-4	0.01382	7.44943&	-3
219	12.0	0.01000	2.11064&	-3	0.01303	3.64612&	-3
237	13.0	0.01045	2.20484&	-4	0.01110	2.84380&	-3
255	14.0	0.01021	5.85695&	-4	0.01056	4.48301&	-3
273	15.0	0.01039	1.79925&	-4	0.01213	2.35441&	-3
292	16.0	0.01038	1.76305&	-4	0.01066	2.37384&	-3
310	17.0	0.01034	1.53888&	-4	0.01085	3.20453&	-3
328	18.0	0.01029	1.36487&	-4	0.01159	3.13098&	-3
346	19.0	0.01028	1.35628&	-4	0.00966	5.11463&	-3
365	20.0	0.00953	2.93543&	-3	0.01149	2.64341&	-3
383	21.0	0.01027	1.28288&	-4	0.01176	2.19889&	-3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
98	1.0	0.01425	2.59778&	-3	0.02500	2.89438&	-2
197	2.0	0.01225	8.92397&	-4	0.01411	1.31331&	-2
295	3.0	0.01096	4.97164&	-4	0.01019	5.07929&	-3
394	4.0	0.01263	4.67118&	-3	0.01025	5.21356&	-3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
257	1.0	0.01218	2.49273&	-3	0.01688	1.03873&	-2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00572	6.64419&	-4	0.00520	8.17501& -3
36	2.0	0.00468	1.01859&	-3	0.00663	5.03906& -3
54	3.0	0.00448	2.15984&	-4	0.00279	4.23509& -3
73	4.0	0.00441	1.56124&	-4	0.00394	4.59410& -3
91	5.0	0.00414	8.65211&	-4	0.00528	1.65592& -3
109	6.0	0.00433	1.01350&	-4	0.00486	1.52331& -3
127	7.0	0.00431	8.72501&	-5	0.00506	1.74396& -3
146	8.0	0.00400	8.35263&	-4	0.00490	1.11072& -3
164	9.0	0.00409	4.32124&	-4	0.00430	1.05531& -3
182	10.0	0.00420	6.45080&	-5	0.00427	1.62825& -3
200	11.0	0.00420	6.82217&	-5	0.00485	1.51885& -3
219	12.0	0.00407	4.63924&	-4	0.00478	9.39524& -4
237	13.0	0.00416	5.70125&	-5	0.00425	7.20420& -4
255	14.0	0.00407	2.97826&	-4	0.00430	1.13165& -3
273	15.0	0.00416	5.00249&	-5	0.00465	5.86686& -4
292	16.0	0.00416	4.96792&	-5	0.00438	7.60613& -4
310	17.0	0.00415	4.49897&	-5	0.00416	7.70910& -4
328	18.0	0.00413	4.02961&	-5	0.00445	8.65665& -4
346	19.0	0.00413	4.13416&	-5	0.00413	1.10400& -3
365	20.0	0.00397	6.52431&	-4	0.00449	7.84662& -4
383	21.0	0.00413	4.02771&	-5	0.00465	6.94877& -4

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00447	2.59368&	-4	0.00542	2.16736& -3
197	2.0	0.00439	1.43442&	-4	0.00476	2.02185& -3
295	3.0	0.00424	1.01171&	-4	0.00420	9.19111& -4
394	4.0	0.00435	3.55685&	-4	0.00411	1.07100& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00433	2.08814&	-4	0.00484	1.24247& -3

Data Analysis Program

Run Number = 107

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel - 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.06293	1.39679&	-2	-1.20919	2.87477& 0
36	2.0	0.02417	3.50243&	-3	-0.16976	5.18205& -1
54	3.0	0.01611	1.76402&	-3	0.06510	1.19296& -1
73	4.0	0.01414	1.06980&	-3	0.02334	5.10245& -2
91	5.0	0.01291	7.23577&	-4	0.06009	1.27806& -1
109	6.0	0.01206	6.27201&	-4	0.01253	3.16097& -2
127	7.0	0.01162	4.43460&	-4	0.03275	3.41309& -2
146	8.0	0.01113	3.57192&	-4	0.03196	4.58274& -2
164	9.0	0.01097	3.04519&	-4	0.01910	4.71987& -2
182	10.0	0.01081	2.73082&	-4	0.01266	1.11109& -2
200	11.0	0.01071	2.20180&	-4	0.01581	2.62785& -2
219	12.0	0.01067	2.17058&	-4	0.01587	1.63040& -2
237	13.0	0.01053	1.90701&	-4	0.02158	1.96971& -2
255	14.0	0.01048	1.81440&	-4	0.02052	2.56912& -2
273	15.0	0.01046	1.59733&	-4	0.01951	2.37292& -2
292	16.0	0.01044	1.48564&	-4	0.01337	1.07512& -2
310	17.0	0.01042	1.39459&	-4	0.01049	7.99305& -3
328	18.0	0.01037	1.31085&	-4	0.01407	1.14500& -2
346	19.0	0.01035	1.29065&	-4	0.01327	6.06974& -3
365	20.0	0.01036	1.13774&	-4	0.01312	1.08119& -2
383	21.0	0.01035	1.16651&	-4	0.01318	1.31990& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01547	2.36148&	-3	0.04279	1.77142& -1
197	2.0	0.01401	3.66742&	-3	0.01950	4.17842& -2
295	3.0	0.01113	4.36929&	-4	0.02040	2.00079& -2
394	4.0	0.01028	2.30378&	-3	0.01310	1.19393& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01218	1.01072&	-3	0.03153	5.50792& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00609	6.52598&	-4	-0.03635	1.40981& -1
36	2.0	0.00509	2.85754&	-4	-0.00465	3.95190& -2
54	3.0	0.00460	1.90011&	-4	0.01139	1.22462& -2
73	4.0	0.00453	1.41746&	-4	0.00680	7.08415& -3
91	5.0	0.00447	1.13424&	-4	0.01199	2.10529& -2
109	6.0	0.00442	1.07780&	-4	0.00780	6.64652& -3
127	7.0	0.00438	8.48709&	-5	0.00921	6.98489& -3
146	8.0	0.00429	7.43537&	-5	0.00862	8.71360& -3
164	9.0	0.00428	6.70146&	-5	0.00674	8.30141& -3
182	10.0	0.00427	6.47210&	-5	0.00496	2.57561& -3
200	11.0	0.00426	5.35606&	-5	0.00524	4.93033& -3
219	12.0	0.00426	5.49311&	-5	0.00539	3.43160& -3
237	13.0	0.00422	4.99413&	-5	0.00717	5.16250& -3
255	14.0	0.00422	4.90954&	-5	0.00663	5.04221& -3
273	15.0	0.00422	4.40502&	-5	0.00591	4.57806& -3
292	16.0	0.00421	4.20633&	-5	0.00504	2.77394& -3
310	17.0	0.00421	4.04630&	-5	0.00449	2.48796& -3
328	18.0	0.00419	3.91524&	-5	0.00514	3.18842& -3
346	19.0	0.00419	3.89658&	-5	0.00541	1.78350& -3
365	20.0	0.00419	3.50244&	-5	0.00503	2.92170& -3
383	21.0	0.00419	3.69770&	-5	0.00504	3.31203& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00464	2.40614&	-4	0.01145	2.18376& -2
197	2.0	0.00446	1.68099&	-4	0.00659	7.80448& -3
295	3.0	0.00431	8.85911&	-5	0.00628	3.76837& -3
394	4.0	0.00407	7.23078&	-4	0.00526	2.67954& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00443	1.52684&	-4	0.00774	8.84003& -3

Data Analysis ProgramRun Number = 108

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.04655	3.13577&	-2	-0.61278	8.04127& -1
36	2.0	0.03247	3.96959&	-2	-0.07952	5.57620& -1
54	3.0	0.01501	1.41206&	-3	-0.02551	1.57080& -1
73	4.0	0.01335	9.62640&	-4	0.01259	5.81792& -2
91	5.0	0.01097	5.91364&	-3	0.03018	9.30670& -2
109	6.0	0.01782	1.60258&	-2	0.01760	3.09710& -2
127	7.0	0.01134	3.55343&	-4	0.03460	5.28317& -2
146	8.0	0.00986	4.17271&	-3	0.04829	1.24002& -1
164	9.0	0.01076	2.63014&	-4	0.01752	5.63977& -2
182	10.0	0.01068	2.25665&	-4	0.00987	5.54026& -2
200	11.0	0.00972	3.29032&	-3	0.02741	3.74720& -2
219	12.0	0.01054	1.72355&	-4	0.01788	3.35968& -2
237	13.0	0.01042	1.48923&	-4	0.01681	2.63461& -2
255	14.0	0.01038	1.47787&	-4	0.01111	2.52484& -2
273	15.0	0.01036	1.31122&	-4	0.01119	3.22739& -2
292	16.0	0.01037	1.08737&	-4	0.01296	3.62698& -2
310	17.0	0.01033	1.18683&	-4	0.00811	1.55014& -2
328	18.0	0.01030	1.24308&	-4	0.01964	2.90999& -2
346	19.0	0.00904	3.30123&	-3	0.01376	1.71558& -2
365	20.0	0.00967	2.32474&	-3	0.02877	4.63704& -2
383	21.0	0.01029	9.52256&	-5	0.01293	1.98201& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01390	1.91280&	-3	-0.10309	1.83430& -1
197	2.0	0.01210	6.37540&	-4	0.04043	8.27910& -2
295	3.0	0.01089	3.33026&	-4	0.01510	4.27482& -2
394	4.0	0.01161	2.67339&	-3	0.03187	5.27226& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01151	8.07780&	-4	0.03116	1.01802& -1

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00541	1.24495&	-3	-0.03239	1.09416& -1
36	2.0	0.00508	6.22512&	-4	0.00637	8.36952& -2
54	3.0	0.00448	1.51056&	-4	0.00639	1.85920& -2
73	4.0	0.00443	1.27120&	-4	0.00620	8.93097& -3
91	5.0	0.00417	8.81436&	-4	0.01042	1.44776& -2
109	6.0	0.00449	4.08584&	-4	0.00691	5.64720& -3
127	7.0	0.00432	6.90016&	-5	0.01042	1.12397& -2
146	8.0	0.00403	8.59159&	-4	0.01513	2.59494& -2
164	9.0	0.00423	5.75826&	-5	0.00613	9.22350& -3
182	10.0	0.00424	5.11597&	-5	0.00555	1.32863& -2
200	11.0	0.00400	8.44809&	-4	0.00914	1.00088& -2
219	12.0	0.00422	4.33082&	-5	0.00635	7.50028& -3
237	13.0	0.00419	3.92371&	-5	0.00607	5.53687& -3
255	14.0	0.00418	3.93569&	-5	0.00422	5.71362& -3
273	15.0	0.00419	3.62341&	-5	0.00532	7.37240& -3
292	16.0	0.00419	3.08571&	-5	0.00521	8.84256& -3
310	17.0	0.00418	3.52720&	-5	0.00426	4.37944& -3
328	18.0	0.00417	3.66623&	-5	0.00786	8.83802& -3
340	19.0	0.00374	1.14201&	-3	0.00598	5.74799& -3
365	20.0	0.00395	8.32536&	-4	0.00780	1.01415& -2
383	21.0	0.00417	2.94705&	-5	0.00572	6.86252& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00448	1.92609&	-4	0.00086	1.46118& -2
197	2.0	0.00441	1.03397&	-4	0.01363	1.47227& -2
295	3.0	0.00426	6.68672&	-5	0.00545	7.50794& -3
394	4.0	0.00430	5.72974&	-5	0.00865	8.69722& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00432	1.22581&	-4	0.00889	1.29773& -2

Data Analysis Program

Run Number = 109

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.04742	4.65498&	-2	-0.01930	9.19048& -1
36	2.0	0.01799	1.49764&	-2	0.48175	1.27792& 0
54	3.0	0.01246	8.80040&	-3	-0.08030	2.47474& -1
73	4.0	0.01199	5.49845&	-3	0.06454	1.23347& -1
91	5.0	0.01136	3.42132&	-3	-0.01685	1.25829& -1
109	6.0	0.01105	2.56680&	-3	0.02917	5.05238& -2
127	7.0	0.01070	2.00262&	-3	0.03735	5.40378& -2
146	8.0	0.01046	1.62376&	-3	0.01512	3.76040& -2
164	9.0	0.01033	1.42247&	-3	0.01670	1.92935& -2
182	10.0	0.01023	1.23040&	-3	0.04302	5.17115& -2
200	11.0	0.01024	1.12217&	-3	0.02739	3.22823& -2
219	12.0	0.01024	9.67185&	-4	0.02027	2.29261& -2
237	13.0	0.01011	8.48591&	-4	0.01386	1.61176& -2
255	14.0	0.01010	8.27433&	-4	0.01300	1.97448& -2
273	15.0	0.01011	7.38471&	-4	0.00876	1.28201& -2
292	16.0	0.00943	2.70485&	-3	0.02408	3.23921& -2
310	17.0	0.01009	5.99658&	-4	0.01619	1.74292& -2
328	18.0	0.01004	6.13410&	-4	0.00966	1.18638& -2
346	19.0	0.01009	5.86609&	-4	0.01164	1.22064& -2
365	20.0	0.00956	1.96258&	-3	0.01284	1.12299& -2
383	21.0	0.01008	5.38730&	-4	0.01345	1.04490& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01172	9.26332&	-3	-0.04376	1.52845& -1
197	2.0	0.01117	3.41701&	-3	0.02896	5.46827& -2
295	3.0	0.01022	2.12916&	-3	0.01685	2.48530& -2
394	4.0	0.01049	1.50445&	-3	0.01464	1.40538& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01043	4.12629&	-3	0.05271	1.36475& -1

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00138	4.50246&	-4	0.00220	1.72514& -2
36	2.0	0.00117	2.68779&	-4	0.02022	4.30133& -2
54	3.0	0.00107	2.10665&	-4	-0.00038	5.60618& -3
73	4.0	0.00107	1.68288&	-4	0.00360	6.04732& -3
91	5.0	0.00107	1.27042&	-4	0.00084	2.77996& -3
109	6.0	0.00107	1.08325&	-4	0.00199	2.12009& -3
127	7.0	0.00106	9.45940&	-5	0.00272	2.83005& -3
146	8.0	0.00105	8.26644&	-5	0.00173	2.47206& -3
164	9.0	0.00104	7.79559&	-5	0.00145	1.00394& -3
182	10.0	0.00104	7.04476&	-5	0.00275	2.21307& -3
200	11.0	0.00104	6.80638&	-5	0.00196	1.58641& -3
219	12.0	0.00105	6.18135&	-5	0.00169	1.38140& -3
237	13.0	0.00104	5.60551&	-5	0.00135	1.02659& -3
255	14.0	0.00104	5.62285&	-5	0.00131	1.26042& -3
273	15.0	0.00104	5.14165&	-5	0.00102	8.95944& -4
292	16.0	0.00098	2.14037&	-4	0.00208	2.12731& -3
310	17.0	0.00104	4.44282&	-5	0.00140	9.14498& -4
328	18.0	0.00103	4.59418&	-5	0.00108	9.07898& -4
346	19.0	0.00104	4.50471&	-5	0.00117	8.60313& -4
365	20.0	0.00100	1.37056&	-4	0.00129	8.65709& -4
383	21.0	0.00104	4.22551&	-5	0.00134	7.79739& -4

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00108	2.20664&	-4	0.00026	2.85321& -3
197	2.0	0.00107	1.34356&	-4	0.00224	2.45868& -3
295	3.0	0.00104	1.04909&	-4	0.00142	1.21405& -3
394	4.0	0.00106	8.62360&	-5	0.00151	8.96770& -4

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00105	1.52290&	-4	0.00276	5.29584& -3

Data Analysis ProgramRun Number 110

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.04997	3.50044&	-2	-0.23682	8.80551& -1
36	2.0	0.02115	1.22492&	-2	0.56651	1.87343& 0
54	3.0	0.01349	6.87684&	-3	0.01255	2.43694& -1
73	4.0	0.01249	5.02682&	-3	-0.05283	5.22252& -1
91	5.0	0.01177	3.07704&	-3	-0.10886	2.03788& -1
109	6.0	0.01124	2.30102&	-3	-0.01413	5.84947& -2
127	7.0	0.01087	1.83991&	-3	0.00163	1.06141& -1
146	8.0	0.01065	1.59442&	-3	0.00406	1.52228& -1
164	9.0	0.01145	6.60408&	-3	-0.04163	1.49371& -1
182	10.0	0.01034	1.13471&	-3	-0.03923	7.24787& -2
200	11.0	0.01036	1.02856&	-3	0.23029	9.96498& -1
219	12.0	0.01040	9.05717&	-4	0.02724	6.50005& -2
237	13.0	0.01024	8.19604&	-4	-0.00223	3.10086& -2
255	14.0	0.00974	2.12330&	-3	0.01744	1.84877& -1
273	15.0	0.00995	1.19365&	-3	0.00096	2.74674& -2
292	16.0	0.01019	6.43713&	-4	0.02372	1.93447& -1
310	17.0	0.01016	5.92684&	-4	0.00615	3.62205& -2
328	18.0	0.01012	5.69892&	-4	0.00361	6.23459& -2
346	19.0	0.01020	5.59086&	-4	0.00113	3.49980& -2
365	20.0	0.01016	4.91934&	-4	-0.03403	1.00639& -1
383	21.0	0.01017	5.10192&	-4	-0.00860	4.51645& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01152	8.63994&	-3	-0.03772	4.47182& -1
197	2.0	0.01168	2.97315&	-3	-0.00891	9.78434& -2
295	3.0	0.01164	5.17491&	-3	0.00299	8.13486& -2
394	4.0	0.01062	1.37242&	-3	-0.01042	1.13889& -1

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01086	3.55487&	-3	-0.08151	1.87165& -1

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00139	3.43721&	-4	-0.01604	4.20999& -2
36	2.0	0.00122	2.20741&	-4	0.04873	1.29263& -1
54	3.0	0.00109	1.66589&	-4	0.00748	1.69335& -2
73	4.0	0.00109	1.50480&	-4	-0.00683	4.50854& -2
91	5.0	0.00108	1.12465&	-4	-0.00437	1.44341& -2
109	6.0	0.00107	9.68587&	-5	0.00187	4.63218& -3
127	7.0	0.00106	8.47424&	-5	0.00161	7.55329& -3
146	8.0	0.00105	7.99227&	-5	0.00193	1.12348& -2
164	9.0	0.00104	1.42910&	-4	-0.00164	1.27430& -2
182	10.0	0.00104	6.46168&	-5	-0.00141	7.85895& -3
200	11.0	0.0105	6.21269&	-5	0.02713	1.08372& -1
219	12.0	0.00105	5.65913&	-5	0.00452	6.63694& -3
237	13.0	0.00104	5.29785&	-5	0.00101	2.04475& -3
255	14.0	0.00101	1.28457&	-4	0.00227	1.66039& -2
273	15.0	0.00102	9.91486&	-5	0.00112	2.01508& -3
292	16.0	0.00104	4.52830&	-5	0.00144	1.02883& -2
310	17.0	0.00104	4.29118&	-5	0.00172	3.51541& -3
328	18.0	0.00103	4.21409&	-5	0.00101	5.91627& -3
346	19.0	0.00104	4.19876&	-5	0.00140	3.30353& -3
365	20.0	0.00104	3.80325&	-5	-0.00044	7.46964& -3
383	21.0	0.00104	3.93772&	-5	0.00004	3.57758& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00106	2.20366&	-4	0.00491	2.71568& -2
197	2.0	0.00109	1.16853&	-4	0.00221	5.85339& -3
295	3.0	0.00107	1.26232&	-4	0.00162	3.98104& -3
394	4.0	0.00106	7.72182&	-5	0.00100	6.05735& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00106	1.30936&	-4	-0.00098	1.04952& -2

Data Analysis ProgramRun Number = 111

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.06696	1.66389&	-2	-0.15572	4.94959& -1
36	2.0	0.02615	3.79102&	-3	-0.16092	3.01648& -1
54	3.0	0.01704	2.28126&	-3	-0.07005	1.02448& -1
73	4.0	0.01445	1.28004&	-3	-0.03456	2.00111& -1
91	5.0	0.01303	8.69966&	-4	-0.06707	1.50380& -1
109	6.0	0.01522	1.17255&	-2	-0.08455	1.09754& -1
127	7.0	0.01185	6.69359&	-4	0.02639	1.21888& -1
146	8.0	0.01131	3.72038&	-4	0.00173	1.10981& -1
164	9.0	0.01105	3.88069&	-4	-0.04395	7.93050& -2
182	10.0	0.01089	4.45950&	-4	-0.01831	6.98481& -2
200	11.0	0.01079	3.52660&	-4	-0.02671	4.14065& -2
219	12.0	0.01074	2.64618&	-4	-0.02947	8.88119& -2
237	13.0	0.01059	2.46424&	-4	-0.01105	3.96063& -2
255	14.0	0.01056	2.35398&	-4	-0.00919	4.80255& -2
273	15.0	0.01047	2.19054&	-4	-0.01766	2.38107& -2
292	16.0	0.01045	1.93630&	-4	0.00016	4.70552& -2
310	17.0	0.01047	1.93997&	-4	-0.02093	2.56028& -2
328	18.0	0.01043	1.93795&	-4	-0.01776	1.20555& -1
346	19.0	0.00979	2.46763&	-3	-0.00308	4.87592& -2
365	20.0	0.00936	4.08042&	-3	0.01164	5.91716& -2
383	21.0	0.01039	1.64778&	-4	-0.00492	2.96210& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01617	2.89784&	-3	-0.16707	1.88712& -1
197	2.0	0.01295	9.91548&	-4	0.10895	5.40580& -1
295	3.0	0.01125	5.40801&	-4	0.06339	3.42072& -1
394	4.0	0.01119	3.54094&	-4	-0.01475	7.84917& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01246	1.23302&	-3	-0.07541	1.34744& -1

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00159	1.96578&	-4	-0.00274	4.71495& -2
36	2.0	0.00132	8.00610&	-5	0.01287	2.67332& -2
54	3.0	0.00118	6.24005&	-5	-0.00085	9.00236& -3
73	4.0	0.00115	4.36150&	-5	0.00637	3.39283& -2
91	5.0	0.00113	3.49480&	-5	-0.00429	1.77182& -2
109	6.0	0.00115	1.06813&	-4	-0.00204	7.50961& -3
127	7.0	0.00111	3.19992&	-5	0.00618	1.64501& -2
146	8.0	0.00109	2.02595&	-5	0.00073	1.09620& -2
164	9.0	0.00108	2.20087&	-5	0.00105	8.47395& -3
182	10.0	0.00108	2.57139&	-5	0.00172	5.56225& -3
200	11.0	0.00108	2.28539&	-5	-0.00053	4.53065& -3
219	12.0	0.00108	1.85947&	-5	-0.00173	1.19375& -2
237	13.0	0.00107	1.72488&	-5	0.00134	4.20035& -3
255	14.0	0.00107	1.64839&	-5	0.00054	3.75874& -3
273	15.0	0.00106	1.56712&	-5	-0.00046	2.31789& -3
292	16.0	0.00106	1.44782&	-5	0.00232	7.09344& -3
310	17.0	0.00106	1.49319&	-5	-0.00031	3.53332& -3
328	18.0	0.00106	1.50656&	-5	-0.00198	1.98412& -2
346	19.0	0.00101	2.14550&	-4	0.00037	6.34806& -3
365	20.0	0.00101	2.09508&	-4	0.00328	8.03369& -3
383	21.0	0.00106	1.31399&	-5	0.00044	2.75115& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00119	7.54686&	-5	-0.00228	1.18969& -2
197	2.0	0.00115	4.14126&	-5	0.01409	4.56217& -2
295	3.0	0.00109	2.85243&	-5	0.01087	3.88386& -2
394	4.0	0.00110	2.21195&	-5	0.00162	6.15451& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00112	4.81137&	-5	-0.00031	7.19562& -3

Data Analysis Program

Run Number = 113

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
18	1.0	0.05982	1.20815&	-2	0.13707	4.63719&	-2
36	2.0	0.03107	3.49645&	-3	0.03954	2.03834&	-2
54	3.0	0.02437	1.85453&	-3	0.02966	9.96292&	-3
73	4.0	0.02294	1.19848&	-3	0.02336	8.30666&	-3
91	5.0	0.02216	8.90787&	-4	0.02049	4.39067&	-3
109	6.0	0.02166	7.03059&	-4	0.02325	4.72324&	-3
127	7.0	0.02141	5.83657&	-4	0.02350	3.94618&	-3
146	8.0	0.02104	5.03748&	-4	0.02211	3.51911&	-3
164	9.0	0.02098	4.42481&	-4	0.02154	3.43154&	-3
182	10.0	0.02088	4.01287&	-4	0.02249	4.22801&	-3
200	11.0	0.02083	3.57523&	-4	0.02103	3.45180&	-3
219	12.0	0.02078	3.28049&	-4	0.02023	2.94403&	-3
237	13.0	0.02067	3.08614&	-4	0.02067	3.74351&	-3
255	14.0	0.01964	3.83499&	-3	0.02059	3.65296&	-3
273	15.0	0.02061	2.74026&	-4	0.01881	3.05214&	-3
292	16.0	0.02058	2.61659&	-4	0.02010	2.59165&	-3
310	17.0	0.02055	2.46541&	-4	0.02065	3.07881&	-3
328	18.0	0.02051	2.36724&	-4	0.02018	2.51278&	-3
346	19.0	0.02051	2.25182&	-4	0.01998	2.63458&	-3
365	20.0	0.02051	2.21664&	-4	0.02080	2.50910&	-3
383	21.0	0.02052	2.08147&	-4	0.02030	1.95630&	-3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
98	1.0	0.02389	2.56669&	-3	0.02958	7.35032&	-3
197	2.0	0.02273	9.85701&	-4	0.02464	5.62922&	-3
295	3.0	0.02119	6.11949&	-4	0.02134	3.25467&	-3
394	4.0	0.02136	4.49425&	-4	0.02109	2.07199&	-3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
257	1.0	0.02172	1.28590&	-3	0.02283	5.02807&	-3

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01878	1.73468&	-3	0.02832	7.35218& -3
36	2.0	0.01654	8.38353&	-4	0.01808	4.56455& -3
54	3.0	0.01520	5.65756&	-4	0.01639	2.45857& -3
73	4.0	0.01504	4.34262&	-4	0.01550	3.03951& -3
91	5.0	0.01492	3.62938&	-4	0.01431	1.44186& -3
109	6.0	0.01484	3.11861&	-4	0.01552	1.59811& -3
127	7.0	0.01478	2.75015&	-4	0.01551	1.90895& -3
146	8.0	0.01457	2.49258&	-4	0.01500	1.40414& -3
164	9.0	0.01457	2.28928&	-4	0.01469	1.73296& -3
182	10.0	0.01455	2.15182&	-4	0.01532	1.78082& -3
200	11.0	0.01455	1.95247&	-4	0.01474	1.81605& -3
219	12.0	0.01453	1.85805&	-4	0.01422	1.51036& -3
237	13.0	0.01445	1.78609&	-4	0.01448	1.95480& -3
255	14.0	0.01371	2.83689&	-3	0.01410	1.98553& -3
273	15.0	0.01444	1.63453&	-4	0.01346	1.72498& -3
292	16.0	0.01443	1.57381&	-4	0.01423	1.49187& -3
310	17.0	0.01443	1.50843&	-4	0.01442	1.76040& -3
328	18.0	0.01439	1.46161&	-4	0.01440	1.51742& -3
346	19.0	0.01439	1.40656&	-4	0.01411	1.39338& -3
365	20.0	0.01440	1.39999&	-4	0.01451	1.50131& -3
383	21.0	0.01441	1.31710&	-4	0.01432	1.26703& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01520	7.25583&	-4	0.01651	2.07147& -3
197	2.0	0.01517	4.04336&	-4	0.01596	2.15335& -3
295	3.0	0.01464	2.93920&	-4	0.01459	1.28187& -3
394	4.0	0.01479	2.37899&	-4	0.01470	1.19338& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01476	4.88784&	-4	0.01510	2.23547& -3

Data Analysis Program

Run Number = 114

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.06944	1.75092&	-2	0.28622	3.03889& -1
36	2.0	0.03394	5.17765&	-3	0.06473	7.50687& -2
54	3.0	0.02591	2.71494&	-3	0.05030	4.13079& -2
73	4.0	0.02397	1.75628&	-3	0.03544	2.87447& -2
91	5.0	0.02297	1.31801&	-3	0.02571	1.60885& -2
109	6.0	0.02228	1.03035&	-3	0.02498	1.46850& -2
127	7.0	0.01973	5.88734&	-3	0.03174	1.99064& -2
146	8.0	0.02152	7.41202&	-4	0.02405	1.07445& -2
164	9.0	0.02030	4.14035&	-3	0.02241	1.20307& -2
182	10.0	0.02127	5.77332&	-4	0.02012	1.09289& -2
200	11.0	0.02118	5.35701&	-4	0.03022	8.66099& -3
219	12.0	0.02111	4.91702&	-4	0.02554	6.88790& -3
237	13.0	0.02099	4.57626&	-4	0.02310	8.98019& -3
255	14.0	0.02094	4.37803&	-4	0.02453	7.42810& -3
273	15.0	0.02090	4.01791&	-4	0.02223	5.49315& -3
292	16.0	0.02086	3.81496&	-4	0.02459	7.69086& -3
310	17.0	0.02083	3.62362&	-4	0.02176	7.07190& -3
328	18.0	0.02079	3.54621&	-4	0.02192	7.39317& -3
346	19.0	0.02077	3.38539&	-4	0.02396	5.38914& -3
365	20.0	0.02077	3.21161&	-4	0.02556	7.02591& -3
383	21.0	0.02077	3.19159&	-4	0.02279	8.97656& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.02763	7.42474&	-3	0.05678	3.79178& -2
197	2.0	0.02273	3.49386&	-3	0.03248	1.24958& -2
295	3.0	0.02176	8.96878&	-4	0.02831	1.06153& -2
394	4.0	0.02180	6.61436&	-4	0.02683	9.63209& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02284	1.88328&	-3	0.03206	1.53226& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.02027	2.56581&	-3	0.05471	5.36166& -2
36	2.0	0.01729	1.25235&	-3	0.02824	2.12645& -2
54	3.0	0.01572	8.33893&	-4	0.02362	1.21391& -2
73	4.0	0.01545	6.40610&	-4	0.02032	1.01254& -2
91	5.0	0.01528	5.38654&	-4	0.01526	5.37893& -3
109	6.0	0.01514	4.58782&	-4	0.01668	6.43661& -3
127	7.0	0.01415	2.44590&	-3	0.01937	8.66370& -3
146	8.0	0.01483	3.67345&	-4	0.01658	4.98167& -3
164	9.0	0.01431	1.90144&	-3	0.01514	5.72416& -3
182	10.0	0.01478	3.09470&	-4	0.01417	5.71928& -3
200	11.0	0.01476	2.94440&	-4	0.01905	3.96106& -3
219	12.0	0.01474	2.75796&	-4	0.01743	3.73277& -3
237	13.0	0.01465	2.61963&	-4	0.01570	4.43431& -3
255	14.0	0.01464	2.54460&	-4	0.01695	4.12425& -3
273	15.0	0.01463	2.38132&	-4	0.01573	3.41663& -3
292	16.0	0.01462	2.30536&	-4	0.01675	5.05694& -3
310	17.0	0.01461	2.20975&	-4	0.01494	3.29507& -3
328	18.0	0.01457	2.18080&	-4	0.01534	4.20563& -3
346	19.0	0.01457	2.10304&	-4	0.01690	3.32557& -3
365	20.0	0.01457	2.00895&	-4	0.01754	3.83887& -3
383	21.0	0.01458	2.01579&	-4	0.01618	5.70344& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01582	1.07794&	-3	0.02300	9.77618& -3
197	2.0	0.01508	1.90386&	-3	0.01888	4.91500& -3
295	3.0	0.01494	4.31848&	-4	0.01799	5.28033& -3
394	4.0	0.01505	3.50922&	-4	0.01783	4.92530& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01522	7.20963&	-4	0.01815	5.28436& -3

Data Analysis ProgramRun Number = 115

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.06137	1.34088&	-2	0.08711	7.14987& -1
36	2.0	0.03149	3.90620&	-3	0.13070	3.19825& -1
54	3.0	0.02465	2.06144&	-3	0.03223	8.51937& -2
73	4.0	0.02175	5.27233&	-3	0.03377	5.42657& -2
91	5.0	0.02229	9.86699&	-4	0.04113	4.07435& -2
109	6.0	0.02176	7.69684&	-4	0.03364	2.61164& -2
127	7.0	0.02150	6.48634&	-4	0.02743	1.90420& -2
146	8.0	0.02112	5.49812&	-4	0.03601	2.73865& -2
164	9.0	0.01976	5.10766&	-3	0.03324	2.45771& -2
182	10.0	0.02095	4.38017&	-4	0.02046	1.14939& -2
200	11.0	0.02089	3.95933&	-4	0.03177	3.73264& -2
219	12.0	0.02084	3.66248&	-4	0.02236	1.61826& -2
237	13.0	0.01973	4.02568&	-3	0.01877	9.89340& -3
255	14.0	0.02069	3.19590&	-4	0.02373	1.56663& -2
273	15.0	0.01971	3.70559&	-3	0.03982	3.36805& -2
292	16.0	0.02063	2.83822&	-4	0.02810	1.63408& -2
310	17.0	0.02061	2.72001&	-4	0.02237	1.20707& -2
328	18.0	0.02057	2.63308&	-4	0.03197	3.18325& -2
346	19.0	0.01631	1.63411&	-2	0.02631	1.61911& -2
365	20.0	0.02056	2.42735&	-4	0.01737	1.03311& -2
383	21.0	0.02056	2.31639&	-4	0.02663	1.93319& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.02708	1.05671&	-2	0.05331	6.55068& -2
197	2.0	0.02285	1.09573&	-3	0.02835	2.79509& -2
295	3.0	0.02129	6.75153&	-4	0.02729	1.94974& -2
394	4.0	0.02107	1.46945&	-3	0.02166	1.71352& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02082	4.94074&	-3	0.03399	3.19047& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01899	1.92262&	-3	0.04386	9.01997& -2
36	2.0	0.01663	9.31671&	-4	0.03825	7.11029& -2
54	3.0	0.01527	6.26567&	-4	0.02050	2.13148& -2
73	4.0	0.01467	1.62287&	-3	0.02013	2.00599& -2
91	5.0	0.01495	3.97509&	-4	0.02283	1.44499& -2
109	6.0	0.01486	3.39916&	-4	0.02098	1.15640& -2
127	7.0	0.01481	3.05247&	-4	0.01835	8.74131& -3
146	8.0	0.01459	2.71174&	-4	0.02211	1.27988& -2
164	9.0	0.01384	2.95399&	-3	0.02160	1.18145& -2
182	10.0	0.01457	2.32810&	-4	0.01425	5.17009& -3
200	11.0	0.01456	2.16136&	-4	0.02067	1.88820& -2
219	12.0	0.01455	2.05060&	-4	0.01569	8.05745& -3
237	13.0	0.01394	2.08678&	-3	0.01312	5.38132& -3
255	14.0	0.01445	1.85330&	-4	0.01720	8.93361& -3
273	15.0	0.01372	2.83096&	-3	0.02290	1.37072& -2
292	16.0	0.01444	1.69755&	-4	0.01840	9.13150& -3
310	17.0	0.01444	1.64679&	-4	0.01558	7.07145& -3
328	18.0	0.01440	1.60786&	-4	0.02016	1.45292& -2
346	19.0	0.01269	6.55283&	-3	0.01791	8.57376& -3
365	20.0	0.01440	1.50874&	-4	0.01222	5.29684& -3
383	21.0	0.01441	1.45490&	-4	0.01745	1.02902& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01550	9.86370&	-4	0.02560	2.03950& -2
197	2.0	0.01520	4.46859&	-4	0.01865	1.32508& -2
295	3.0	0.01468	3.21860&	-4	0.01782	8.91796& -3
394	4.0	0.01464	7.05736&	-4	0.01531	9.16794& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01440	1.86817&	-3	0.02022	1.18063& -2

Data Analysis Program

Run Number = 116

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.07607	1.17926& -2	0.09676	1.14433& -1
36	2.0	0.03598	3.37857& -3	0.00875	8.77036& -2
54	3.0	0.02695	1.76847& -3	0.02611	2.07435& -2
73	4.0	0.02455	1.21219& -3	0.01791	1.20340& -2
91	5.0	0.02340	8.51118& -4	0.02686	1.32471& -2
109	6.0	0.02262	6.84461& -4	0.02423	7.25061& -3
127	7.0	0.02222	5.70842& -4	0.02139	7.56137& -3
146	8.0	0.02173	4.82435& -4	0.02311	1.00057& -2
164	9.0	0.02157	4.28898& -4	0.02378	6.59959& -3
182	10.0	0.02144	4.00118& -4	0.02226	4.99732& -3
200	11.0	0.02134	3.50388& -4	0.02266	4.59369& -3
219	12.0	0.02124	3.23574& -4	0.02160	5.25113& -3
237	13.0	0.02111	3.09586& -4	0.02027	5.29908& -3
255	14.0	0.02104	2.75853& -4	0.02076	6.46949& -3
273	15.0	0.02098	2.60249& -4	0.02192	5.59113& -3
292	16.0	0.02093	2.44739& -4	0.02230	4.75929& -3
310	17.0	0.02090	2.51251& -4	0.02119	4.18380& -3
328	18.0	0.02085	2.20131& -4	0.02117	6.45277& -3
346	19.0	0.02082	2.13796& -4	0.02180	4.73125& -3
365	20.0	0.02082	2.19364& -4	0.02342	3.69165& -3
383	21.0	0.02082	2.03478& -4	0.02082	3.93702& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.02740	2.46684& -3	0.03059	2.27972& -2
197	2.0	0.02412	9.57087& -4	0.02310	7.84555& -3
295	3.0	0.02203	5.78623& -4	0.02235	4.94897& -3
394	4.0	0.02197	4.49009& -4	0.02155	5.17090& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.02308	2.22772& -3	0.02401	1.13665& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01212	9.97737&	-4	0.01403	8.10367& -3
36	2.0	0.01016	4.69189&	-4	0.00855	7.02560& -3
54	3.0	0.00916	3.11816&	-4	0.00924	3.45032& -3
73	4.0	0.00895	2.48911&	-4	0.00785	2.30258& -3
91	5.0	0.00884	1.97960&	-4	0.00962	3.02669& -3
109	6.0	0.00875	1.71662&	-4	0.00907	1.60142& -3
127	7.0	0.00869	1.53266&	-4	0.00870	1.77014& -3
146	8.0	0.00854	1.35134&	-4	0.00892	2.39788& -3
164	9.0	0.00853	1.25733&	-4	0.00919	2.04593& -3
182	10.0	0.00851	1.21037&	-4	0.00878	1.55223& -3
200	11.0	0.00849	1.09168&	-4	0.00888	1.37013& -3
219	12.0	0.00848	1.02926&	-4	0.00850	1.67106& -3
237	13.0	0.00842	9.91915&	-5	0.00826	1.58217& -3
255	14.0	0.00841	9.16462&	-5	0.00833	2.00614& -3
273	15.0	0.00840	8.78903&	-5	0.00858	1.84965& -3
292	16.0	0.00839	8.34113&	-5	0.00876	1.48902& -3
310	17.0	0.00839	8.64773&	-5	0.00850	1.41575& -3
328	18.0	0.00836	7.65688&	-5	0.00839	2.07231& -3
346	19.0	0.00836	7.49291&	-5	0.00872	1.74059& -3
365	20.0	0.00836	7.77563&	-5	0.00906	1.18194& -3
383	21.0	0.00836	7.27643&	-5	0.00846	1.45752& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00928	4.02916&	-4	0.00983	3.66317& -3
197	2.0	0.00902	2.23482&	-4	0.00895	1.72687& -3
295	3.0	0.00862	1.57748&	-4	0.00868	1.20114& -3
394	4.0	0.00866	1.34444&	-4	0.00856	1.30554& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00868	7.59685&	-4	0.00906	2.42471& -3

Data Analysis ProgramRun Number = 117

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.06523	1.76823&	-2	1.66457	5.71588& 0
36	2.0	0.03282	5.18280&	-3	0.30583	3.99836& -1
54	3.0	0.02527	2.71056&	-3	0.06526	1.07177& -1
73	4.0	0.02352	1.77953&	-3	0.03312	3.74001& -2
91	5.0	0.02262	1.31933&	-3	0.04887	5.05105& -2
109	6.0	0.02201	1.03140&	-3	0.02763	2.70147& -2
127	7.0	0.02172	8.47437&	-4	0.02124	1.92803& -2
146	8.0	0.02130	7.29795&	-4	0.02575	3.11777& -2
164	9.0	0.02120	6.41319&	-4	0.02749	1.96542& -2
182	10.0	0.02110	5.78120&	-4	0.01944	1.91111& -2
200	11.0	0.02105	5.17944&	-4	0.02561	2.27841& -2
219	12.0	0.02098	4.84074&	-4	0.03972	3.82741& -2
237	13.0	0.02086	4.51084&	-4	0.02231	1.10434& -2
255	14.0	0.01982	3.96806&	-3	0.03000	2.45762& -2
273	15.0	0.02076	3.96499&	-4	0.02391	1.43882& -2
292	16.0	0.01980	3.50045&	-3	0.02493	1.72442& -2
310	17.0	0.02070	3.60069&	-4	0.01715	9.73651& -3
328	18.0	0.02067	3.46930&	-4	0.02466	1.97168& -2
346	19.0	0.02065	3.31003&	-4	0.02529	1.96055& -2
365	20.0	0.02064	3.17205&	-4	0.02533	2.52724& -2
383	21.0	0.02065	3.10743&	-4	0.02343	1.41789& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.02511	3.77376&	-3	0.07749	1.02622& -1
197	2.0	0.02325	1.44482&	-3	0.05177	5.64232& -2
295	3.0	0.02150	8.91991&	-4	0.03004	1.95130& -2
394	4.0	0.02297	5.50144&	-3	0.02265	1.45003& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02235	1.88593&	-3	0.04141	3.64459& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01123	1.47984&	-3	0.07726	1.62036& -1
36	2.0	0.00972	7.14446&	-4	0.05140	6.63960& -2
54	3.0	0.00887	4.75527&	-4	0.01372	1.22934& -2
73	4.0	0.00873	3.67857&	-4	0.01103	7.74414& -3
91	5.0	0.00865	3.07285&	-4	0.01521	1.19951& -2
109	6.0	0.00859	2.60764&	-4	0.01025	6.26843& -3
127	7.0	0.00855	2.29737&	-4	0.00846	4.20140& -3
146	8.0	0.00841	2.06090&	-4	0.00969	8.38421& -3
164	9.0	0.00841	1.89573&	-4	0.01023	4.76891& -3
182	10.0	0.00840	1.76798&	-4	0.00866	5.71962& -3
200	11.0	0.00840	1.62471&	-4	0.01005	6.52406& -3
219	12.0	0.00838	1.55318&	-4	0.01378	1.00523& -2
237	13.0	0.00833	1.46852&	-4	0.00881	3.50985& -3
255	14.0	0.00791	1.65589&	-3	0.01109	6.96830& -3
273	15.0	0.00832	1.33680&	-4	0.00890	3.65026& -3
292	16.0	0.00789	1.60599&	-3	0.00924	4.88393& -3
310	17.0	0.00831	1.25554&	-4	0.00736	3.22306& -3
328	18.0	0.00829	1.21273&	-4	0.00988	5.84041& -3
346	19.0	0.00829	1.16908&	-4	0.00997	6.55420& -3
365	20.0	0.00829	1.13516&	-4	0.00972	6.93898& -3
383	21.0	0.00829	1.11131&	-4	0.00900	4.59813& -3

Quadrature Size = 6

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00891	6.14219&	-4	0.01838	1.64907& -2
197	2.0	0.00881	3.38780&	-4	0.01495	1.15441& -2
295	3.0	0.00847	2.44699&	-4	0.01129	5.63673& -3
394	4.0	0.00873	7.88210&	-4	0.00886	4.11069& -3

Quadrature Size = 9

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00859	4.11415&	-4	0.01344	7.61712& -3

Data Analysis Program

Run Number = 118

Time Marker Pulse Setting = 1.0
 Number of Channels = 2
 Data Values per Channel = 400
 Sets of Readings = 15

Time Constant 1

Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.06498	2.75500&	-2	-0.06938	1.11172& 0
36	2.0	0.03329	6.80791&	-3	0.02612	2.06163& -1
54	3.0	0.02548	3.55365&	-3	-0.06957	2.15782& -1
73	4.0	0.02364	2.37256&	-3	0.08254	2.22389& -1
91	5.0	0.02270	1.71814&	-3	0.09128	1.19296& -1
109	6.0	0.02207	1.35690&	-3	0.03364	4.32595& -2
127	7.0	0.02177	1.13348&	-3	0.06470	1.09827& -1
146	8.0	0.02134	9.68865&	-4	0.05163	1.71847& -1
164	9.0	0.01999	5.50554&	-3	0.01563	1.63020& -2
182	10.0	0.01990	4.60671&	-3	0.04632	9.16697& -2
200	11.0	0.02107	7.00097&	-4	0.05950	9.57828& -2
219	12.0	0.02098	6.39690&	-4	0.01923	1.95785& -2
237	13.0	0.02086	6.08617&	-4	0.17751	6.02990& -1
255	14.0	0.02082	5.60049&	-4	0.04265	5.01856& -2
273	15.0	0.02078	5.30903&	-4	0.03025	2.80132& -2
292	16.0	0.02704	1.42890&	-2	0.03168	2.98667& -2
310	17.0	0.02071	4.98031&	-4	0.01065	3.64809& -2
328	18.0	0.02068	4.65982&	-4	0.02547	2.84605& -2
346	19.0	0.02065	4.35867&	-4	0.01915	2.16129& -2
365	20.0	0.02064	4.35652&	-4	0.02938	2.73645& -2
383	21.0	0.01986	3.10008&	-3	0.01774	8.13151& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.02725	5.07121&	-3	0.08209	1.28045& -1
197	2.0	0.02336	1.92333&	-3	0.03592	3.59891& -2
295	3.0	0.02154	1.16966&	-3	0.02448	3.17066& -2
394	4.0	0.02162	8.86366&	-4	0.04100	3.87988& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02293	3.17991&	-3	0.04876	7.33354& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01129	2.11362&	-3	0.02158	9.15731& -2
36	2.0	0.00980	9.28827&	-4	0.01654	3.05686& -2
54	3.0	0.00892	6.22464&	-4	-0.00182	3.04334& -2
73	4.0	0.00877	4.90534&	-4	0.02992	5.26090& -2
91	5.0	0.00868	4.01113&	-4	0.02278	2.23781& -2
109	6.0	0.00862	3.44830&	-4	0.01047	7.98291& -3
127	7.0	0.00858	3.07749&	-4	0.02232	3.05873& -2
146	8.0	0.00844	2.74896&	-4	0.01492	3.88874& -2
164	9.0	0.00803	1.76800&	-3	0.00711	4.20848& -3
182	10.0	0.00798	1.66837&	-3	0.01631	2.31707& -2
200	11.0	0.00842	2.20230&	-4	0.01881	2.43509& -2
219	12.0	0.00840	2.06502&	-4	0.00903	6.62569& -3
237	13.0	0.00835	1.99938&	-4	0.05605	1.81150& -1
255	14.0	0.00835	1.87330&	-4	0.01729	1.82458& -2
273	15.0	0.00834	1.80968&	-4	0.01207	1.00536& -2
292	16.0	0.00753	3.12985&	-3	0.01194	9.92708& -3
310	17.0	0.00833	1.74096&	-4	0.00665	1.02807& -2
328	18.0	0.00831	1.64450&	-4	0.01045	1.08127& -2
346	19.0	0.00831	1.55533&	-4	0.00853	9.90199& -3
365	20.0	0.00830	1.56609&	-4	0.01222	1.04628& -2
383	21.0	0.00790	1.58663&	-3	0.00874	2.11382& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00902	6.88008&	-4	0.02148	2.17536& -2
197	2.0	0.00885	4.50620&	-4	0.01217	8.36068& -3
295	3.0	0.00850	3.21741&	-4	0.01026	8.62630& -3
394	4.0	0.00856	2.68270&	-4	0.01509	1.21978& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00866	5.79488&	-4	0.01511	1.42093& -2

Data Analysis Program

Run Number = 119

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.06514	1.72787&	-2	0.76951	4.04327& 0
36	2.0	0.03352	3.58569&	-3	0.26975	5.23030& -1
54	3.0	0.02553	2.04232&	-3	0.04648	1.79918& -1
73	4.0	0.02163	8.43594&	-3	0.07628	1.78180& -1
91	5.0	0.02165	7.72019&	-3	0.07074	1.21103& -1
109	6.0	0.02208	7.61985&	-4	0.03324	3.76245& -2
127	7.0	0.02178	6.52638&	-4	0.05201	1.16583& -1
146	8.0	0.02136	5.50740&	-4	0.03309	5.03578& -2
164	9.0	0.02127	5.37598&	-4	0.03166	3.20132& -2
182	10.0	0.02116	4.37355&	-4	0.03647	3.35700& -2
200	11.0	0.01995	4.31985&	-3	0.02822	2.54712& -2
219	12.0	0.02106	3.97776&	-4	0.04297	4.73887& -2
237	13.0	0.02090	3.39682&	-4	0.02285	1.31329& -2
255	14.0	0.02085	3.46554&	-4	0.03671	4.48722& -2
273	15.0	0.02079	3.10665&	-4	0.05099	8.19624& -2
292	16.0	0.02081	2.80986&	-4	0.01887	1.16651& -2
310	17.0	0.02074	2.69746&	-4	0.01691	1.20254& -2
328	18.0	0.01965	4.17158&	-3	0.02396	1.67635& -2
346	19.0	0.02068	2.65577&	-4	0.02597	2.14978& -2
365	20.0	0.02067	2.45257&	-4	0.01746	9.26284& -3
383	21.0	0.02067	2.29886&	-4	0.02861	3.03043& -2

Quadrature Size = 6

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.02558	2.76698&	-3	0.11321	2.16188& -1
197	2.0	0.02341	1.06802&	-3	0.04366	4.87859& -2
295	3.0	0.02163	6.70821&	-4	0.02944	2.10205& -2
394	4.0	0.02161	5.06023&	-4	0.03775	4.33360& -2

Quadrature Size = 9

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02257	1.37022&	-3	0.04162	4.59276& -2

Time Constant 2Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.00280	4.01899& -4	0.04189	1.73464& -1
36	2.0	0.00247	1.28837& -4	0.01213	1.69663& -2
54	3.0	0.00224	9.00211& -5	0.00233	4.94885& -3
73	4.0	0.00210	4.44317& -4	0.00508	9.04292& -3
91	5.0	0.00205	4.25465& -4	0.00451	5.30533& -3
109	6.0	0.00216	4.88039& -5	0.00321	2.55984& -3
127	7.0	0.00215	4.46631& -5	0.00410	6.90358& -3
146	8.0	0.00212	3.96767& -5	0.00297	3.51629& -3
164	9.0	0.00212	3.97246& -5	0.00283	1.86487& -3
182	10.0	0.00212	3.35317& -5	0.00336	2.40325& -3
200	11.0	0.00201	4.15259& -4	0.00286	2.20586& -3
219	12.0	0.00211	3.21172& -5	0.00381	2.80595& -3
237	13.0	0.00210	2.82486& -5	0.00231	1.02314& -3
255	14.0	0.00210	2.93700& -5	0.00302	2.09370& -3
273	15.0	0.00210	2.59581& -5	0.00450	6.14189& -3
292	16.0	0.00210	2.37775& -5	0.00194	8.08579& -4
310	17.0	0.00209	2.36625& -5	0.00185	1.06426& -3
328	18.0	0.00200	3.40007& -4	0.00273	1.62054& -3
346	19.0	0.00209	2.37753& -5	0.00269	1.84059& -3
365	20.0	0.00209	2.22152& -5	0.00199	9.40775& -4
383	21.0	0.00209	2.09091& -5	0.00271	2.29303& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.00226	1.14236& -4	0.00654	9.65434& -3
197	2.0	0.00223	6.36052& -5	0.00358	3.06521& -3
295	3.0	0.00214	4.62048& -5	0.00277	1.51693& -3
394	4.0	0.00215	3.85949& -5	0.00333	2.62922& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00217	7.54203& -5	0.00336	2.46164& -3

Data Analysis Program

Run Number = 120

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.07430	1.48851&	-2	-0.13690	5.34630& -1
36	2.0	0.03544	4.15096&	-3	-0.05166	2.46629& -1
54	3.0	0.02645	2.48946&	-3	-0.05418	1.85784& -1
73	4.0	0.02443	1.48220&	-3	0.00832	1.61146& -1
91	5.0	0.02319	1.12697&	-3	0.01540	2.89104& -1
109	6.0	0.02236	8.41546&	-4	-0.01269	1.44049& -1
127	7.0	0.01104	8.02611&	-4	0.00579	1.47951& -1
146	8.0	0.02158	6.47878&	-4	0.00794	6.42010& -2
164	9.0	0.02145	5.68738&	-4	-0.00818	8.10489& -2
182	10.0	0.02137	5.62474&	-4	-0.00910	4.28522& -2
200	11.0	0.02132	4.88030&	-4	-0.00384	5.45906& -2
219	12.0	0.02117	4.20344&	-4	0.02634	6.46971& -2
237	13.0	0.02106	3.87451&	-4	-0.01261	9.36050& -2
255	14.0	0.02099	3.72303&	-4	-0.05416	1.56364& -1
273	15.0	0.02092	3.73268&	-4	0.02804	6.25207& -2
292	16.0	0.02092	3.30587&	-4	0.01264	1.83909& -2
310	17.0	0.02082	3.24892&	-4	-0.00220	4.78068& -2
328	18.0	0.02079	3.30734&	-4	-0.05015	1.85849& -1
346	19.0	0.01966	4.20789&	-3	-0.00710	6.45327& -2
365	20.0	0.02073	2.65056&	-4	-0.01300	5.46115& -2
383	21.0	0.02071	2.88885&	-4	-0.00556	7.57670& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.02703	3.23906&	-3	-0.07035	2.54133& -1
197	2.0	0.02399	1.22627&	-3	-0.00247	1.21663& -1
295	3.0	0.02193	8.03139&	-4	0.00441	7.24253& -2
394	4.0	0.02186	5.57096&	-4	0.02074	7.74813& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02328	1.59088&	-3	-0.03470	1.75658& -1

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00302	3.16425&	-4	0.00860	3.41718& -2
36	2.0	0.00254	1.46589&	-4	0.00323	1.64269& -2
54	3.0	0.00229	1.08502&	-4	0.00306	1.27135& -2
73	4.0	0.00225	7.88775&	-5	0.00598	1.62127& -2
91	5.0	0.00222	6.55920&	-5	0.00851	3.46579& -2
109	6.0	0.00219	5.42658&	-5	0.00389	1.24387& -2
127	7.0	0.00218	5.35187&	-5	0.00389	1.72392& -2
146	8.0	0.00214	4.66739&	-5	0.00248	5.77754& -3
164	9.0	0.00214	4.21279&	-5	0.00165	8.29746& -3
182	10.0	0.00214	4.28345&	-5	0.00027	3.81709& -3
200	11.0	0.00214	3.87076&	-5	0.00155	4.33174& -3
219	12.0	0.00213	3.43022&	-5	0.00439	7.56800& -3
237	13.0	0.00212	3.13001&	-5	0.00039	8.17454& -3
255	14.0	0.00212	3.12168&	-5	-0.00424	1.69113& -2
273	15.0	0.00211	3.11024&	-5	0.00402	5.20225& -3
292	16.0	0.00212	2.79604&	-5	0.00192	2.04618& -3
310	17.0	0.00211	2.83002&	-5	0.00060	5.43725& -3
328	18.0	0.00210	2.91164&	-5	-0.00628	2.41740& -2
346	19.0	0.00201	3.48517&	-4	0.00035	5.03486& -3
365	20.0	0.00210	2.40185&	-5	-0.00047	6.28710& -3
383	21.0	0.00210	2.64353&	-5	0.00094	8.43753& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00233	1.33400&	-4	0.00103	1.61548& -2
197	2.0	0.00227	7.31500&	-5	0.00253	7.15947& -3
295	3.0	0.00217	5.50961&	-5	0.00203	4.11283& -3
394	4.0	0.00218	4.21815&	-5	0.00318	5.53090& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00222	8.79478&	-5	0.00096	1.09901& -2

Data Analysis Program

Run Number = 121

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.07622	1.42570& -2	-0.18564	5.38074& -1
36	2.0	0.03600	4.00225& -3	-0.29318	2.51095& -1
54	3.0	0.02545	7.08789& -3	-0.09520	1.61800& -1
73	4.0	0.02465	1.43153& -3	-0.00672	1.18602& -1
91	5.0	0.02143	6.90216& -3	-0.09067	1.21466& -1
109	6.0	0.02260	9.04071& -4	0.01228	2.58392& -1
127	7.0	0.02220	6.81064& -4	-0.07271	1.08752& -1
146	8.0	0.02174	6.29552& -4	-0.01124	5.82520& -2
164	9.0	0.02161	5.54015& -4	-0.02542	7.20062& -2
182	10.0	0.02145	4.81755& -4	-0.00727	4.42504& -2
200	11.0	0.02139	4.43412& -4	-0.00212	6.03242& -2
219	12.0	0.02129	3.82092& -4	-0.00123	1.29158& -1
237	13.0	0.02112	3.89167& -4	-0.02248	1.26906& -1
255	14.0	0.02107	3.91766& -4	0.03318	9.61549& -2
273	15.0	0.01994	4.13987& -3	-0.02743	6.84413& -2
292	16.0	0.02101	2.97800& -4	-0.02082	4.31126& -2
310	17.0	0.01707	1.49643& -2	0.04033	1.86254& -1
328	18.0	0.02087	3.02689& -4	-0.00531	3.53414& -2
346	19.0	0.02084	2.56002& -4	0.03616	9.89935& -2
365	20.0	0.02080	2.59821& -4	-0.02054	6.32441& -2
383	21.0	0.02078	2.66008& -4	0.01176	6.36366& -2

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.02735	3.19480& -3	-0.04760	2.27334& -1
197	2.0	0.02418	1.17090& -3	-0.12829	1.55214& -1
295	3.0	0.02177	1.76492& -3	-0.01811	1.02345& -1
394	4.0	0.02197	5.07540& -4	-0.00533	6.74581& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.02346	1.59037& -3	-0.05039	1.21890& -1

Time Constant 2Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.00306	3.09698& -4	0.01780	3.90945& -2
36	2.0	0.00256	1.40622& -4	-0.00484	3.56468& -2
54	3.0	0.00225	2.69811& -4	-0.00328	1.52450& -2
73	4.0	0.00226	7.53429& -5	0.00307	1.17935& -2
91	5.0	0.00210	4.33121& -4	-0.00156	1.34936& -2
109	6.0	0.00220	5.80674& -5	0.00710	2.95795& -2
127	7.0	0.00219	4.71202& -5	-0.00021	1.18642& -2
146	8.0	0.00215	4.49596& -5	0.00175	7.34019& -3
164	9.0	0.00215	4.11467& -5	0.00173	9.38630& -3
182	10.0	0.00214	3.67691& -5	0.00326	5.37578& -3
200	11.0	0.00214	3.50798& -5	0.00030	4.13956& -3
219	12.0	0.00214	3.06612& -5	0.00269	1.54524& -2
237	13.0	0.00212	3.25182& -5	-0.00123	2.17614& -2
255	14.0	0.00212	3.32184& -5	0.00619	1.86573& -2
273	15.0	0.00203	3.23696& -4	-0.00254	1.27114& -2
292	16.0	0.00212	2.55297& -5	-0.00073	5.32016& -3
310	17.0	0.00190	8.40722& -4	0.00606	2.63322& -2
328	18.0	0.00211	2.71275& -5	0.00074	3.59081& -3
346	19.0	0.00211	2.31836& -5	0.00576	1.30460& -2
365	20.0	0.00210	2.33577& -5	-0.00109	6.93968& -3
383	21.0	0.00210	2.40330& -5	0.00411	8.00892& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.00234	1.32037& -4	0.00926	1.57435& -2
197	2.0	0.00227	6.94917& -5	-0.00542	1.67424& -2
295	3.0	0.00216	1.12528& -4	0.00168	1.10238& -2
394	4.0	0.00218	3.89421& -5	0.00213	8.86906& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00223	8.81364& -5	0.00208	6.36849& -3

Data Analysis ProgramRun Number = 122

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01960	2.56801&	-2	-0.03229	2.34511& -1
36	2.0	0.02401	1.41641&	-2	0.02000	2.01847& -2
54	3.0	0.02432	1.05959&	-2	0.02585	1.30010& -2
73	4.0	0.02594	8.62781&	-3	0.02979	1.04313& -2
91	5.0	0.02667	7.88182&	-3	0.03121	1.07565& -2
109	6.0	0.02705	7.32919&	-3	0.02764	1.01096& -2
127	7.0	0.02738	6.90016&	-3	0.02823	9.73088& -3
146	8.0	0.02740	6.74844&	-3	0.02731	8.78247& -3
164	9.0	0.02752	6.70869&	-3	0.02796	8.70367& -3
182	10.0	0.02757	6.81688&	-3	0.02699	8.35348& -3
200	11.0	0.02762	6.87918&	-3	0.02734	7.45856& -3
219	12.0	0.02760	7.13045&	-3	0.02667	8.91687& -3
237	13.0	0.02761	7.24922&	-3	0.02892	8.59538& -3
255	14.0	0.02767	7.32345&	-3	0.02954	7.71864& -3
273	15.0	0.02776	7.33113&	-3	0.02811	7.25028& -3
292	16.0	0.02788	7.31441&	-3	0.02785	7.75758& -3
310	17.0	0.02801	7.31997&	-3	0.02735	8.17571& -3
328	18.0	0.02817	7.32523&	-3	0.02771	7.93006& -3
346	19.0	0.02836	7.28804&	-3	0.02808	7.61269& -3
365	20.0	0.02856	7.26990&	-3	0.02863	8.00419& -3
383	21.0	0.02879	7.28719&	-3	0.02912	8.07803& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.02116	1.10645&	-2	0.02486	1.14816& -2
197	2.0	0.02696	8.25067&	-3	0.02595	8.00437& -3
295	3.0	0.02686	7.27092&	-3	0.02743	8.07086& -3
394	4.0	0.02787	7.01549&	-3	0.03055	1.08695& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02430	8.38680&	-3	0.02555	4.29720& -3

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01840	5.33076&	-3	0.01821	1.13068& -2
36	2.0	0.01918	5.03569&	-3	0.01783	6.25687& -3
54	3.0	0.01865	4.74498&	-3	0.01889	5.73257& -3
73	4.0	0.01905	4.71323&	-3	0.02062	5.76873& -3
91	5.0	0.01927	4.72293&	-3	0.01956	4.29435& -3
109	6.0	0.01941	4.67465&	-3	0.01988	5.59656& -3
127	7.0	0.01952	4.62577&	-3	0.02022	5.66725& -3
146	8.0	0.01941	4.59003&	-3	0.01963	5.31157& -3
164	9.0	0.01948	4.59592&	-3	0.01989	5.35303& -3
182	10.0	0.01953	4.61577&	-3	0.01935	5.14010& -3
200	11.0	0.01956	4.63987&	-3	0.01935	4.83210& -3
219	12.0	0.01958	4.66763&	-3	0.01935	5.35078& -3
237	13.0	0.01957	4.67879&	-3	0.02033	5.45378& -3
255	14.0	0.01961	4.70294&	-3	0.02069	5.01856& -3
273	15.0	0.01965	4.72425&	-3	0.01997	4.86502& -3
292	16.0	0.01972	4.74097&	-3	0.01968	5.06223& -3
310	17.0	0.01979	4.76140&	-3	0.01949	5.27397& -3
328	18.0	0.01986	4.77790&	-3	0.01948	5.08183& -3
346	19.0	0.01997	4.78622&	-3	0.01990	5.13556& -3
365	20.0	0.02008	4.80151&	-3	0.02020	5.32246& -3
383	21.0	0.02022	4.83293&	-3	0.02050	5.41146& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01790	4.66384&	-3	0.01814	4.12796& -3
197	2.0	0.01943	4.79524&	-3	0.01872	4.87877& -3
295	3.0	0.01923	4.63056&	-3	0.01948	5.14818& -3
394	4.0	0.01973	4.67720&	-3	0.02087	5.62823& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01839	4.60932&	-3	0.01864	4.12875& -3

Data Analysis ProgramRun Number = 123

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.01383	3.18091& -2	0.05985	1.75517& -1
36	2.0	0.02326	1.17672& -2	0.00941	3.34246& -2
54	3.0	0.02416	8.17693& -3	0.03065	2.51103& -2
73	4.0	0.02585	6.77620& -3	0.02754	2.30954& -2
91	5.0	0.02669	6.07744& -3	0.02322	2.13558& -2
109	6.0	0.02732	4.98669& -3	0.02464	1.48166& -2
127	7.0	0.02775	4.26319& -3	0.03015	2.46801& -2
146	8.0	0.02789	3.76530& -3	0.03047	1.23108& -2
164	9.0	0.02813	3.38844& -3	0.03657	1.55937& -2
182	10.0	0.02830	3.10852& -3	0.03616	2.01751& -2
200	11.0	0.02844	2.88322& -3	0.03375	9.42246& -3
219	12.0	0.02729	5.53460& -3	0.02651	8.25497& -3
237	13.0	0.02864	2.55009& -3	0.03376	1.37752& -2
255	14.0	0.02876	2.42306& -3	0.03163	1.08890& -2
273	15.0	0.02889	2.31972& -3	0.02947	1.18411& -2
292	16.0	0.02903	2.22597& -3	0.03049	1.24785& -2
310	17.0	0.02920	2.15701& -3	0.03304	8.36722& -3
328	18.0	0.02342	2.29166& -2	0.03219	3.94220& -3
346	19.0	0.02957	2.03333& -3	0.03033	1.24429& -2
365	20.0	0.02979	1.98117& -3	0.03376	1.19503& -2
383	21.0	0.03003	1.94301& -3	0.03560	1.28414& -2

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.02018	1.06163& -2	0.01946	3.38885& -2
197	2.0	0.02735	4.88800& -3	0.02733	1.24480& -2
295	3.0	0.03017	1.16240& -2	0.02832	8.48523& -3
394	4.0	0.02698	6.98781& -3	0.03051	1.20603& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.02419	6.49825& -3	0.02358	1.79115& -2

Time Constant 2

Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01780	5.18277&	-3	0.03012	3.09807& -2
36	2.0	0.01921	3.43631&	-3	0.01682	9.34954& -3
54	3.0	0.01884	2.91328&	-3	0.02188	9.12235& -3
73	4.0	0.01933	2.75893&	-3	0.02180	1.02055& -2
91	5.0	0.01959	2.70370&	-3	0.01825	8.07127& -3
109	6.0	0.01982	2.41091&	-3	0.01859	6.82286& -3
127	7.0	0.01998	2.19103&	-3	0.02105	1.17817& -2
146	8.0	0.01992	2.01845&	-3	0.02096	6.54343& -3
164	9.0	0.02004	1.88433&	-3	0.02352	9.02765& -3
182	10.0	0.02013	1.78098&	-3	0.02415	1.04632& -2
200	11.0	0.02020	1.69099&	-3	0.02317	5.25739& -3
219	12.0	0.01923	4.26316&	-3	0.01891	5.73566& -3
237	13.0	0.02026	1.54972&	-3	0.02334	7.43290& -3
255	14.0	0.02033	1.49410&	-3	0.02178	6.44331& -3
273	15.0	0.02040	1.44779&	-3	0.02116	7.06569& -3
292	16.0	0.02048	1.40441&	-3	0.02186	7.55209& -3
310	17.0	0.02057	1.37238&	-3	0.02307	5.95777& -3
328	18.0	0.01799	1.02706&	-2	0.02272	3.58776& -3
346	19.0	0.02077	1.31422&	-3	0.02141	7.65919& -3
365	20.0	0.02090	1.28954&	-3	0.02346	7.39397& -3
383	21.0	0.02104	1.27123&	-3	0.02473	7.27038& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01785	3.48850&	-3	0.01771	1.01779& -2
197	2.0	0.01986	2.30447&	-3	0.02045	5.73806& -3
295	3.0	0.02024	2.89319&	-3	0.02040	4.53170& -3
394	4.0	0.01942	3.89357&	-3	0.02072	5.36873& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01860	2.79963&	-3	0.01846	7.58319& -3

Data Analysis ProgramRun Number = 124

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.28293	9.94628&	-1	-0.05976	2.86114& -1
36	2.0	0.16961	4.91711&	-1	0.12710	1.98701& -1
54	3.0	0.04536	7.13055&	-2	0.08929	1.27848& -1
73	4.0	0.04132	5.13899&	-2	0.03963	6.57914& -2
91	5.0	0.04117	4.87949&	-2	0.03997	4.73181& -2
109	6.0	0.03358	1.83972&	-2	0.02423	3.47044& -2
127	7.0	0.03294	1.50716&	-2	0.02758	2.46425& -2
146	8.0	0.03135	9.13068&	-3	0.04486	9.31373& -2
164	9.0	0.02969	2.37697&	-3	0.03474	2.96334& -2
182	10.0	0.02481	1.49506&	-2	0.03230	2.03150& -2
200	11.0	0.02603	8.71876&	-3	0.02663	2.96089& -2
219	12.0	0.02735	7.62845&	-3	0.05855	5.63216& -2
237	13.0	0.02716	8.48216&	-3	0.03383	2.27922& -2
255	14.0	0.02723	8.52857&	-3	0.03507	2.77238& -2
273	15.0	0.02728	8.69736&	-3	0.02616	2.52207& -2
292	16.0	0.02737	8.76025&	-3	0.03559	2.62574& -2
310	17.0	0.02749	8.80847&	-3	0.02883	2.42757& -2
328	18.0	0.02763	8.85392&	-3	0.03448	2.49323& -2
346	19.0	0.02781	8.84395&	-3	0.04435	1.91213& -2
365	20.0	0.02634	1.06688&	-2	0.03739	3.15743& -2
383	21.0	0.02821	8.93123&	-3	0.03043	1.74107& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.06272	1.50252&	-1	0.02314	8.23402& -2
197	2.0	0.03061	1.54634&	-2	0.02498	3.26235& -2
295	3.0	0.02688	6.81167&	-3	0.04541	2.11727& -2
394	4.0	0.02730	8.76113&	-3	0.02919	2.37512& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.02834	7.90871&	-3	0.01957	5.66167& -2

Time Constant 2Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.01856	5.31788& -3	0.01462	3.19484& -2
36	2.0	0.02027	6.82932& -3	0.04491	5.06181& -2
54	3.0	0.01850	5.15844& -3	0.04207	3.43993& -2
73	4.0	0.01886	5.23922& -3	0.02402	1.47783& -2
91	5.0	0.01906	5.26930& -3	0.02772	1.88023& -2
109	6.0	0.01918	5.31739& -3	0.02133	1.41211& -2
127	7.0	0.01927	5.35696& -3	0.02093	1.08628& -2
146	8.0	0.01914	5.30245& -3	0.02770	3.16367& -2
164	9.0	0.01921	5.32147& -3	0.02371	1.30830& -2
182	10.0	0.01781	7.53971& -3	0.02198	1.14229& -2
200	11.0	0.01851	6.01951& -3	0.02002	1.36804& -2
219	12.0	0.01932	5.35487& -3	0.03128	2.11819& -2
237	13.0	0.01930	5.35035& -3	0.02423	1.30330& -2
255	14.0	0.01935	5.36169& -3	0.02405	1.26563& -2
273	15.0	0.01940	5.37586& -3	0.02082	1.01210& -2
292	16.0	0.01946	5.39125& -3	0.02401	1.64784& -2
310	17.0	0.01953	5.41078& -3	0.02101	1.28215& -2
328	18.0	0.01960	5.42918& -3	0.02350	1.58088& -2
346	19.0	0.01969	5.45504& -3	0.02673	1.53271& -2
365	20.0	0.01879	6.59564& -3	0.02569	1.72759& -2
383	21.0	0.01993	5.52159& -3	0.02231	1.09019& -2

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.01780	4.98059& -3	0.02178	1.78947& -2
197	2.0	0.01846	6.00030& -3	0.01897	1.40658& -2
295	3.0	0.01899	5.27934& -3	0.02626	1.34189& -2
394	4.0	0.01946	5.40302& -3	0.02228	1.13545& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.01822	5.10421& -3	0.02083	1.35189& -2

Data Analysis Program

Run Number = 125

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.01828	2.03082& -2	0.00902	9.59923& -2
36	2.0	0.02526	6.42394& -3	0.03225	4.06311& -2
54	3.0	0.02575	3.56674& -3	0.03040	1.30832& -2
73	4.0	0.02726	2.43009& -3	0.02975	1.49474& -2
91	5.0	0.02807	1.88725& -3	0.02868	1.17495& -2
109	6.0	0.02844	1.52355& -3	0.02850	1.06610& -2
127	7.0	0.02872	1.32318& -3	0.02734	6.44570& -3
146	8.0	0.02877	1.17816& -3	0.03201	7.32479& -3
164	9.0	0.02893	1.04592& -3	0.03283	7.12292& -3
182	10.0	0.02901	9.59442& -4	0.03073	4.68416& -3
200	11.0	0.02910	8.90806& -4	0.03138	8.40955& -3
219	12.0	0.02916	8.40454& -4	0.03020	7.63629& -3
237	13.0	0.02923	7.83731& -4	0.03077	6.89075& -3
255	14.0	0.02932	7.48746& -4	0.03127	6.20583& -3
273	15.0	0.02943	7.15263& -4	0.03000	5.61907& -3
292	16.0	0.02957	6.93852& -4	0.02991	6.74693& -3
310	17.0	0.02373	2.31182& -2	0.02823	7.23790& -3
328	18.0	0.02988	6.41526& -4	0.03150	7.39295& -3
346	19.0	0.03005	6.23728& -4	0.03268	6.19826& -3
365	20.0	0.03026	6.18338& -4	0.03012	4.01279& -3
383	21.0	0.03050	6.11149& -4	0.03181	7.48448& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.02218	4.99103& -3	0.02123	2.48324& -2
197	2.0	0.02831	2.15155& -3	0.02901	9.53677& -3
295	3.0	0.02826	1.41103& -3	0.02934	6.08649& -3
394	4.0	0.03083	5.74321& -3	0.03069	6.08559& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.02549	2.72897& -3	0.02493	1.22402& -2

Time Constant 2Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.01055	2.01577& -3	0.01006	7.81438& -3
36	2.0	0.01129	1.08534& -3	0.01265	5.93168& -3
54	3.0	0.01107	7.55409& -4	0.01199	2.85176& -3
73	4.0	0.01135	5.98040& -4	0.01182	5.15217& -3
91	5.0	0.01152	5.11347& -4	0.01197	2.96180& -3
109	6.0	0.01162	4.42973& -4	0.01168	2.97073& -3
127	7.0	0.01168	4.05441& -4	0.01132	1.81384& -3
146	8.0	0.01163	3.72325& -4	0.01250	2.26521& -3
164	9.0	0.01168	3.43330& -4	0.01287	2.15269& -3
182	10.0	0.01171	3.20994& -4	0.01248	1.43316& -3
200	11.0	0.01174	3.05715& -4	0.01233	2.78611& -3
219	12.0	0.01176	2.93060& -4	0.01194	2.49729& -3
237	13.0	0.01176	2.75948& -4	0.01238	2.42147& -3
255	14.0	0.01179	2.67586& -4	0.01236	2.12266& -3
273	15.0	0.01183	2.58480& -4	0.01196	1.86243& -3
292	16.0	0.01187	2.53179& -4	0.01183	2.28317& -3
310	17.0	0.01042	5.79386& -3	0.01129	2.60920& -3
328	18.0	0.01196	2.37082& -4	0.01250	2.57896& -3
346	19.0	0.01202	2.32563& -4	0.01299	2.11079& -3
365	20.0	0.01209	2.31892& -4	0.01218	1.45374& -3
383	21.0	0.01217	2.29854& -4	0.01271	2.65864& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.01056	9.69015& -4	0.01053	4.45095& -3
197	2.0	0.01159	5.80177& -4	0.01191	2.62879& -3
295	3.0	0.01151	4.32335& -4	0.01173	1.95967& -3
394	4.0	0.01207	9.47553& -4	0.01238	1.93145& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.01093	6.83900& -4	0.01090	3.03045& -3

Data Analysis ProgramRun Number = 126

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.08240	1.61734& -2	0.80246	2.28409& 0
36	2.0	0.04122	1.72448& -2	-0.03822	2.68155& -1
54	3.0	0.03744	3.13780& -3	0.04509	5.59786& -2
73	4.0	0.03500	1.95714& -3	0.07554	6.03714& -2
91	5.0	0.03395	1.50823& -3	0.03615	2.58131& -2
109	6.0	0.03326	1.22407& -3	0.03166	6.66274& -2
127	7.0	0.03287	1.06713& -3	0.05410	3.55511& -2
146	8.0	0.03241	9.30046& -4	0.04255	2.93538& -2
164	9.0	0.03220	8.41750& -4	0.04467	3.33816& -2
182	10.0	0.03203	7.73070& -4	0.02756	1.65740& -2
200	11.0	0.03025	6.40093& -3	0.03443	2.85251& -2
219	12.0	0.03015	6.45040& -3	0.02998	1.82039& -2
237	13.0	0.03167	6.55921& -4	0.04606	4.44702& -2
255	14.0	0.03166	6.04860& -4	0.04604	2.52180& -2
273	15.0	0.03168	5.68333& -4	0.03346	1.69958& -2
292	16.0	0.03170	5.61046& -4	0.03745	3.30216& -2
310	17.0	0.03176	5.44638& -4	0.03863	2.18939& -2
328	18.0	0.03186	5.19142& -4	0.03698	2.30161& -2
346	19.0	0.03201	5.14023& -4	0.03780	3.08939& -2
365	20.0	0.03217	5.05381& -4	0.05541	3.54062& -2
383	21.0	0.03237	4.82388& -4	0.04278	2.39172& -2

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.03783	3.97962& -3	0.05223	6.56088& -2
197	2.0	0.03301	8.16620& -3	0.03202	2.86025& -2
295	3.0	0.03266	1.12089& -3	0.03635	2.84603& -2
394	4.0	0.03093	7.00784& -3	0.03658	1.63156& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.03403	2.18767& -3	0.03895	2.95689& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01745	1.89857&	-3	0.11066	2.38184& -1
36	2.0	0.01412	3.09390&	-3	0.00520	3.04801& -2
54	3.0	0.01336	1.00004&	-3	0.01576	1.28806& -2
73	4.0	0.01332	5.04032&	-4	0.02297	1.49441& -2
91	5.0	0.01318	4.24537&	-4	0.01362	7.15046& -3
109	6.0	0.01307	3.66834&	-4	0.01423	1.38149& -2
127	7.0	0.01300	3.35274&	-4	0.02009	1.17877& -2
146	8.0	0.01283	3.02479&	-4	0.01685	9.53302& -3
164	9.0	0.01280	2.81003&	-4	0.01622	8.51158& -3
182	10.0	0.01277	2.63233&	-4	0.01128	5.58015& -3
200	11.0	0.01222	2.03767&	-3	0.01365	8.95885& -3
219	12.0	0.01219	2.09636&	-3	0.01268	6.55818& -3
237	13.0	0.01266	2.34433&	-4	0.01794	1.31643& -2
255	14.0	0.01267	2.18793&	-4	0.01803	8.45827& -3
273	15.0	0.01268	2.08315&	-4	0.01297	5.11784& -3
292	16.0	0.01269	2.06652&	-4	0.01463	1.05033& -2
310	17.0	0.01271	2.02632&	-4	0.01528	7.18310& -3
328	18.0	0.01274	1.93991&	-4	0.01356	7.00867& -3
346	19.0	0.01280	1.93563&	-4	0.01471	9.92630& -3
365	20.0	0.01285	1.91566&	-4	0.02173	1.16064& -2
383	21.0	0.01292	1.83618&	-4	0.01633	7.56354& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.01371	8.23602&	-4	0.01774	1.34613& -2
197	2.0	0.01295	2.10186&	-3	0.01252	6.92581& -3
295	3.0	0.01291	3.51529&	-4	0.01355	7.25524& -3
394	4.0	0.01242	2.25673&	-3	0.01426	5.71112& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01315	5.70826&	-4	0.01498	7.25327& -3

Data Analysis Program

Run Number = 127

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.01029	2.25892&	-1	-0.18891	8.57150& -1
36	2.0	0.01821	8.33854&	-2	0.10385	3.90718& -1
54	3.0	0.01773	4.60632&	-2	-0.07920	5.86811& -1
73	4.0	0.01412	5.83866&	-2	-0.01064	4.16143& -2
91	5.0	0.01224	5.51283&	-2	-0.03810	1.78194& -1
109	6.0	0.02483	9.94733&	-3	0.01798	6.29177& -2
127	7.0	0.02423	6.54385&	-3	0.04652	4.53784& -2
146	8.0	0.02334	1.30744&	-2	0.02749	6.32822& -2
164	9.0	0.02305	1.38435&	-2	0.04084	3.56475& -2
182	10.0	0.02465	8.17065&	-3	0.04223	6.50626& -2
200	11.0	0.02343	1.21853&	-2	0.01989	5.14257& -2
219	12.0	0.02371	1.13755&	-2	0.05620	7.87946& -2
237	13.0	0.02344	1.24060&	-2	0.05659	1.36342& -1
255	14.0	0.02389	1.10306&	-2	0.00969	3.35986& -2
273	15.0	0.02380	1.16669&	-2	0.01245	7.90428& -2
292	16.0	0.02285	1.11898&	-2	0.02979	3.27168& -2
310	17.0	0.02308	1.19655&	-2	0.02341	2.30455& -2
328	18.0	0.02481	9.81489&	-3	0.03634	8.34039& -2
346	19.0	0.02458	1.09257&	-2	-0.00801	1.09741& -1
365	20.0	0.02504	1.00624&	-2	0.03186	6.32248& -2
383	21.0	0.02503	1.07940&	-2	0.02691	8.20466& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00844	7.24116&	-2	0.15682	5.15112& -1
197	2.0	0.02271	1.92433&	-2	0.00791	9.05064& -2
295	3.0	0.02062	1.57080&	-2	0.04111	6.65688& -2
394	4.0	0.02589	5.35390&	-3	0.00629	4.99450& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.01164	5.08864&	-2	0.02463	1.00445& -1

Time Constant 2Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.00824	4.00460& -3	0.01894	1.42983& -1
36	2.0	0.00906	3.98861& -3	0.04684	8.12682& -2
54	3.0	0.00847	4.29548& -3	0.00428	9.58025& -2
73	4.0	0.00916	3.97231& -3	0.00550	4.34672& -3
91	5.0	0.00935	3.99737& -3	0.00388	3.56561& -2
109	6.0	0.00947	3.99730& -3	0.01216	1.72124& -2
127	7.0	0.00921	4.05003& -3	0.01454	1.33048& -2
146	8.0	0.00954	3.98450& -3	0.01387	1.99411& -2
164	9.0	0.00960	3.99831& -3	0.01592	1.12201& -2
182	10.0	0.00965	4.00787& -3	0.01781	1.87671& -2
200	11.0	0.00968	4.01382& -3	0.00944	1.54239& -2
219	12.0	0.00971	4.02180& -3	0.02158	2.68037& -2
237	13.0	0.00971	4.01795& -3	0.02134	3.34062& -2
255	14.0	0.00973	4.02376& -3	0.00764	7.55512& -3
273	15.0	0.00977	4.03602& -3	0.01136	1.41543& -2
292	16.0	0.00929	4.30326& -3	0.01164	1.26900& -2
310	17.0	0.00944	4.38990& -3	0.01076	6.60848& -3
328	18.0	0.00989	4.07729& -3	0.01713	3.11148& -2
346	19.0	0.00994	4.09904& -3	0.00102	3.97905& -2
365	20.0	0.00999	4.11943& -3	0.01589	1.86522& -2
383	21.0	0.01006	4.15025& -3	0.01332	3.02409& -2

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.00844	3.75146& -3	0.04267	1.05051& -1
197	2.0	0.00945	3.98464& -3	0.01271	1.59475& -2
295	3.0	0.00898	4.12785& -3	0.01629	1.87144& -2
394	4.0	0.00971	4.04757& -3	0.00868	9.31784& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00886	3.80607& -3	0.01547	1.94985& -2

Data Analysis Program

Run Number = 128

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD.	DEV.	MEAN	STD. DEV.
18	1.0	0.04610	1.49614&	-2	0.11725	4.46261& -1
36	2.0	0.03390	4.68946&	-3	0.06358	1.46093& -1
54	3.0	0.03064	2.79853&	-3	0.09259	1.02470& -1
73	4.0	0.03064	1.84746&	-3	0.06274	8.32648& -2
91	5.0	0.03060	1.42991&	-3	0.05018	6.26398& -2
109	6.0	0.03045	1.20662&	-3	0.07885	1.36222& -1
127	7.0	0.03055	9.93810&	-4	0.05422	4.80069& -2
146	8.0	0.03043	8.28939&	-4	0.01252	8.33236& -2
164	9.0	0.03037	7.57675&	-4	0.06687	7.28663& -2
182	10.0	0.03037	7.00239&	-4	0.07652	1.31501& -1
200	11.0	0.03036	6.82732&	-4	0.02540	1.43575& -2
219	12.0	0.02308	2.31680&	-2	0.04201	2.81955& -2
237	13.0	0.03032	5.98673&	-4	0.03572	3.33961& -2
255	14.0	0.03038	5.74333&	-4	0.02921	1.90081& -2
273	15.0	0.03040	5.82316&	-4	0.05724	6.05453& -2
292	16.0	0.02947	4.34257&	-3	-0.04570	4.12948& -1
310	17.0	0.03062	5.07258&	-4	0.05787	7.20727& -2
328	18.0	0.03075	5.41943&	-4	0.04298	2.75844& -2
346	19.0	0.03092	5.07910&	-4	0.04389	2.50498& -2
365	20.0	0.03107	4.59983&	-4	0.03904	3.28276& -2
383	21.0	0.03129	4.47672&	-4	0.02906	2.10663& -2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD.	DEV.	MEAN	STD. DEV.
98	1.0	0.02899	3.68939&	-3	0.01683	6.35245& -2
197	2.0	0.03122	1.60405&	-3	0.03002	4.75446& -2
295	3.0	0.03022	1.12058&	-3	0.04971	2.96617& -2
394	4.0	0.03087	8.30126&	-4	0.03744	2.44815& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD.	DEV.	MEAN	STD. DEV.
257	1.0	0.02920	2.02467&	-3	0.02676	4.33360& -2

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00334	3.97925&	-4	0.00828	1.01865& -2
36	2.0	0.00319	2.02423&	-4	0.00513	6.49982& -3
54	3.0	0.00303	1.50085&	-4	0.00693	6.10366& -3
73	4.0	0.00305	1.15481&	-4	0.00547	5.56496& -3
91	5.0	0.00306	9.74906&	-5	0.00410	3.28378& -3
109	6.0	0.00305	8.90271&	-5	0.00597	8.37212& -3
127	7.0	0.00306	7.69364&	-5	0.00500	3.76236& -3
146	8.0	0.00304	6.63328&	-5	0.00236	4.64199& -3
164	9.0	0.00304	6.27937&	-5	0.00590	4.96225& -3
182	10.0	0.00305	5.91058&	-5	0.00621	8.59685& -3
200	11.0	0.00305	5.93098&	-5	0.00272	1.15862& -3
219	12.0	0.00256	1.38419&	-3	0.00372	1.80985& -3
237	13.0	0.00304	5.34232&	-5	0.00365	2.54633& -3
255	14.0	0.00340	5.21605&	-5	0.00304	1.77400& -3
273	15.0	0.00305	5.24661&	-5	0.00490	4.77328& -3
292	16.0	0.00291	5.78288&	-4	-0.00232	3.09321& -2
310	17.0	0.00306	4.71553&	-5	0.00520	4.33959& -3
328	18.0	0.00307	4.99553&	-5	0.00407	2.25833& -3
346	19.0	0.00309	4.69280&	-5	0.00414	2.28350& -3
365	20.0	0.00310	4.38254&	-5	0.00390	3.03402& -3
383	21.0	0.00312	4.27282&	-5	0.00291	1.84993& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00297	1.83332&	-4	0.00284	3.11208& -3
197	2.0	0.00310	1.09764&	-4	0.00329	3.25485& -3
295	3.0	0.00303	8.66847&	-5	0.00474	2.48376& -3
394	4.0	0.00309	6.94008&	-5	0.00394	2.35100& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00297	1.29354&	-4	0.00314	2.46430& -3

Run Number 129

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time ConstantQuadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
18	1.0	0.03812	1.89106&	-2	-0.27699	5.92916&	-1
36	2.0	0.03088	5.82795&	-3	0.14247	3.49134&	-1
54	3.0	0.02868	3.43452&	-3	-0.03810	2.20632&	-1
73	4.0	0.02899	2.30774&	-3	0.02747	9.50742&	-2
91	5.0	0.02928	1.83458&	-3	-0.00932	4.39632&	-2
109	6.0	0.02941	1.56770&	-3	-0.03530	1.47282&	-1
127	7.0	0.02827	5.76716&	-3	-0.03492	1.53746&	-1
146	8.0	0.02952	1.40189&	-3	0.02784	3.00883&	-2
164	9.0	0.02960	1.42070&	-3	-0.05538	9.84550&	-2
182	10.0	0.02964	1.33780&	-3	-0.01239	1.05661&	-1
200	11.0	0.02961	1.42039&	-3	-0.01439	7.02932&	-2
219	12.0	0.02960	1.42792&	-3	0.01350	7.85364&	-2
237	13.0	0.02954	1.53087&	-3	-0.02018	8.16529&	-2
255	14.0	0.02957	1.48713&	-3	0.00268	1.11994&	-1
273	15.0	0.02961	1.62073&	-3	-0.00094	2.42300&	-2
292	16.0	0.02973	1.77426&	-3	-0.04080	7.40469&	-2
310	17.0	0.02985	1.82018&	-3	0.03195	8.97369&	-2
328	18.0	0.02987	1.88347&	-3	-0.00799	5.08707&	-2
346	19.0	0.03015	1.95364&	-3	-0.02921	9.65986&	-2
365	20.0	0.03031	1.94873&	-3	0.00305	4.86807&	-2
383	21.0	0.03047	1.97301&	-3	0.00617	2.48582&	-2

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
98	1.0	0.02647	4.43262&	-3	-0.11950	1.92335&	-1
197	2.0	0.02982	2.20709&	-3	0.03497	9.79914&	-2
295	3.0	0.02907	1.86073&	-3	0.10967	3.33483&	-1
394	4.0	0.02989	1.63608&	-3	0.01588	5.74637&	-2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>		
			STD. DEV.		MEAN	STD. DEV.	
257	1.0	0.02718	3.34777&	-3	0.00946	6.29264&	-2

Time Constant 2Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.00306	4.77454& -4	0.00528	3.48753& -2
36	2.0	0.00301	2.61090& -4	0.01521	2.77598& -2
54	3.0	0.00288	2.04687& -4	0.00233	1.47705& -2
73	4.0	0.00291	1.64633& -4	0.00564	8.76079& -3
91	5.0	0.00293	1.41981& -4	0.00165	2.80257& -3
109	6.0	0.00294	1.23873& -4	-0.00102	1.57760& -2
127	7.0	0.00287	3.96167& -4	-0.00025	1.15210& -2
146	8.0	0.00294	1.11657& -4	0.00478	4.07549& -3
164	9.0	0.00295	1.13100& -4	-0.00231	9.43294& -3
182	10.0	0.00295	1.05719& -4	0.00049	1.27576& -2
200	11.0	0.00295	1.15432& -4	0.00024	5.62931& -3
219	12.0	0.00295	1.16275& -4	0.00333	5.96562& -3
237	13.0	0.00294	1.24085& -4	-0.00085	8.54787& -3
255	14.0	0.00295	1.21633& -4	0.00166	1.00138& -2
273	15.0	0.00295	1.35160& -4	0.00072	1.88494& -3
292	16.0	0.00296	1.49083& -4	-0.00362	7.69559& -3
310	17.0	0.00297	1.51870& -4	0.00469	9.91077& -3
328	18.0	0.00296	1.58281& -4	0.00022	5.29032& -3
346	19.0	0.00299	1.63381& -4	-0.00238	1.11756& -2
365	20.0	0.00300	1.61253& -4	0.00131	4.96058& -3
383	21.0	0.00301	1.62024& -4	0.00163	2.36851& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.00280	2.26239& -4	-0.00011	8.59413& -3
197	2.0	0.00296	1.65229& -4	0.00531	7.68999& -3
295	3.0	0.00291	1.53497& -4	0.01184	3.27922& -2
394	4.0	0.00297	1.37053& -4	0.00243	3.82281& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00277	3.03913& -4	0.00217	3.22335& -3

Data Analysis ProgramRun Number = 130

Time Marker Pulse Setting = 1.0

Number of Channels = 2

Data Values per Channel = 400

Sets of Readings = 15

Time Constant 1Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.	MEAN	STD. DEV.	
18	1.0	0.06804	4.77695& -2	-0.16125	4.10084& -1	
36	2.0	0.04079	1.63795& -2	-0.22854	3.99349& -1	
54	3.0	0.03371	1.07402& -2	-0.09917	3.36356& -1	
73	4.0	0.03239	8.56366& -3	-0.05779	9.48175& -2	
91	5.0	0.03194	6.12296& -3	-0.00965	2.04417& -1	
109	6.0	0.03177	5.09934& -3	0.02245	1.32701& -1	
127	7.0	0.03153	4.35045& -3	-0.02589	9.60811& -2	
146	8.0	0.02960	7.45913& -3	-0.03692	6.06816& -2	
164	9.0	0.02980	6.97149& -3	-0.03598	7.32083& -2	
182	10.0	0.03107	3.23489& -3	-0.03393	1.70458& -1	
200	11.0	0.03096	2.94725& -3	0.00651	8.00294& -2	
219	12.0	0.03097	2.74491& -3	0.00135	1.64288& -1	
237	13.0	0.03084	2.63372& -3	-0.06773	1.60257& -1	
255	14.0	0.03085	2.47692& -3	-0.01159	3.51536& -2	
273	15.0	0.03099	2.42338& -3	-0.01735	3.53887& -2	
292	16.0	0.03100	2.26210& -3	-0.01195	1.59179& -1	
310	17.0	0.03108	2.21490& -3	0.00549	8.12312& -2	
328	18.0	0.03118	2.15389& -3	-0.00364	5.46745& -2	
346	19.0	0.02532	2.32879& -2	-0.03741	9.68501& -2	
365	20.0	0.03041	4.32421& -3	-0.01194	3.23584& -2	
383	21.0	0.03176	1.98607& -3	-0.00070	5.53455& -2	

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.	MEAN	STD. DEV.	
98	1.0	0.03360	1.31361& -2	-0.01847	1.74029& -1	
197	2.0	0.03324	5.98768& -3	-0.16656	7.31384& -1	
295	3.0	0.03196	5.32352& -3	0.00475	1.56487& -1	
394	4.0	0.03212	4.39578& -3	0.01008	4.36378& -2	

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.	MEAN	STD. DEV.	
257	1.0	0.03159	7.58451& -3	-0.00228	9.92039& -2	

Time Constant 2Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00404	1.24190&	-3	0.01434	2.39361& -2
36	2.0	0.00354	7.08320&	-4	-0.01302	4.75503& -2
54	3.0	0.00324	5.60698&	-4	-0.00634	4.46554& -2
73	4.0	0.00320	5.09341&	-4	0.00230	7.29276& -3
91	5.0	0.00318	4.10390&	-4	0.00606	2.53545& -2
109	6.0	0.00318	3.67552&	-4	0.00579	1.85106& -2
127	7.0	0.00317	3.32316&	-4	-0.00092	1.20766& -2
146	8.0	0.00298	6.93640&	-4	-0.00086	6.31732& -3
164	9.0	0.00303	5.39474&	-4	-0.00063	1.07353& -2
182	10.0	0.00313	2.71279&	-4	-0.00182	1.89727& -2
200	11.0	0.00313	2.52516&	-4	0.00359	1.02363& -2
219	12.0	0.00313	2.40718&	-4	0.00239	2.04138& -2
237	13.0	0.00311	2.33237&	-4	-0.00021	1.50169& -2
255	14.0	0.00311	2.23039&	-4	0.00146	2.97596& -3
273	15.0	0.00313	2.20648&	-4	-0.00013	3.31501& -3
292	16.0	0.00313	2.07711&	-4	0.00157	2.25843& -2
310	17.0	0.00314	2.04805&	-4	0.00268	1.09625& -2
328	18.0	0.00314	2.00440&	-4	0.00120	9.56211& -3
346	19.0	0.00276	1.54726&	-3	-0.00538	1.85381& -2
365	20.0	0.00302	5.99226&	-4	-0.00017	5.04086& -3
383	21.0	0.00319	1.88655&	-4	0.00215	8.35318& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00324	6.48595&	-4	0.00424	1.34387& -2
197	2.0	0.00326	4.10606&	-4	-0.01335	8.40958& -2
295	3.0	0.00317	3.62146&	-4	0.00554	2.12673& -2
394	4.0	0.00320	3.28668&	-4	0.00281	4.03096& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00315	4.82382&	-4	0.00326	7.16948& -3

Data Analysis Program

Run Number = 200

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	-0.02883	9.44889& -2	-0.17052	1.21462& -1
36	2.0	-0.00718	4.30435& -2	-0.02474	4.17360& -2
54	3.0	-0.00053	2.98881& -2	-0.00072	3.42762& -2
73	4.0	0.00167	2.27974& -2	0.00636	2.76745& -2
91	5.0	0.00046	1.87017& -2	-0.00116	1.97232& -2
109	6.0	0.00353	1.45650& -2	0.00143	1.41640& -2
127	7.0	0.00392	1.20050& -2	0.00466	1.28853& -2
146	8.0	0.00537	1.02361& -2	0.00461	1.05676& -2
164	9.0	0.00642	9.16550& -3	0.00768	1.17181& -2
182	10.0	0.00593	8.07457& -3	0.00636	8.56762& -3
200	11.0	0.00585	7.52257& -3	0.00443	7.04977& -3
219	12.0	0.00632	6.51499& -3	0.00595	6.61982& -3
237	13.0	0.00771	5.47654& -3	0.00767	5.62723& -3
255	14.0	0.00612	5.96156& -3	0.00582	6.20642& -3
273	15.0	0.00620	5.64182& -3	0.00638	6.15077& -3
292	16.0	0.00765	4.89703& -3	0.00857	5.52056& -3
310	17.0	0.00794	4.88608& -3	0.00890	5.97660& -3
328	18.0	0.00816	3.87053& -3	0.00780	3.85171& -3
346	19.0	0.00813	4.23841& -3	0.00775	4.02302& -3
365	20.0	0.00789	4.23282& -3	0.00781	4.19749& -3
383	21.0	0.00779	4.61288& -3	0.00801	4.73432& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	-0.00900	4.62626& -2	-0.03192	4.30648& -2
197	2.0	-0.00085	2.31972& -2	-0.00368	2.30364& -2
295	3.0	0.00335	1.49301& -2	0.00513	1.61603& -2
394	4.0	0.00523	1.03930& -2	0.00546	1.03889& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	-0.00312	3.29578& -2	-0.00847	3.19673& -2

Data Analysis ProgramRun Number = 201

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00712	5.83411&	-3	-0.32491	5.25713& -2
36	2.0	0.01039	4.55998&	-3	-0.13781	7.16059& -2
54	3.0	0.01148	1.19004&	-3	-0.03580	3.44384& -2
73	4.0	0.01041	2.66246&	-4	-0.01615	3.20251& -2
91	5.0	0.01004	6.24398&	-4	0.00728	1.59473& -2
109	6.0	0.00962	8.98988&	-4	0.01384	9.24645& -3
127	7.0	0.00959	6.82666&	-4	0.01195	1.31944& -2
146	8.0	0.01000	4.97427&	-4	0.01022	6.54975& -3
164	9.0	0.00990	3.54915&	-4	0.00695	9.39182& -3
182	10.0	0.00983	3.11480&	-4	0.00774	5.19591& -3
200	11.0	0.00888	3.69808&	-3	0.01462	7.97127& -3
219	12.0	0.00986	1.67231&	-4	0.00900	4.25206& -3
237	13.0	0.01004	1.42244&	-4	0.01025	4.58196& -3
255	14.0	0.01005	9.92854&	-5	0.00778	2.27901& -3
273	15.0	0.00930	3.02059&	-3	0.00879	5.11907& -3
292	16.0	0.01012	8.26370&	-5	0.00854	4.00528& -3
310	17.0	0.01012	5.09170&	-5	0.00947	2.28984& -3
328	18.0	0.01023	6.65951&	-5	0.01049	3.38705& -3
346	19.0	0.01027	6.02466&	-5	0.01106	2.44926& -3
365	20.0	0.01030	4.41536&	-5	0.01024	2.46546& -3
383	21.0	0.01033	3.18625&	-5	0.01214	2.57548& -3

Quadrature Size = 6

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00903	6.47593&	-4	-0.07845	4.56304& -2
197	2.0	0.00984	3.38908&	-4	-0.00239	2.32805& -2
295	3.0	0.00986	2.51994&	-4	-0.00016	7.53601& -3
394	4.0	0.00984	5.80950&	-5	0.00422	5.52018& -3

Quadrature Size = 9

SP	SI	MEAN	CHANNEL 1		CHANNEL 2	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00954	2.20480&	-4	-0.01126	3.00097& -2

Data Analysis Program

Run Number = 202

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.00937	5.43571& -3	-0.26338	4.94405& -2
36	2.0	0.00935	1.05903& -3	-0.16184	7.39642& -2
54	3.0	0.01103	4.97250& -4	-0.05650	6.20447& -2
73	4.0	0.01047	2.91494& -4	-0.00503	2.55937& -2
91	5.0	0.00931	3.02955& -3	-0.01464	2.69801& -2
109	6.0	0.00915	2.45545& -3	-0.00289	1.12541& -2
127	7.0	0.00917	2.11666& -3	0.00253	1.49964& -2
146	8.0	0.01005	1.27004& -4	0.00452	4.27532& -2
164	9.0	0.00996	8.57926& -5	-0.00441	2.63837& -2
182	10.0	0.00985	7.20961& -5	0.00001	2.13034& -2
200	11.0	0.00795	5.09410& -3	-0.00007	1.07565& -2
219	12.0	0.00985	6.90078& -5	0.01513	8.02305& -3
237	13.0	0.01004	5.54935& -5	0.01039	5.16080& -3
255	14.0	0.01008	4.42663& -5	0.01339	8.97251& -3
273	15.0	0.01009	4.41221& -5	0.01190	4.49164& -3
292	16.0	0.01008	5.76593& -5	0.00943	4.76097& -3
310	17.0	0.01001	5.44105& -5	0.01037	4.40457& -3
328	18.0	0.01024	4.35410& -5	0.00969	4.34476& -3
346	19.0	0.00959	2.58912& -3	0.00932	4.59262& -3
365	20.0	0.01029	3.28556& -5	0.01137	5.33948& -3
383	21.0	0.01006	9.73253& -4	0.00764	2.60129& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.00908	6.94808& -4	-0.09348	5.26602& -2
197	2.0	0.00969	1.65607& -4	-0.02965	4.14573& -2
295	3.0	0.00982	1.65607& -4	0.00223	1.73225& -2
394	4.0	0.00974	2.48393& -4	0.00394	6.10860& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00917	1.25639& -3	-0.03008	3.76380& -2

Data Analysis Program

Run Number = 203

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	0.03696	6.15663& -2	-0.22009	1.48346& -1
36	2.0	0.09486	2.79416& -1	-0.04699	9.04093& -2
54	3.0	0.02572	2.72947& -2	-0.00407	5.23898& -2
73	4.0	0.02075	1.95104& -2	0.00876	2.57064& -2
91	5.0	0.01802	1.53448& -2	0.00979	1.97390& -2
109	6.0	0.01598	1.21797& -2	0.00855	1.42881& -2
127	7.0	0.01439	1.10429& -2	0.01306	1.20658& -2
146	8.0	0.01486	9.56902& -3	0.01579	1.05949& -2
164	9.0	0.01358	8.93182& -3	0.01446	9.48128& -3
182	10.0	0.01153	7.02294& -3	0.01251	9.70911& -3
200	11.0	0.01153	7.02294& -3	0.01251	9.70911& -3
219	12.0	0.01145	7.97461& -3	0.01093	8.23089& -3
237	13.0	0.01228	5.21105& -3	0.01138	7.06039& -3
255	14.0	0.01048	8.02677& -3	0.01010	9.22644& -3
273	15.0	0.01268	5.14845& -3	0.01283	4.61837& -3
292	16.0	0.01005	5.72413& -3	0.01097	7.10224& -3
310	17.0	0.01170	5.63106& -3	0.01270	6.39005& -3
328	18.0	0.01191	3.43612& -3	0.01289	3.80082& -3
346	19.0	0.01182	3.30002& -3	0.01311	3.92245& -3
365	20.0	0.01225	3.92272& -3	0.01284	4.73054& -3
383	21.0	0.01220	3.71432& -3	0.01420	6.21316& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.02100	2.81974& -2	-0.05577	8.55147& -2
197	2.0	0.01676	1.44198& -2	0.01006	1.31356& -2
295	3.0	0.01445	9.85573& -3	0.01396	1.40044& -2
394	4.0	0.01365	7.25347& -3	0.01313	8.26655& -3

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.01377	1.23459& -2	-0.00648	2.95663& -2

Data Analysis Program

Run Number = 204

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	0.00002	8.20376&	-3	-0.25310	5.85474& -2
36	2.0	0.00738	1.85112&	-3	-0.11722	6.05277& -2
54	3.0	0.01031	7.44135&	-4	-0.03497	6.76941& -2
73	4.0	0.01011	3.85710&	-4	-0.01198	2.54082& -2
91	5.0	0.00989	2.88154&	-4	-0.00807	2.67865& -2
109	6.0	0.00967	2.05832&	-4	-0.00342	1.12356& -2
127	7.0	0.00854	2.85187&	-3	-0.00640	2.76649& -2
146	8.0	0.00994	1.11391&	-4	0.00125	2.66599& -2
164	9.0	0.00984	1.42190&	-4	0.00764	9.54150& -3
182	10.0	0.00942	1.57825&	-3	0.00299	6.35004& -3
200	11.0	0.00847	3.91929&	-3	0.00114	1.49583& -2
219	12.0	0.00984	1.25007&	-4	0.00865	8.17895& -3
237	13.0	0.01003	1.04046&	-4	0.00805	1.21054& -2
255	14.0	0.01000	5.36198&	-5	0.00966	1.03590& -2
273	15.0	0.01007	9.23956&	-5	0.00814	1.52748& -2
292	16.0	0.01003	6.73281&	-5	0.01214	4.96467& -3
310	17.0	0.01006	7.60351&	-5	0.01145	4.03489& -3
328	18.0	0.01021	6.14901&	-5	0.00862	3.63536& -3
346	19.0	0.01021	7.54666&	-5	0.00960	3.62627& -3
365	20.0	0.01024	6.91460&	-5	0.01317	6.26333& -3
383	21.0	0.01029	6.43349&	-5	0.01038	3.63835& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	0.00786	9.22190&	-4	-0.08156	8.35672& -2
197	2.0	0.00890	1.34529&	-3	-0.01431	2.25897& -2
295	3.0	0.00967	1.47900&	-4	0.01233	1.01504& -2
394	4.0	0.00919	1.38638&	-3	0.00398	6.27380& -3

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00900	9.58710&	-4	-0.03547	4.64812& -2

Data Analysis Program

Run Number = 205

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	-0.00017	7.44558& -3	-0.27415	5.82639& -2
36	2.0	0.00676	1.36850& -3	-0.10478	3.64960& -2
54	3.0	0.00963	9.24718& -4	-0.06355	3.43679& -2
73	4.0	0.00860	3.72129& -3	-0.03609	3.29617& -2
91	5.0	0.00944	3.80697& -4	-0.03659	3.78935& -2
109	6.0	0.00860	2.34858& -3	-0.01533	3.46001& -2
127	7.0	0.00932	5.82031 & -4	-0.00876	2.10359& -2
146	8.0	0.00954	9.47592& -5	-0.01771	2.50307& -2
164	9.0	0.00840	4.25704& -3	-0.01362	2.99954& -2
182	10.0	0.00915	1.52169& -3	-0.00535	2.36635& -2
200	11.0	0.00853	2.83925& -3	-0.00184	1.40779& -2
219	12.0	0.00963	1.41910& -4	0.00398	1.75375& -2
237	13.0	0.00908	3.31436& -3	0.00695	1.33253& -2
255	14.0	0.00917	1.64470& -3	0.00286	2.94945& -2
273	15.0	0.00992	5.70935& -4	0.00912	1.40725& -2
292	16.0	0.00883	2.93103& -3	0.00813	9.21729& -3
310	17.0	0.00889	2.89875& -3	0.01071	1.07798& -2
328	18.0	0.00973	1.08248& -3	0.00601	6.41949& -3
346	19.0	0.00936	2.56214& -3	0.01080	5.96818& -3
365	20.0	0.00946	2.46253& -3	0.01095	1.28261& -2
383	21.0	0.01009	1.08465& -4	0.00750	1.61519& -2

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	0.00649	2.74513& -3	-0.12275	4.97681& -2
197	2.0	0.00692	4.90599& -3	-0.04212	3.07196& -2
295	3.0	0.00917	9.36355& -4	-0.00645	2.57725& -2
394	4.0	0.00829	2.51183& -3	-0.00392	1.81198& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00915	1.70235& -3	-0.05073	3.12406& -2

Data Analysis ProgramRun Number = 206

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	-0.04485	1.21849& -2	-0.24569	6.16763& -2
36	2.0	-0.00510	3.46061& -3	-0.12848	5.39237& -2
54	3.0	0.00328	1.83439& -3	-0.07023	5.12496& -2
73	4.0	0.00555	1.08821& -3	-0.04133	5.62495& -2
91	5.0	0.00519	4.31904& -3	-0.00557	6.59157& -2
109	6.0	0.00716	4.68591& -4	0.00537	1.72071& -2
127	7.0	0.00621	5.26932& -3	-0.00397	2.40459& -2
146	8.0	0.00712	3.74902& -3	0.00545	6.38851& -2
164	9.0	0.00882	3.96374& -4	-0.00462	2.70451& -2
182	10.0	0.00863	4.02428& -4	-0.00586	3.07801& -2
200	11.0	0.00655	4.66747& -3	-0.00354	1.54807& -2
219	12.0	0.00843	1.23768& -3	0.00655	1.14150& -2
237	13.0	0.00908	3.01279& -4	0.00382	1.12564& -2
255	14.0	0.00803	2.84028& -3	0.01057	8.46290& -3
273	15.0	0.00820	2.75199& -3	0.00503	1.39041& -2
292	16.0	0.00925	3.22066& -4	0.00805	6.35746& -3
310	17.0	0.00861	2.67234& -3	0.00995	7.53388& -3
328	18.0	0.00940	2.62181& -4	0.00992	1.23089& -2
346	19.0	0.00877	2.63087& -3	0.00903	8.40962& -3
365	20.0	0.00869	2.57334& -3	0.00946	7.49693& -3
383	21.0	0.00958	2.57973& -4	0.00596	4.52788& -3

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	-0.00386	6.30177& -3	-0.12246	5.71765& -2
197	2.0	0.00480	3.59818& -3	-0.02728	4.19009& -2
295	3.0	0.00740	1.39061& -3	-0.00236	1.48662& -2
394	4.0	0.00835	4.12048& -4	0.00123	1.22440& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00455	2.00250& -3	-0.04367	3.91418& -2

Data Analysis ProgramRun Number = 207

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
18	1.0	-0.04186	1.61825& -2	-0.23117	7.31180& -2
36	2.0	-0.00302	8.67285& -3	-0.13058	4.23662& -2
54	3.0	0.00235	7.79970& -3	-0.08539	5.37965& -2
73	4.0	0.00474	5.46105& -3	-0.06050	2.01861& -2
91	5.0	0.00634	4.43385& -3	-0.05673	2.35655& -2
109	6.0	0.00703	9.84261& -4	-0.03910	3.15307& -2
127	7.0	0.00789	1.07653& -3	-0.03606	1.89159& -2
146	8.0	0.00831	9.38401& -4	-0.01643	1.33781& -2
164	9.0	0.00827	5.62599& -4	-0.02267	2.60256& -2
182	10.0	0.00690	3.34569& -3	-0.02352	2.54485& -2
200	11.0	0.00852	4.75658& -4	-0.01750	1.48045& -2
219	12.0	0.00871	3.91356& -4	0.00266	2.32019& -2
237	13.0	0.00894	3.14261& -4	-0.00202	1.37383& -2
255	14.0	0.00912	1.88710& -4	-0.02340	7.14833& -2
273	15.0	0.00827	2.85452& -3	-0.01616	3.82659& -2
292	16.0	0.00917	2.70471& -4	-0.01092	2.19361& -2
310	17.0	0.00891	1.13062& -3	0.00147	1.22053& -2
328	18.0	0.00869	2.47064& -3	-0.00724	1.56046& -2
346	19.0	0.00961	2.43716& -4	0.00067	1.76661& -2
365	20.0	0.00953	2.20101& -4	0.00065	2.23131& -2
383	21.0	0.00893	2.37500& -3	-0.00333	1.35821& -2

Quadrature Size = 6

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
98	1.0	-0.00036	8.73649& -3	-0.14019	3.49813& -2
197	2.0	0.00632	1.21413& -3	-0.06421	3.08205& -2
295	3.0	0.00737	1.50951& -3	-0.03454	2.34073& -2
394	4.0	0.00802	1.33071& -3	-0.02825	1.90315& -2

Quadrature Size = 9

SP	SI	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
		MEAN	STD. DEV.	MEAN	STD. DEV.
257	1.0	0.00471	3.62891& -3	-0.08224	3.94941& -2

Data Analysis Program

Run Number = 208

Time Marker Pulse Setting = 1.0

Number of Channels = 3

Data Values per Channel = 400

Sets of Readings = 15

Quadrature Size = 3

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
18	1.0	-0.05347	4.77984&	-2	-0.29039	3.40677& -2
36	2.0	-0.01107	2.83374&	-2	-0.14470	3.16220& -2
54	3.0	0.00030	1.68310&	-2	-0.09622	2.30451& -2
73	4.0	0.00195	1.30639&	-2	-0.06480	2.04049& -2
91	5.0	0.00396	9.86765&	-3	-0.04985	2.55363& -2
109	6.0	0.00573	7.66803&	-3	-0.03558	1.62184& -2
127	7.0	0.00489	7.55793&	-3	-0.02189	2.04587& -2
146	8.0	0.00588	9.55330&	-3	-0.02582	2.54863& -2
164	9.0	0.00722	4.84371&	-3	-0.02008	1.01132& -2
182	10.0	0.00721	4.39427&	-3	-0.02005	1.85187& -2
200	11.0	0.00806	3.98413&	-3	-0.02081	2.03846& -2
219	12.0	0.00723	6.64458&	-3	-0.02300	2.18909& -2
237	13.0	0.00839	3.06714&	-3	-0.01690	1.43328& -2
255	14.0	0.00803	2.97850&	-3	-0.01203	1.10578& -2
273	15.0	0.00775	3.68835&	-3	-0.00519	1.02404& -2
292	16.0	0.00877	2.50880&	-3	-0.00790	1.25284& -2
310	17.0	0.00884	2.28549&	-3	-0.00431	1.59643& -2
328	18.0	0.00781	3.94460&	-3	-0.01600	1.76070& -2
346	19.0	0.00879	2.32009&	-3	-0.00692	1.91003& -2
365	20.0	0.00924	1.98212&	-3	-0.00872	1.78282& -2
383	21.0	0.00875	2.16754&	-3	-0.00322	2.40149& -3

Quadrature Size = 6

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
98	1.0	-0.00786	2.55866&	-2	-0.14650	4.48173& -2
197	2.0	0.00344	1.23076&	-2	-0.06875	2.17948& -2
295	3.0	0.00567	7.81808&	-3	-0.03599	2.42548& -2
394	4.0	0.00540	8.14642&	-3	-0.02272	1.65932& -2

Quadrature Size = 9

SP	SI	MEAN	<u>CHANNEL 1</u>		<u>CHANNEL 2</u>	
			STD. DEV.		MEAN	STD. DEV.
257	1.0	0.00107	1.49313&	-2	-0.08665	3.87649& -2

Appendix IV

Graphs 1 - 21 are the standard deviation graphs, whilst graphs 22 - 33 show the behaviour of the means of the parameter estimates.

For graphs 1 - 21 the following list is for curve identification:

<hr/>	Sample Size = 3
<hr/>	Sample Size = 6
<hr/>	Sample Size = 9

For graphs 22 - 33:

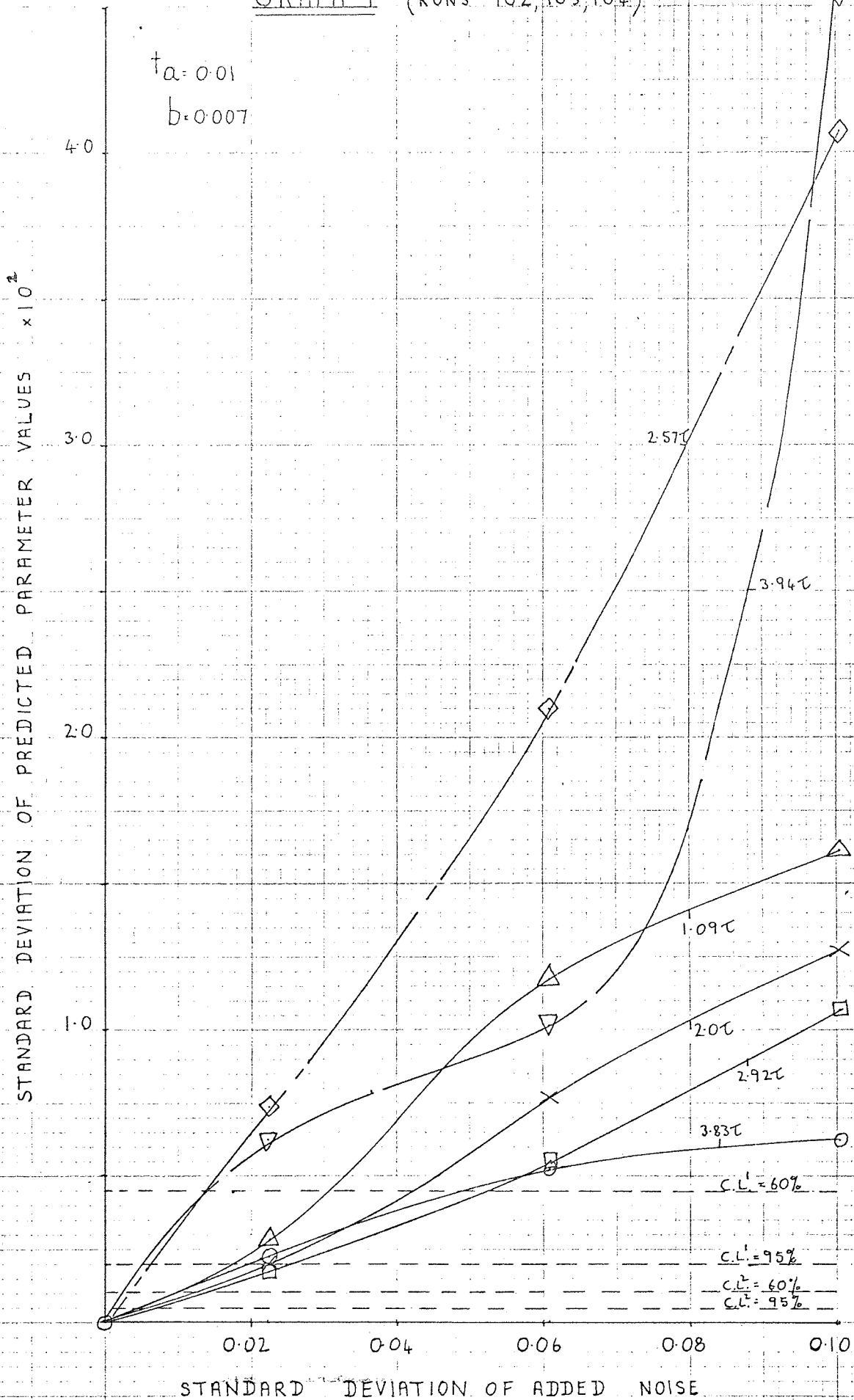
- ⊙ Noise free results
 - ⊠ Results with added noise level of standard deviation 0.022
-

Notes

- † This shows the parameter *displayed in the graph.*
 (Note: Both parameters were estimated simultaneously.)
- a : Model parameter
 - b : Step input amplitude
 - c : Forcing function final amplitude where the form of the forcing function is unknown

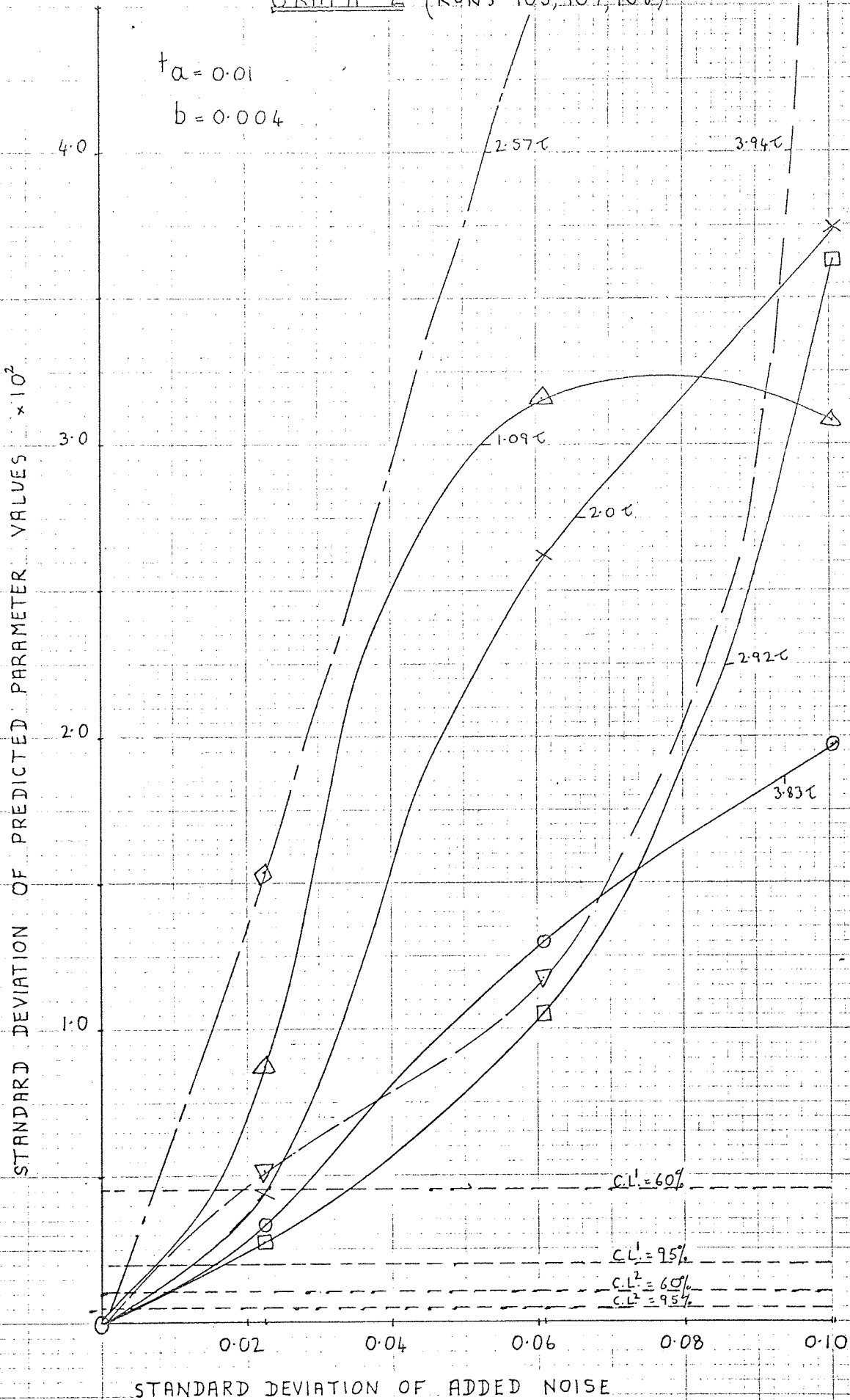
GRAPH 1 (RUNS 102, 103, 104)

$t_a = 0.01$
 $b = 0.0007$



GRAPH 2 (RUNS 105, 107, 108)

$t_a = 0.01$
 $b = 0.004$



GRAPH 3 (RUNS 109, 110, 111)

$\dagger a = 0.01$
 $b = 0.001$

STANDARD DEVIATION OF PREDICTED PARAMETER VALUES $\times 10^2$

4.0

3.0

2.0

1.0

2.92t
2.0t

3.94t

3.83t

C.L.¹ = 60%

C.L.¹ = 95%

C.L.² = 60%

C.L.² = 95%

0.02

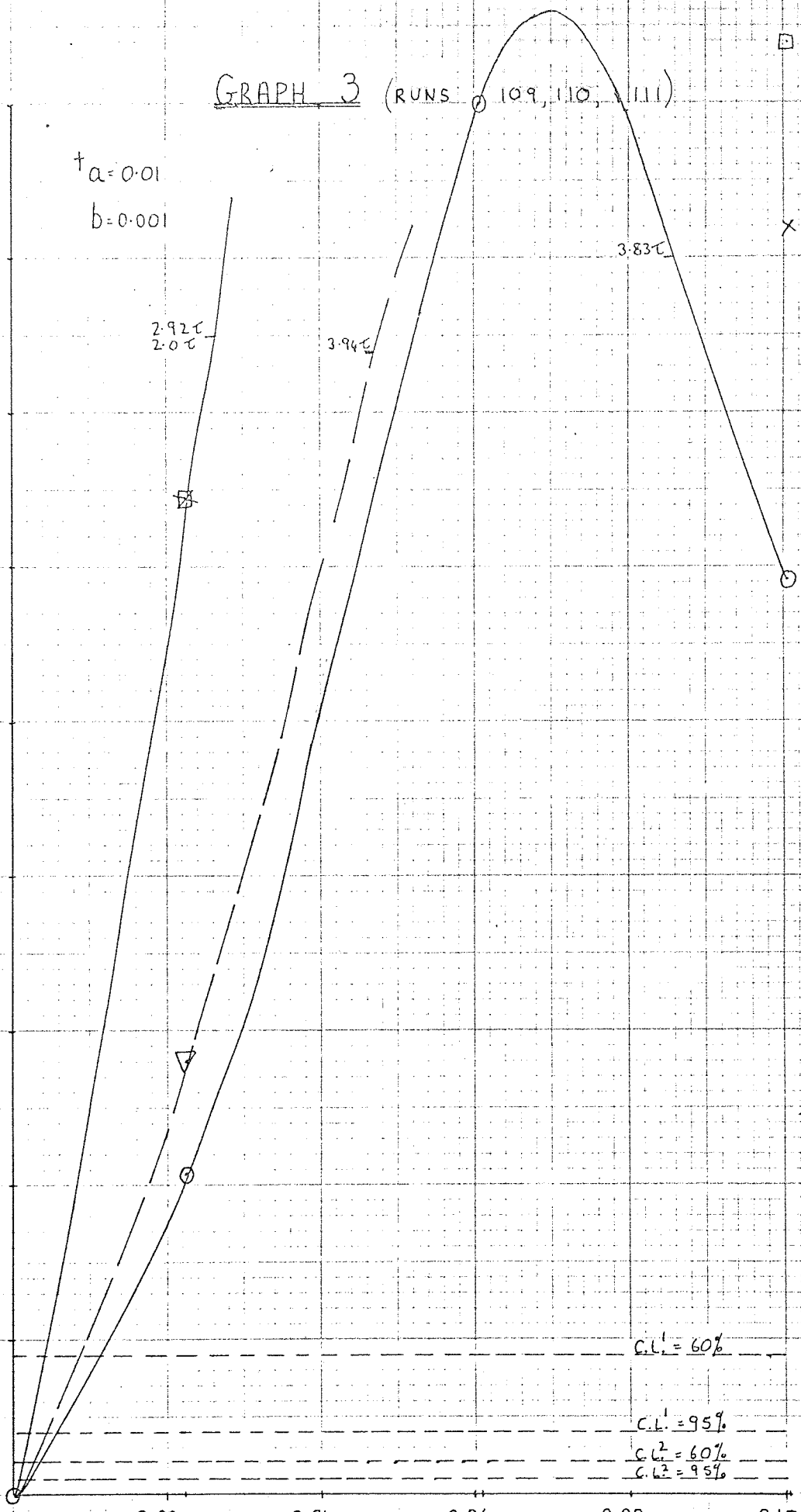
0.04

0.06

0.08

0.10

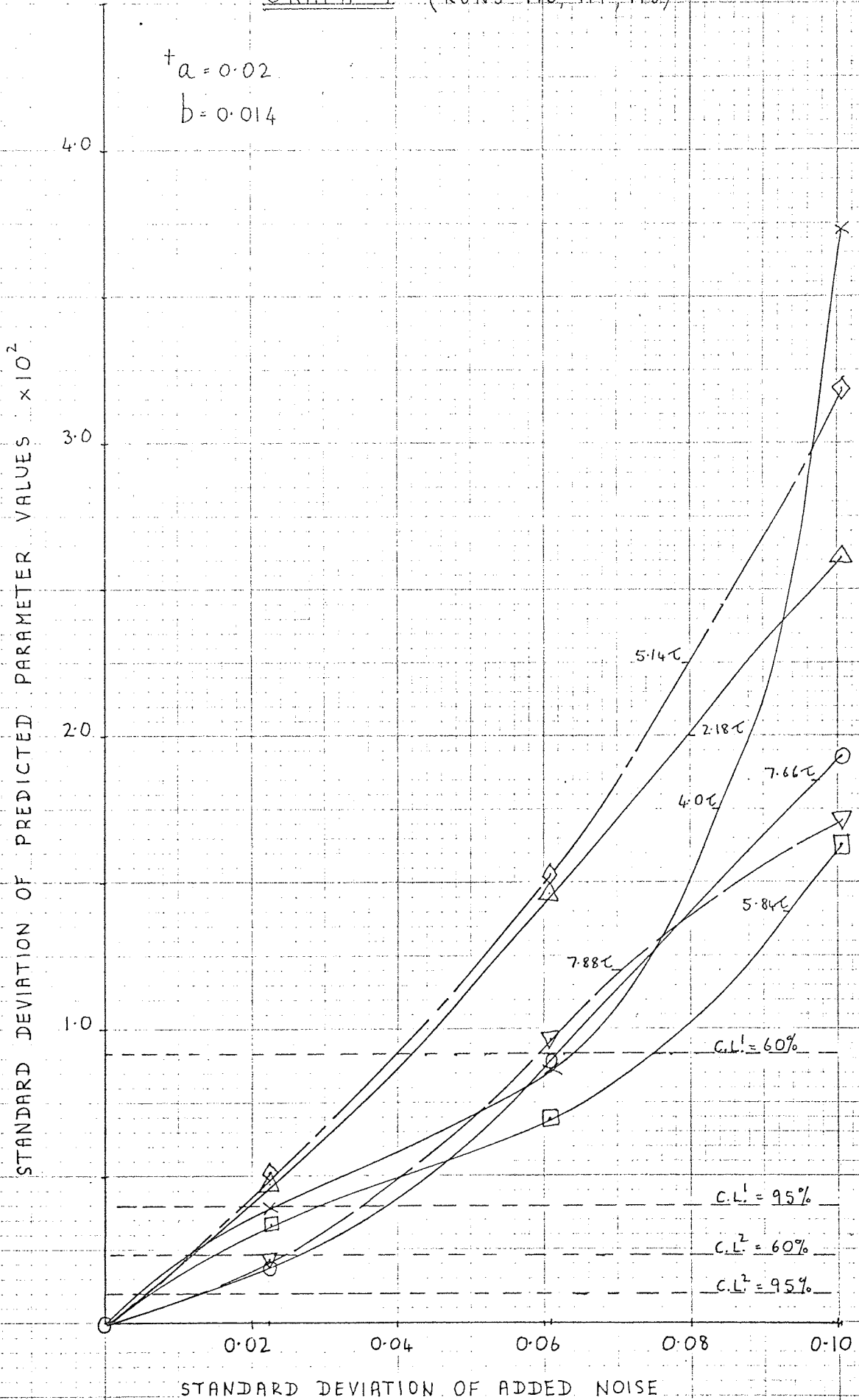
STANDARD DEVIATION OF ADDED NOISE



GRAPH 4 (RUNS 113, 114, 115)

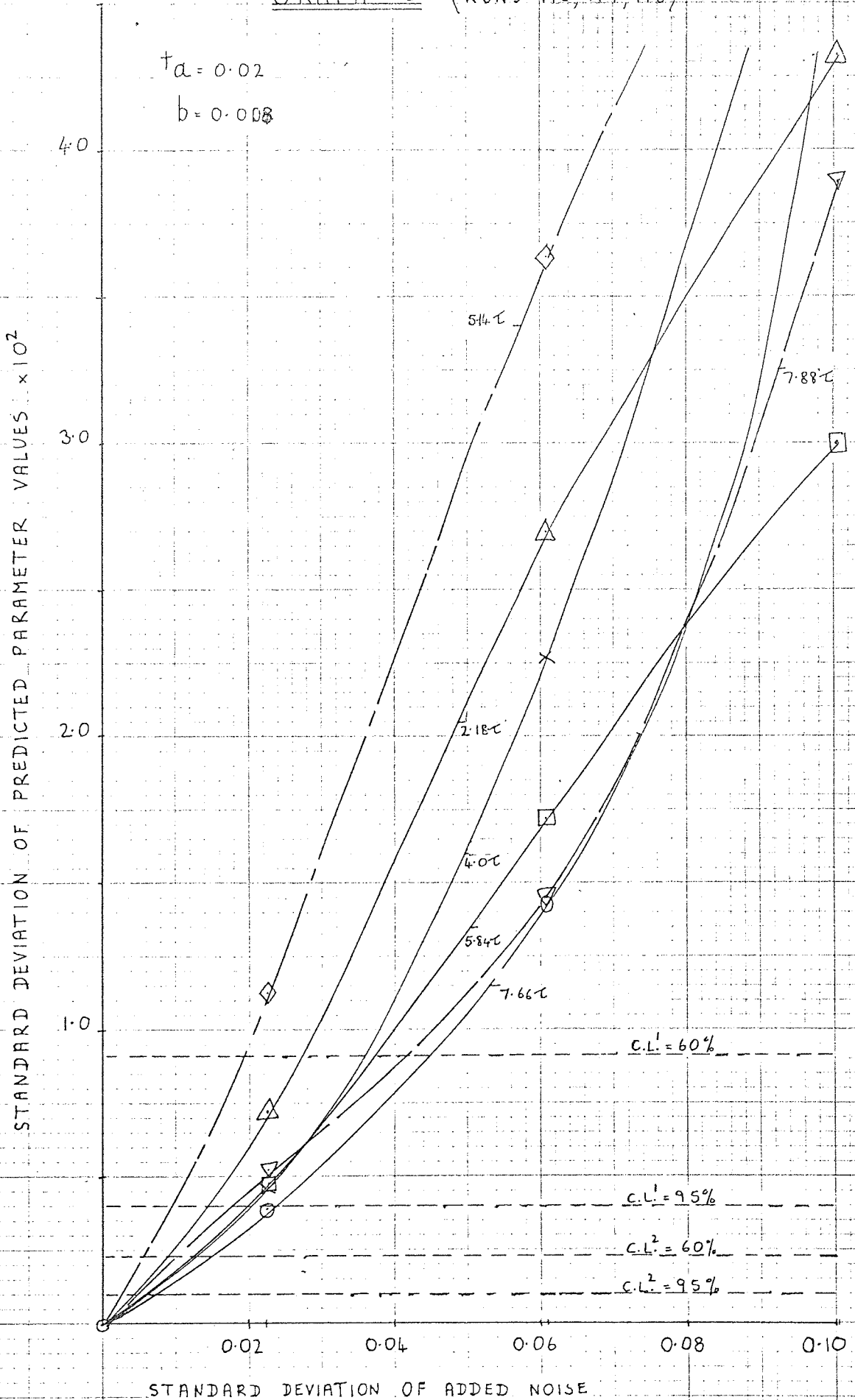
$a = 0.02$

$b = 0.014$

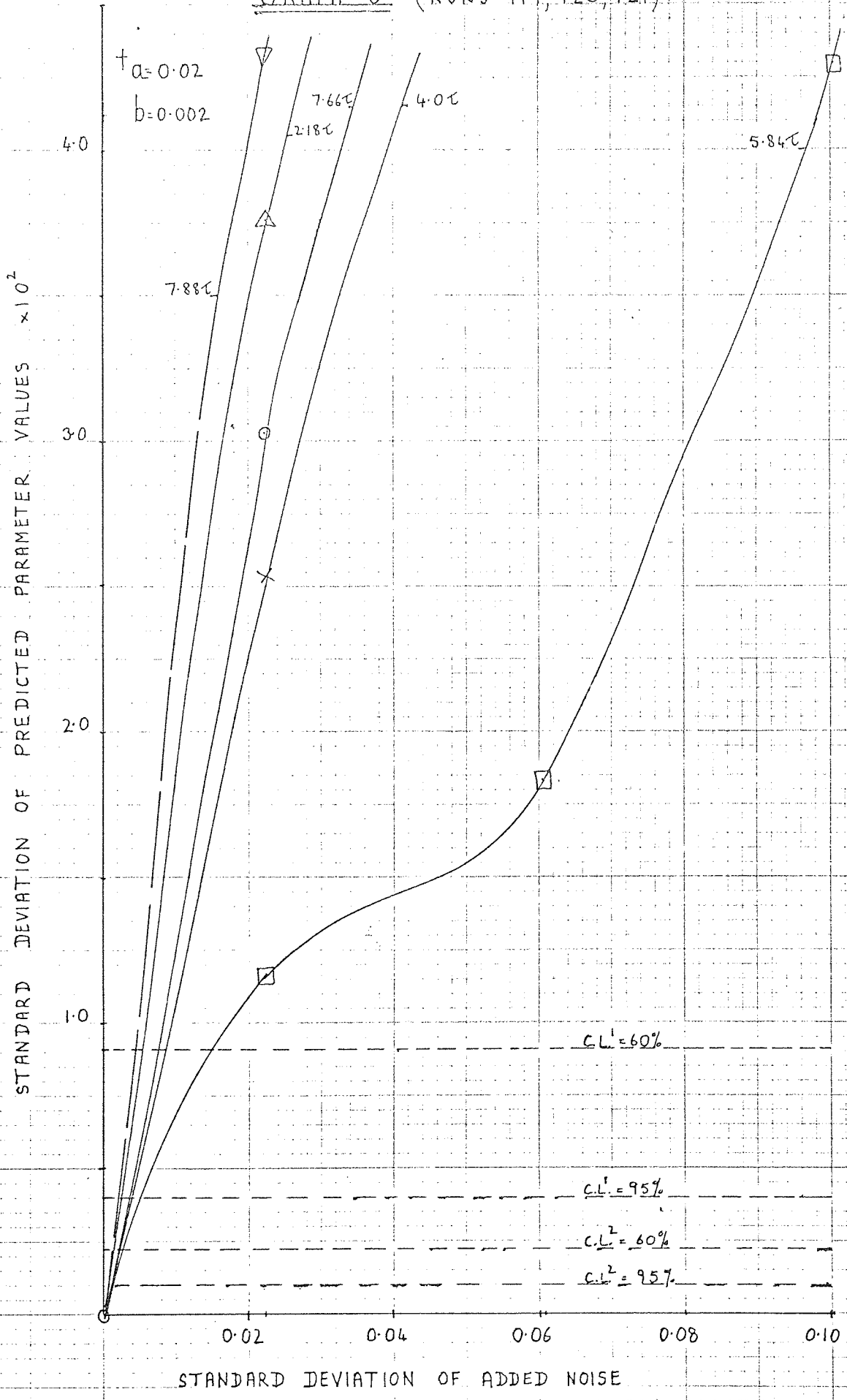


GRAPH 5 (RUNS 116, 117, 118)

$t_a = 0.02$
 $b = 0.008$

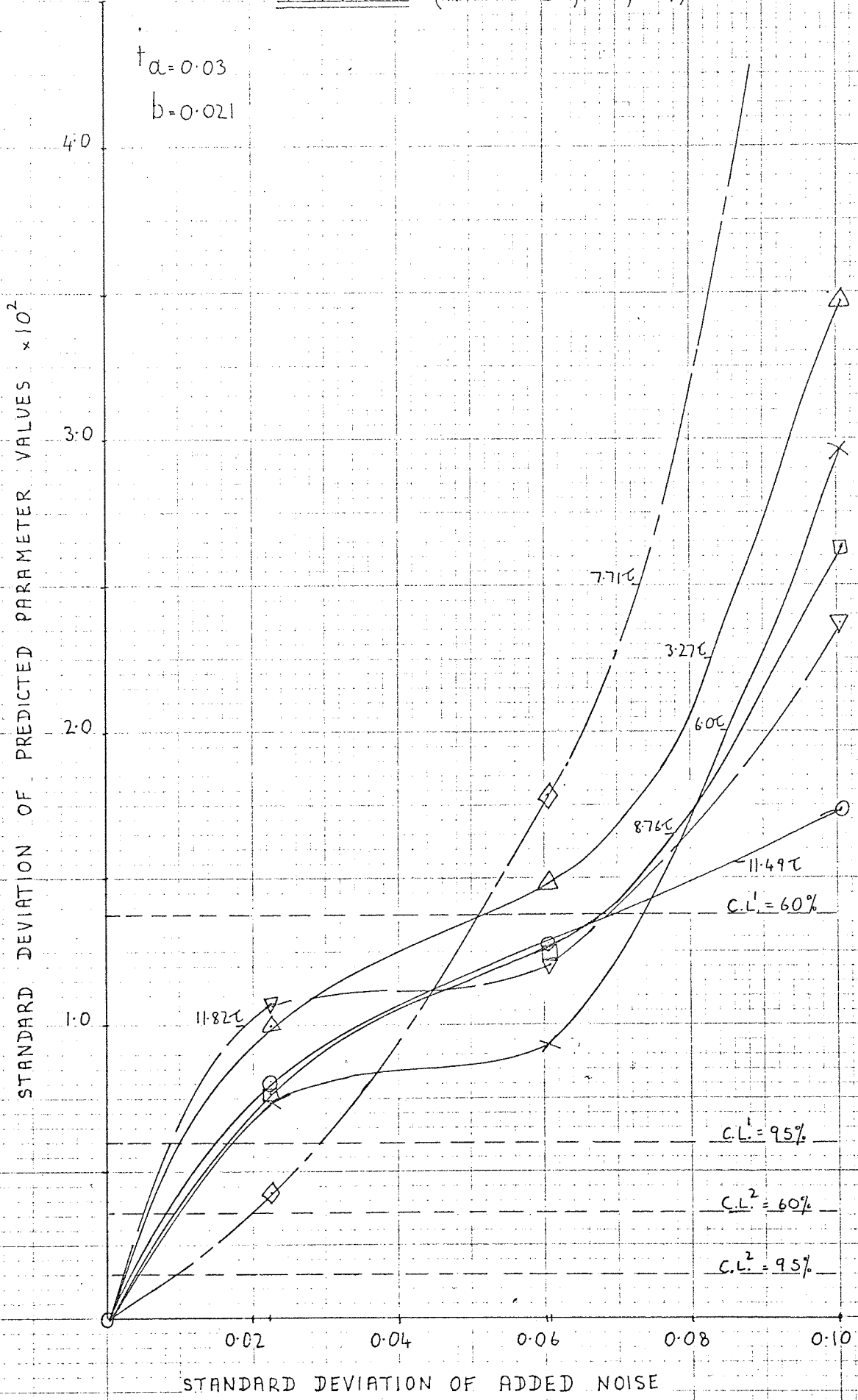


GRAPH 6 (RUNS 119, 120, 121)



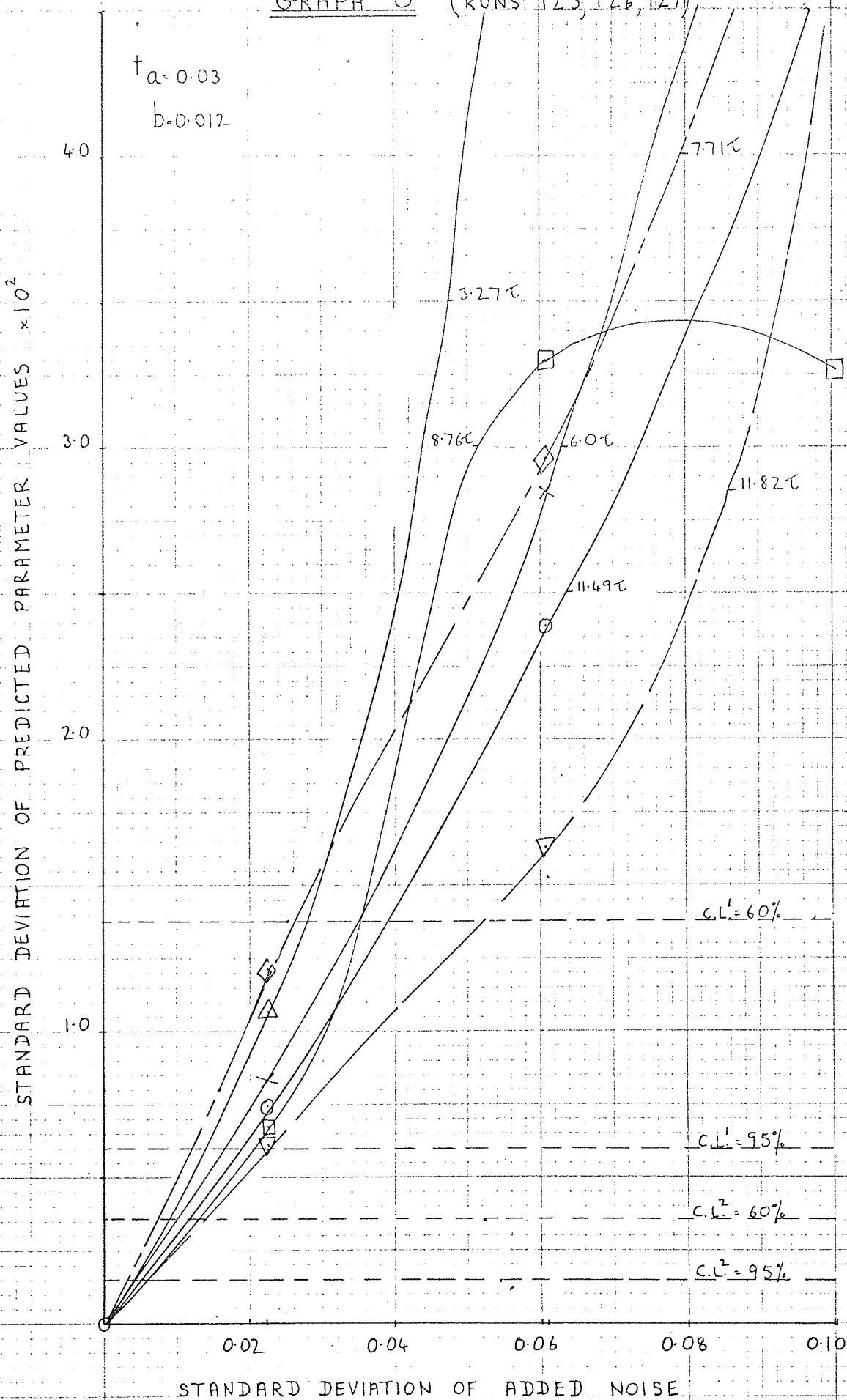
GRAPH 7 (RUNS 122, 123, 124)

$t_a = 0.03$
 $b = 0.021$



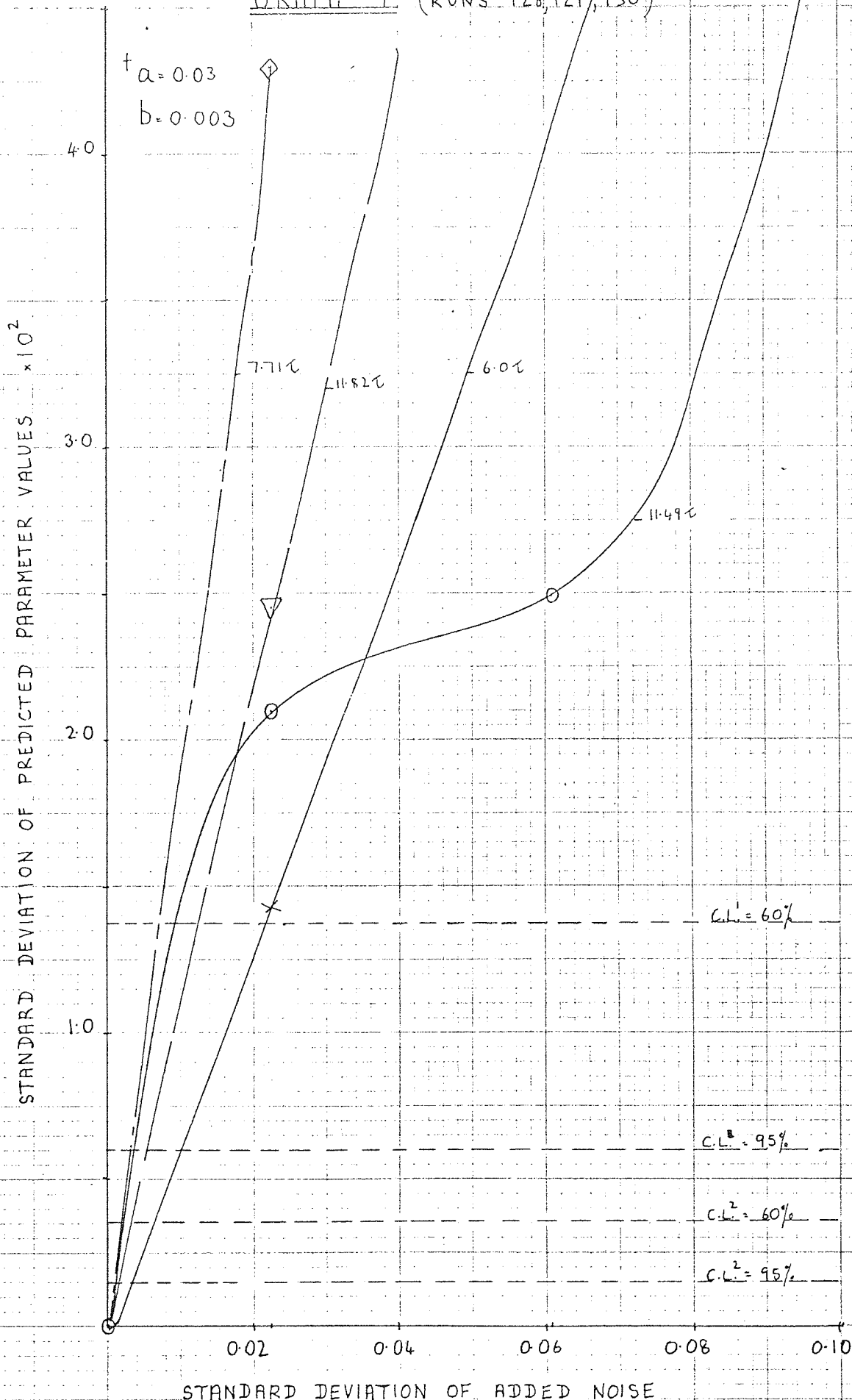
GRAPH 8 (RUNS 125, 126, 127)

$t_a = 0.03$
 $b = 0.012$



GRAPH 9 (RUNS 128, 129, 130)

t
 $a = 0.03$
 $b = 0.003$



STANDARD DEVIATION OF ADDED NOISE

C.L. = 60%

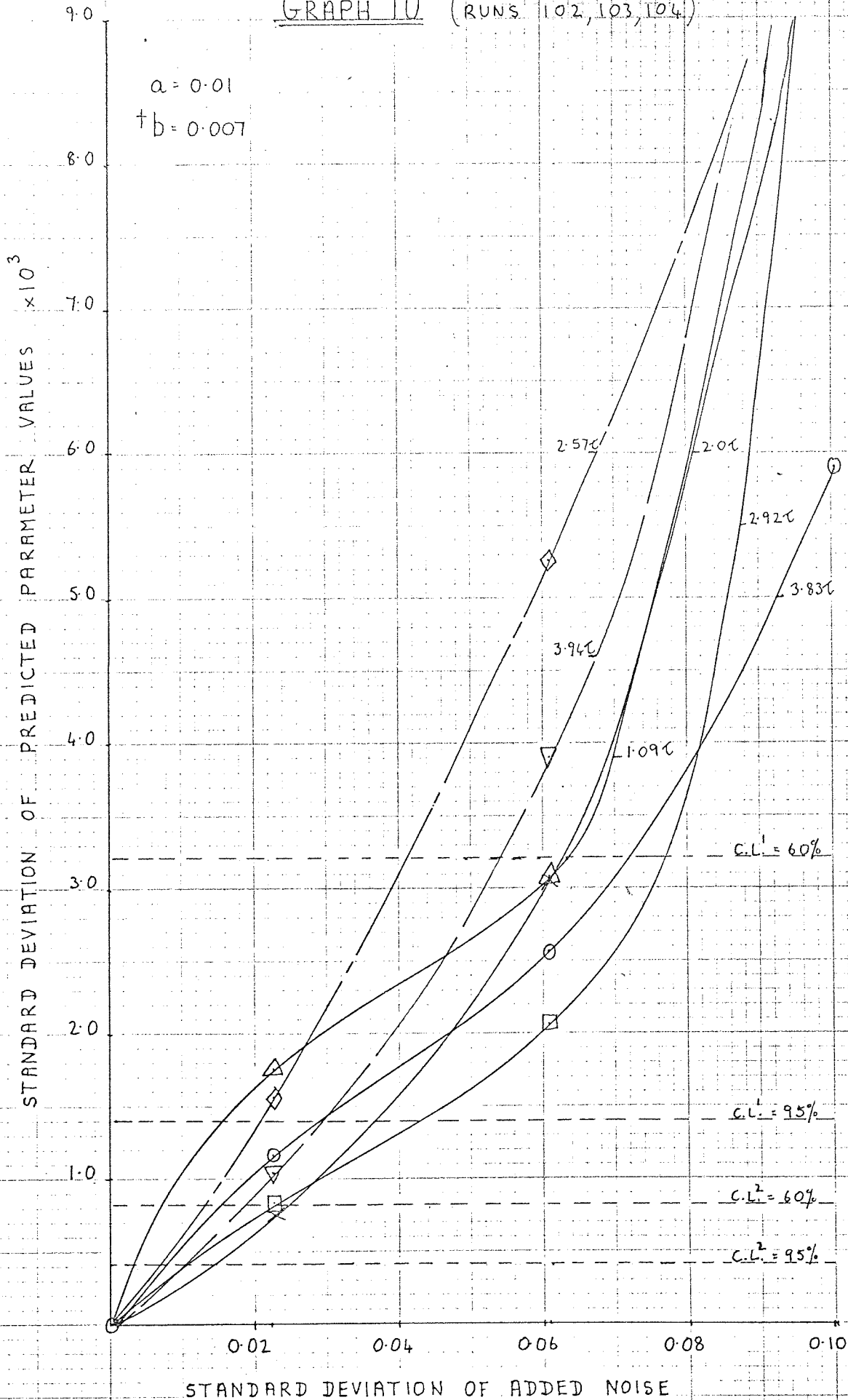
C.L. = 95%

C.L. = 60%

C.L. = 95%

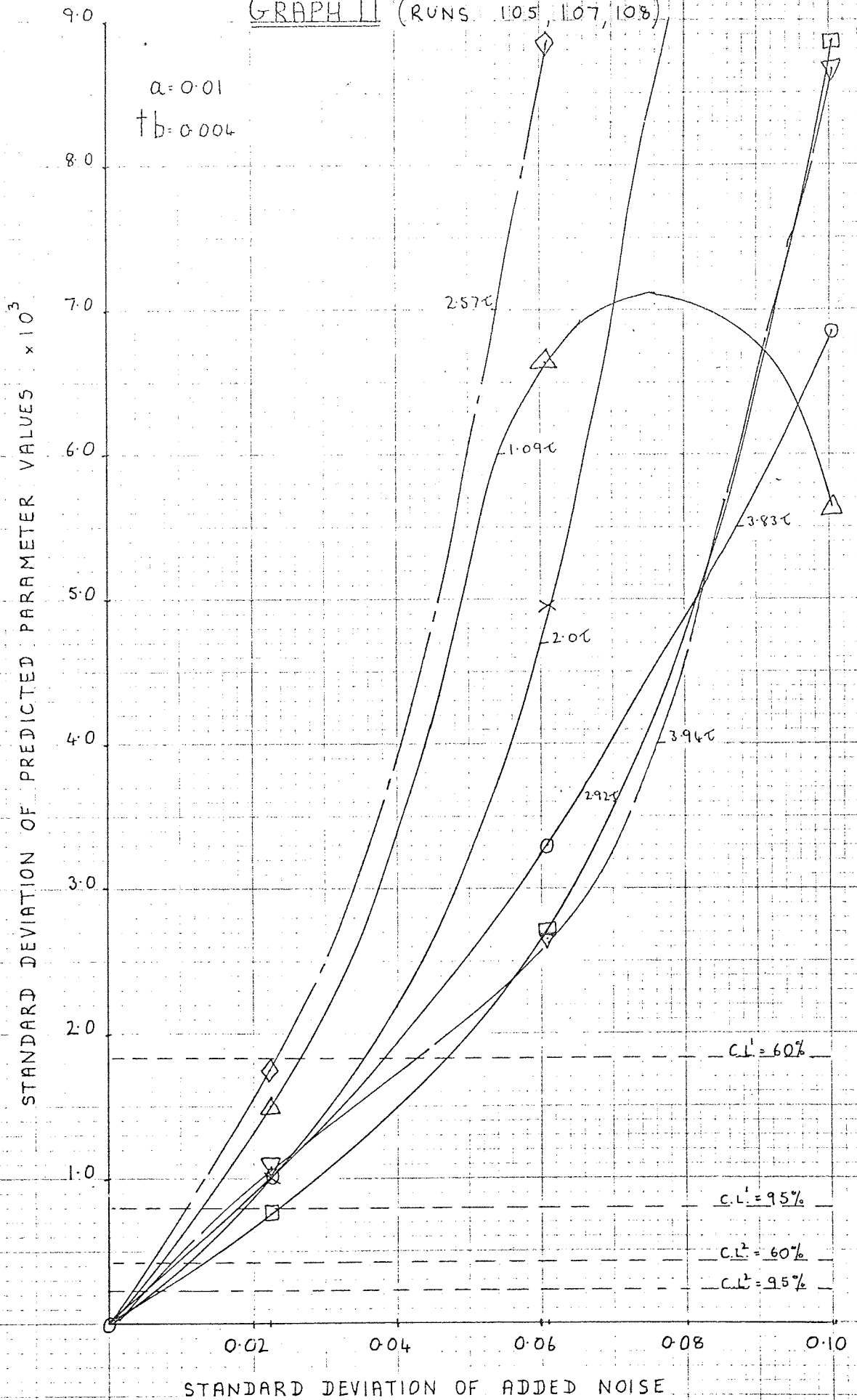
GRAPH 10 (RUNS 102, 103, 104)

$a = 0.01$
 $\dagger b = 0.007$

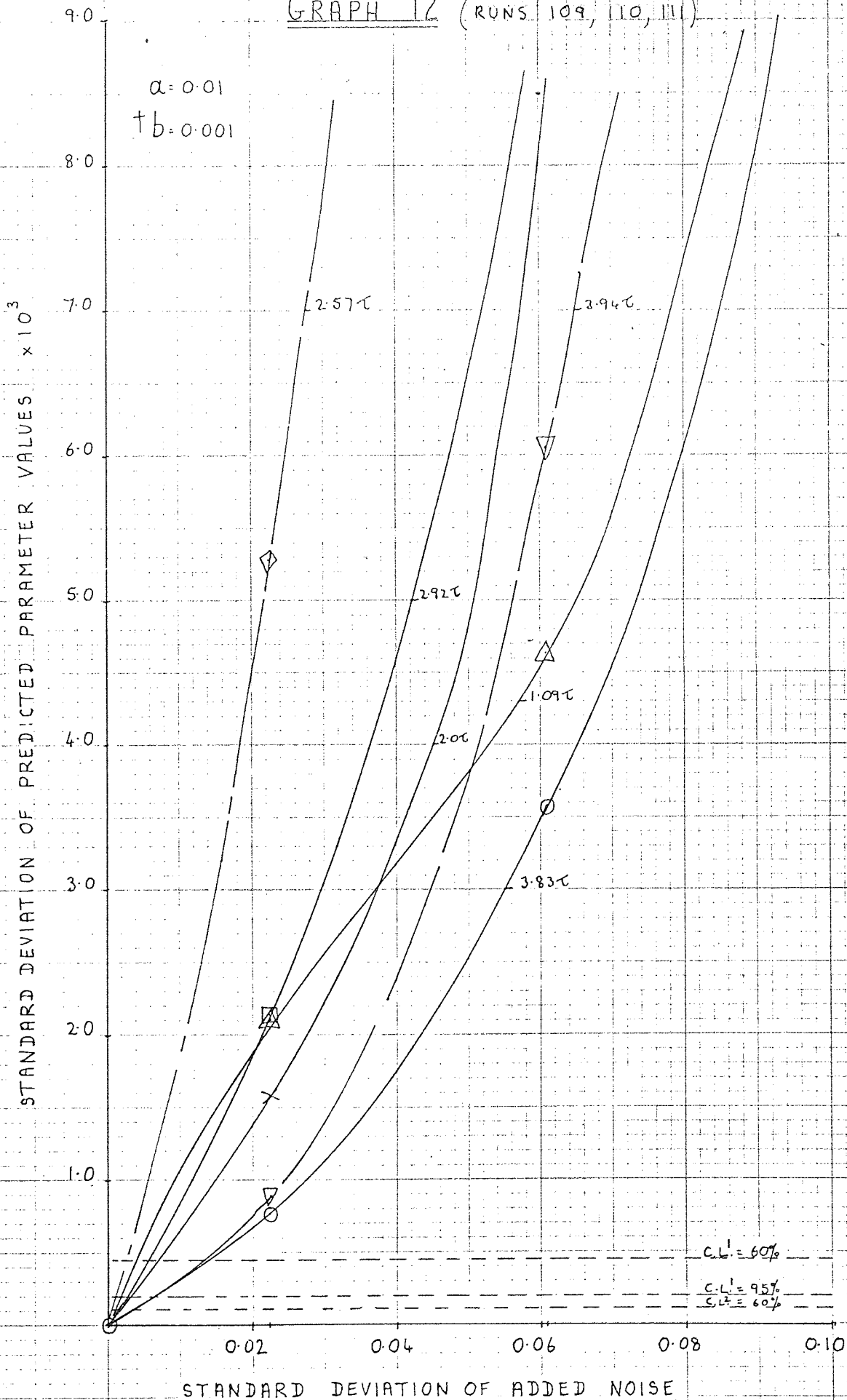


GRAPH II (RUNS 105, 107, 108)

$\alpha = 0.01$
 $t_b = 0.004$

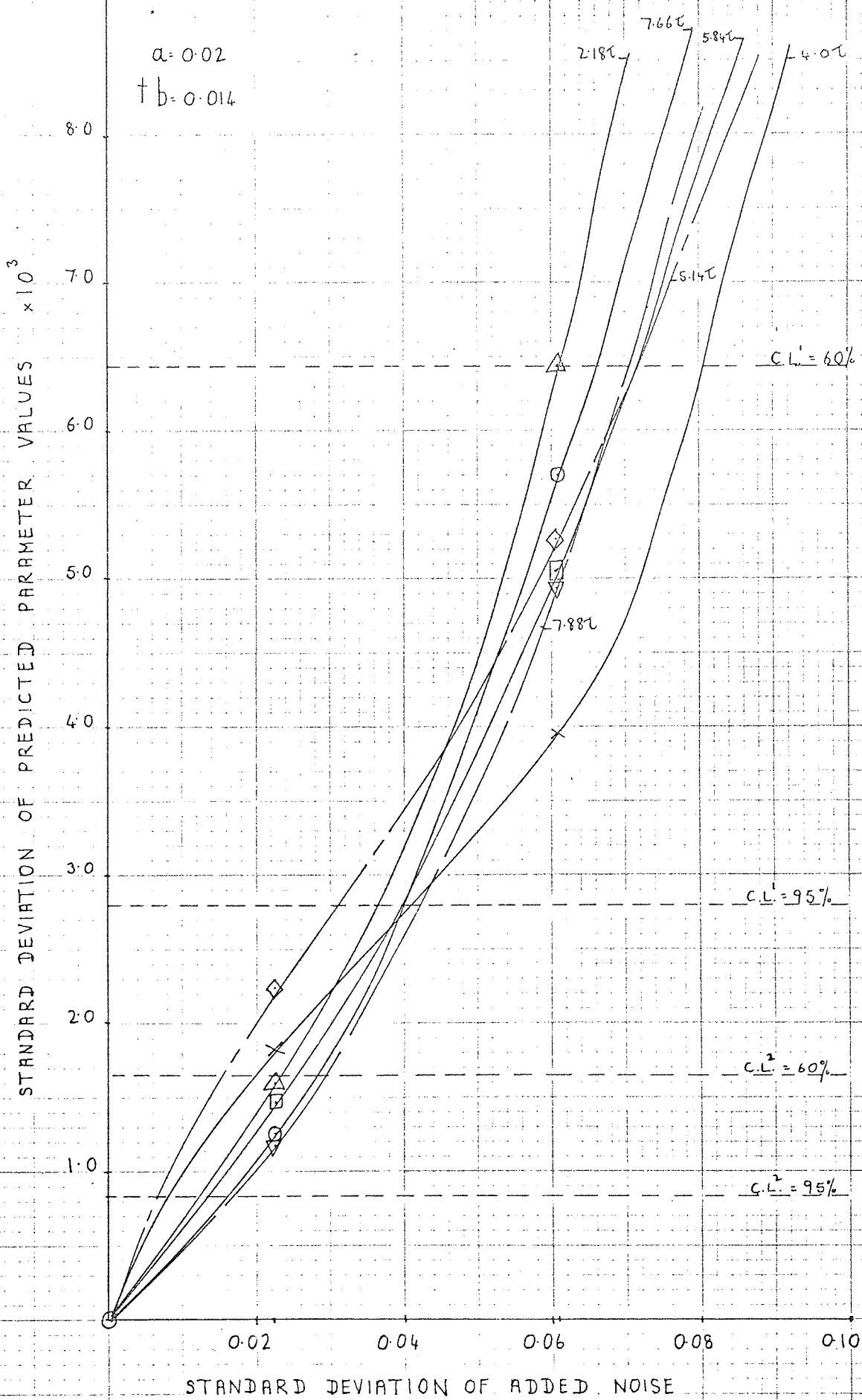


GRAPH 12 (RUNS 109, 110, 111)



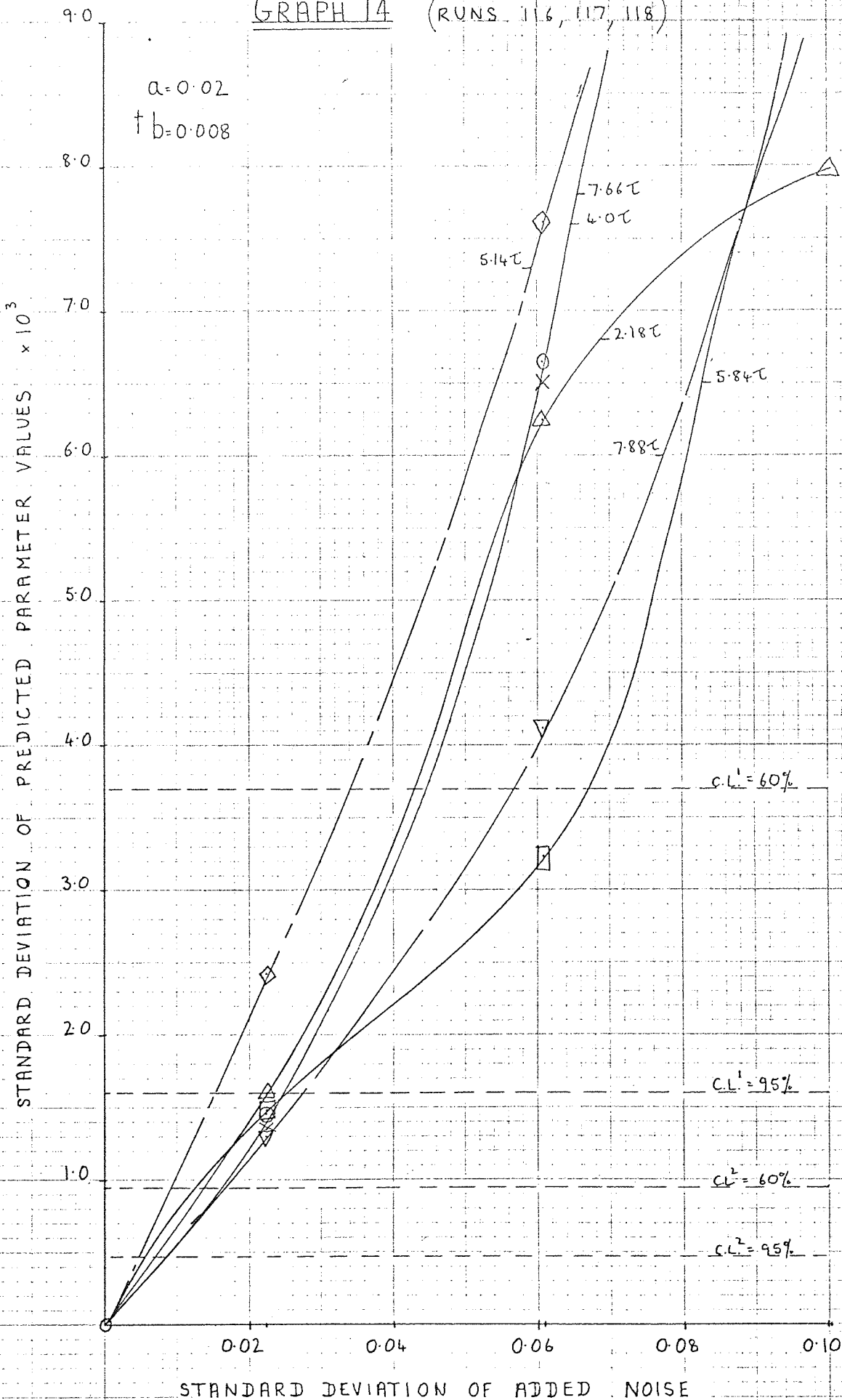
GRAPH 13 (RUNS 113, 114, 115)

$\alpha = 0.02$
 $\dagger b = 0.014$



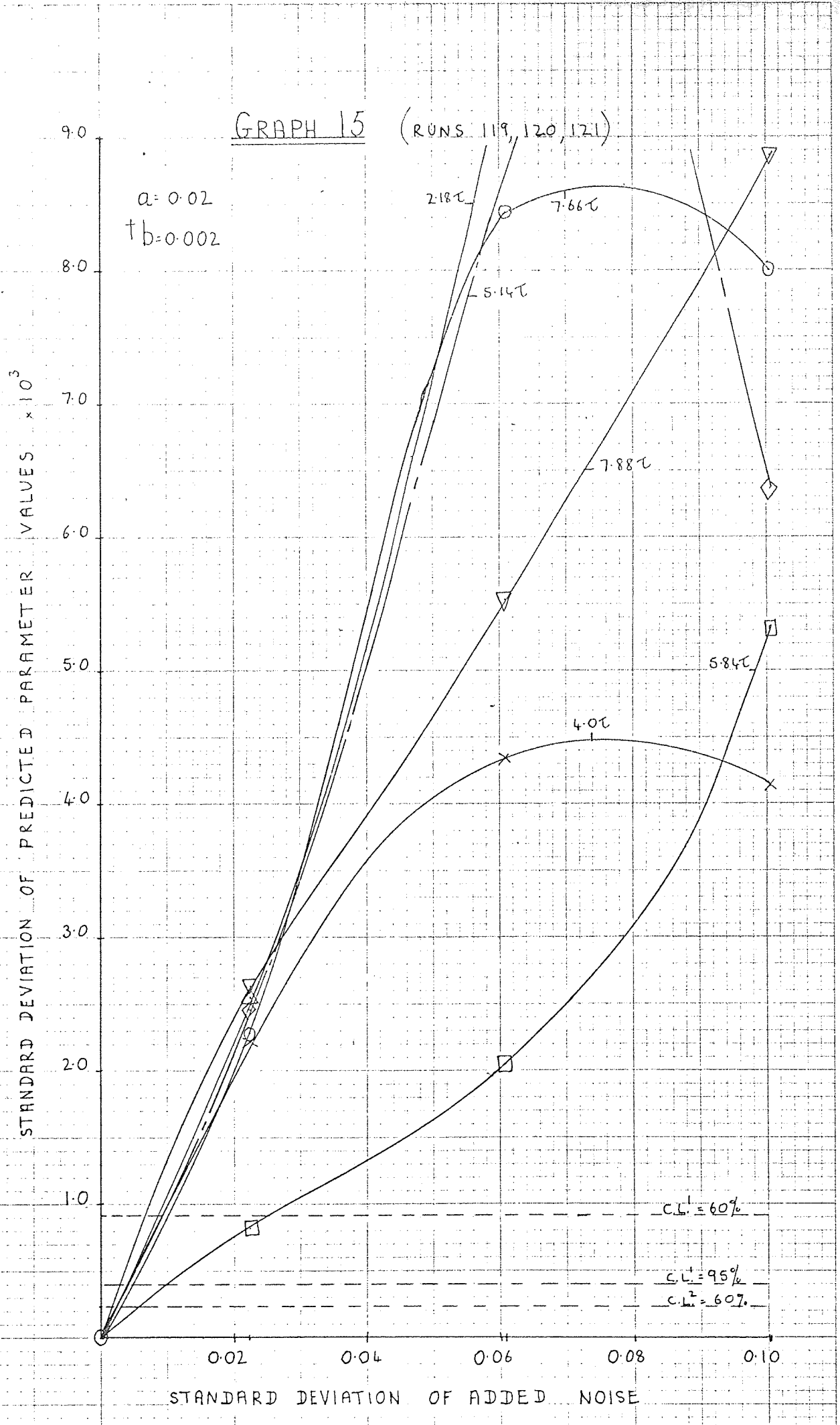
GRAPH 14 (RUNS 116, 117, 118)

$a=0.02$
 $\dagger b=0.008$



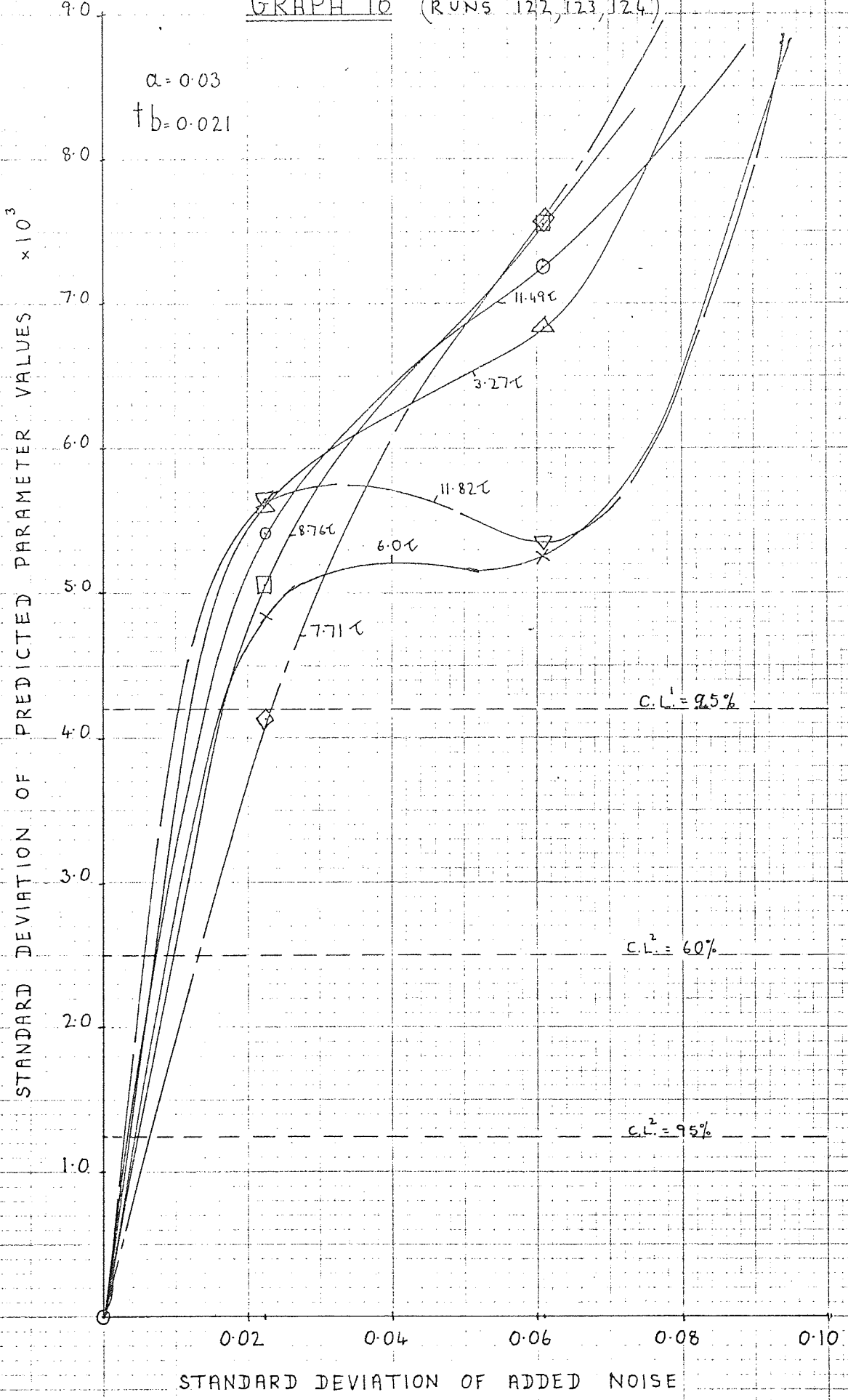
GRAPH 15 (RUNS 119, 120, 121)

$a = 0.02$
 $t_b = 0.002$



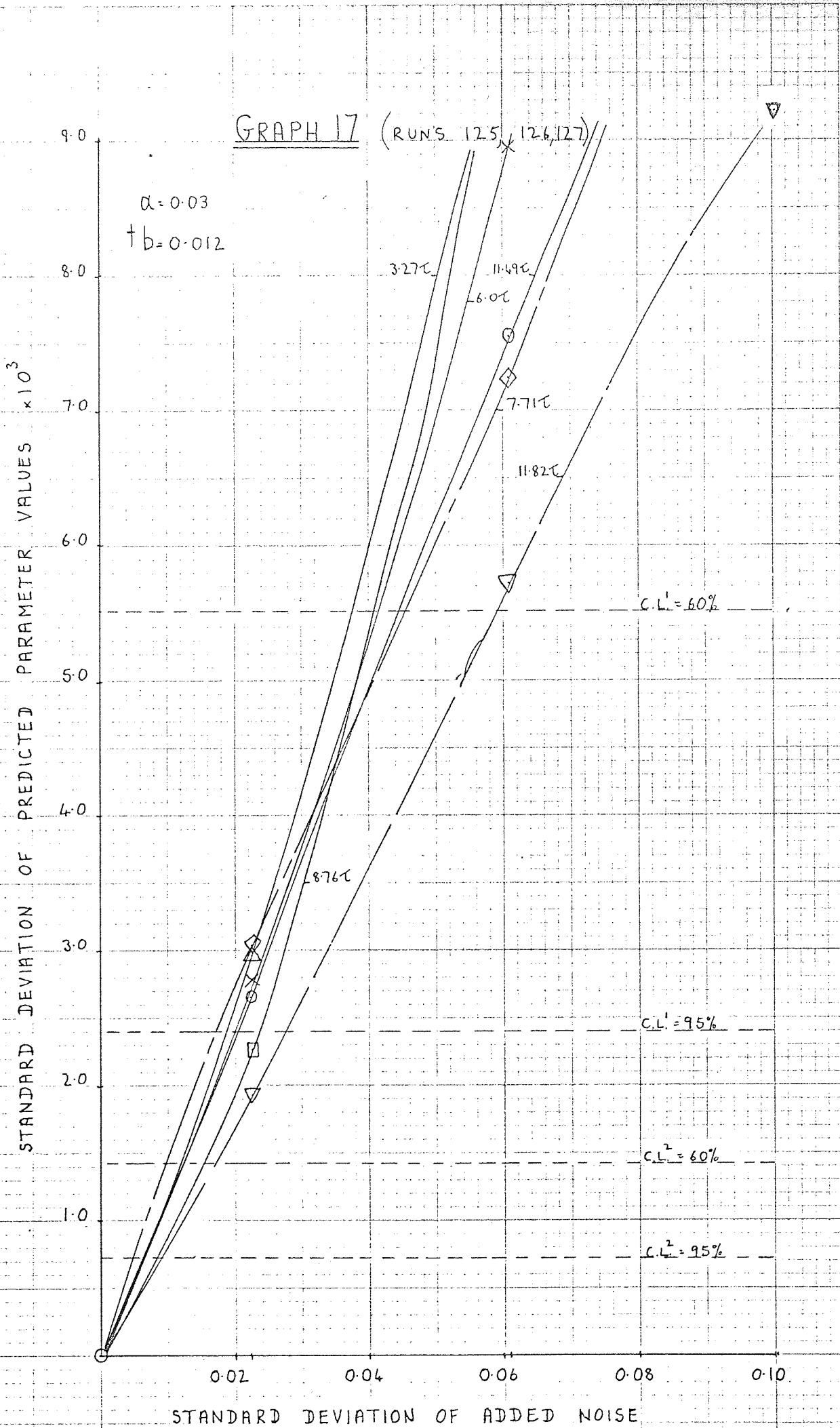
GRAPH 16 (RUNS 122, 123, 124)

$\alpha = 0.03$
 $t_b = 0.021$



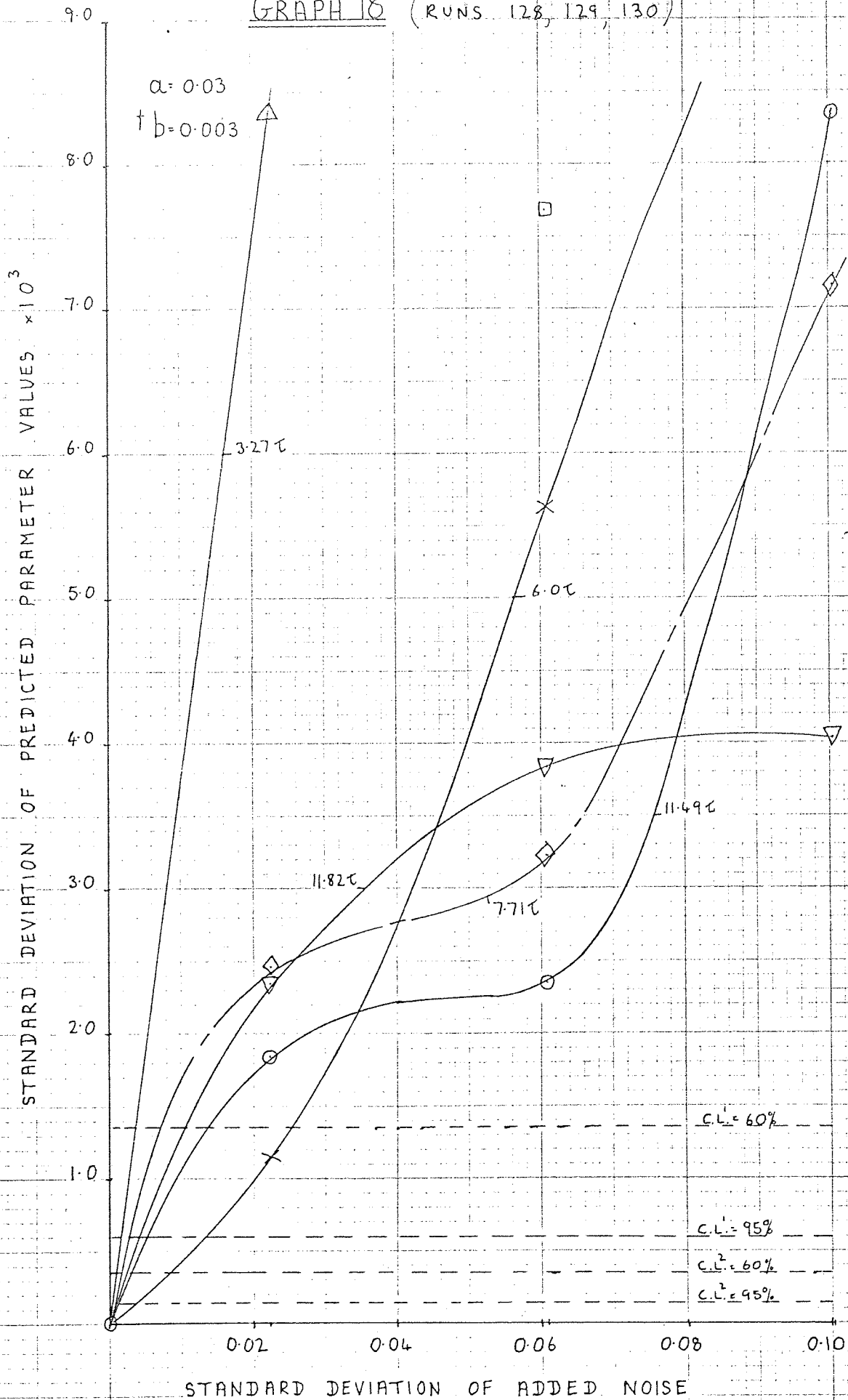
GRAPH 17 (RUNS 125, 126, 127)

$\alpha = 0.03$
 $\dagger b = 0.012$



STANDARD DEVIATION OF ADDED NOISE

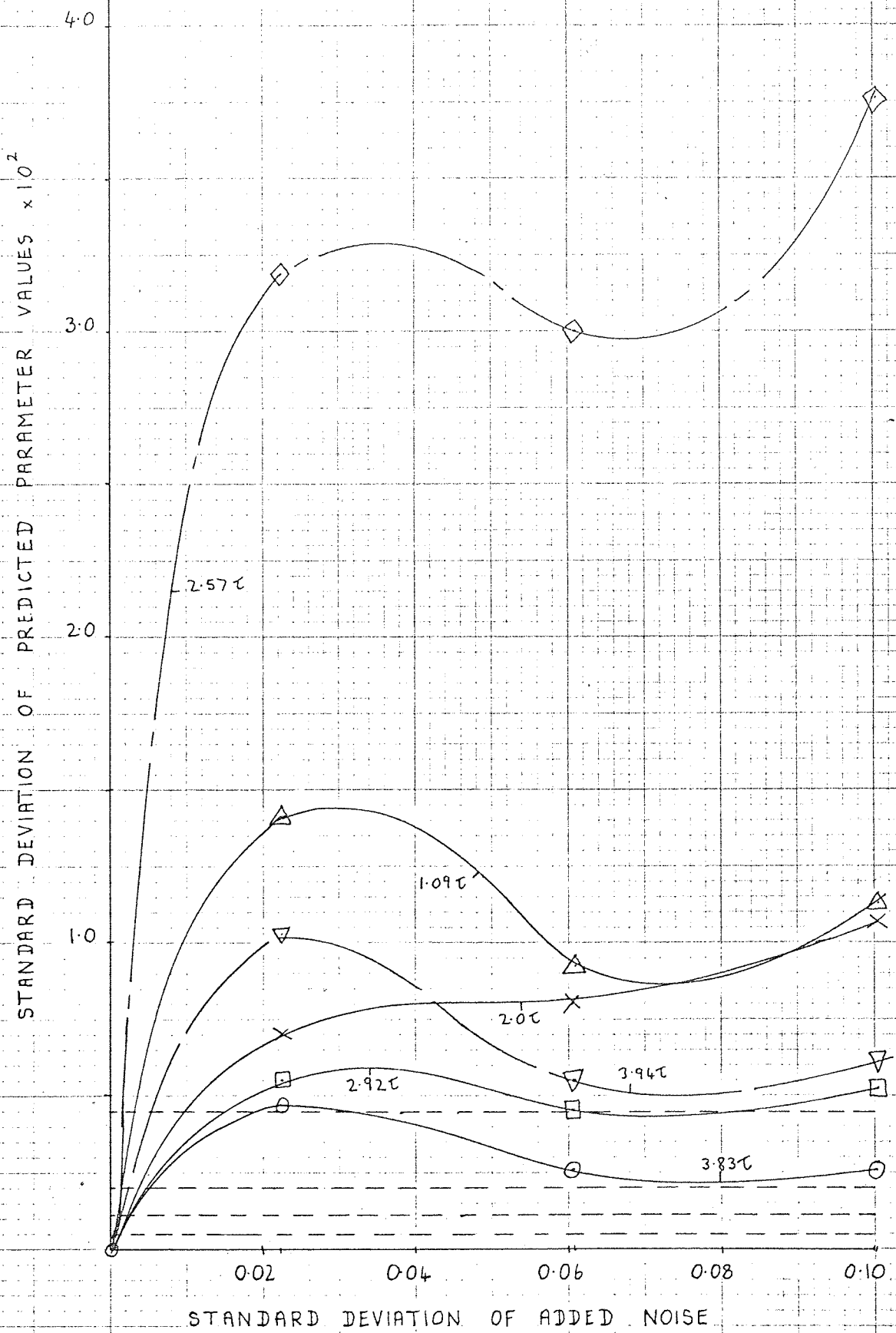
GRAPH 18 (RUNS 128, 129, 130)



GRAPH 19 (RUNS 200, 201, 202)

$t_a = 0.01$

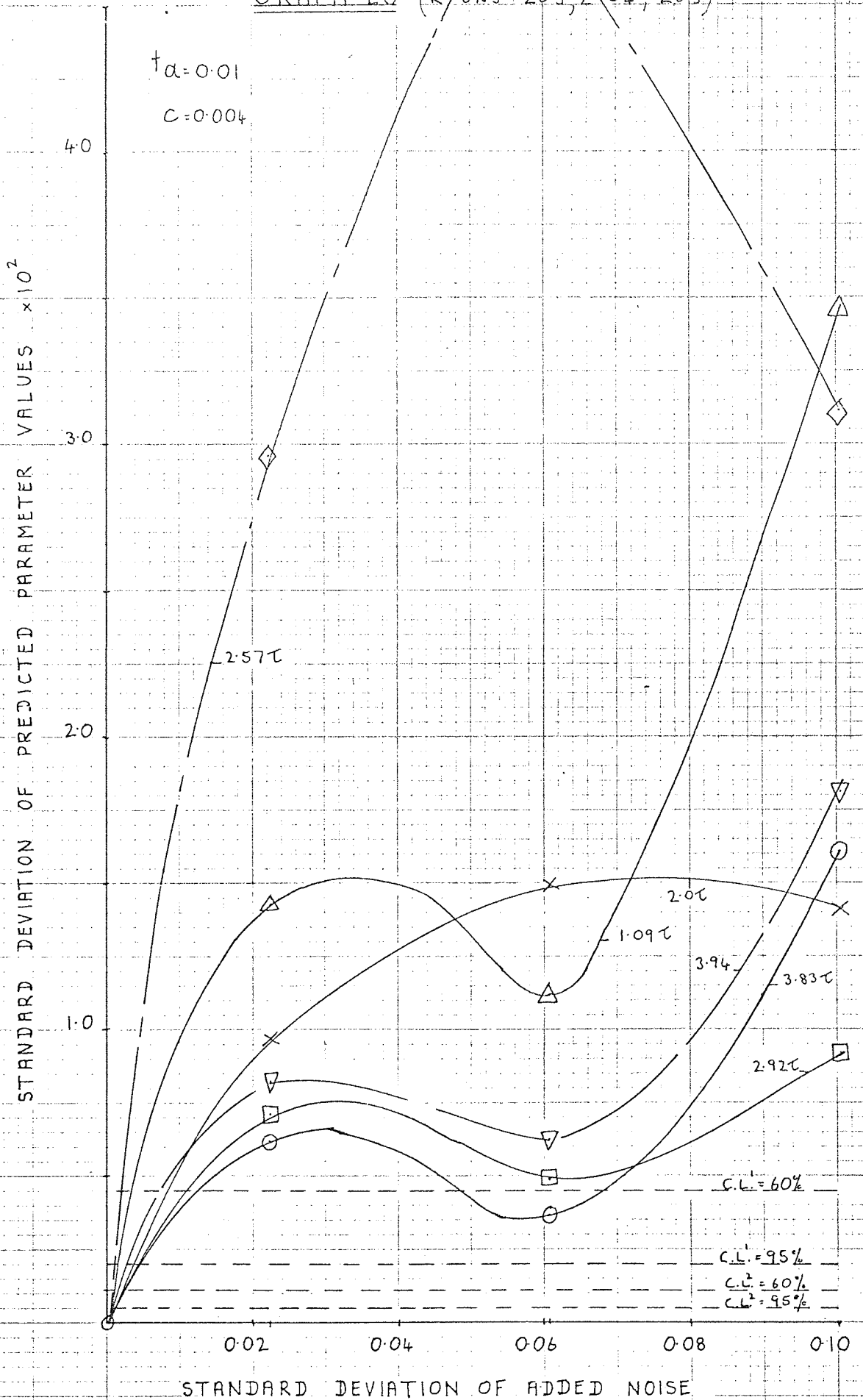
$c = 0.007$



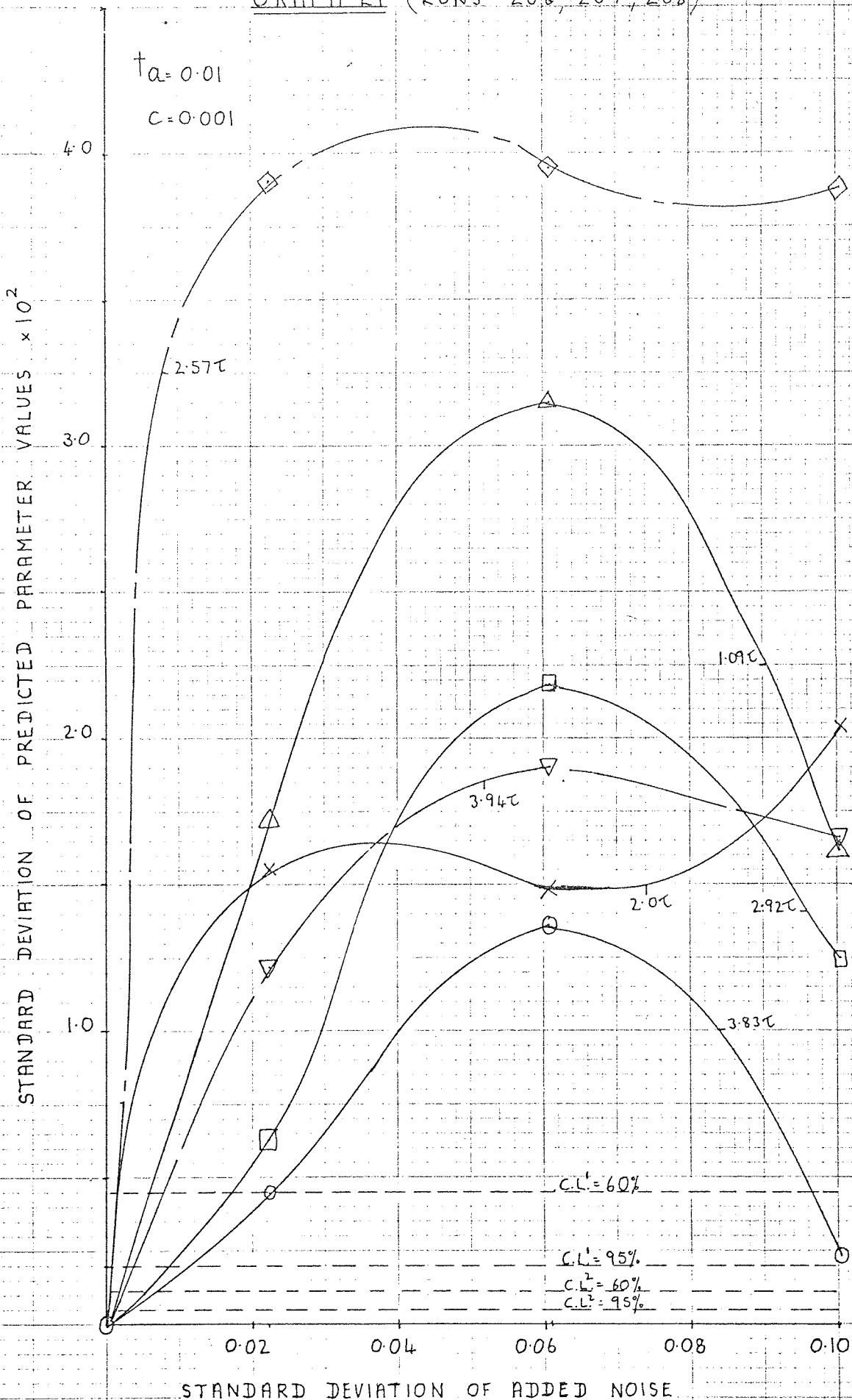
GRAPH 20 (R/UNS 203, 204, 205)

$t_{\alpha} = 0.01$

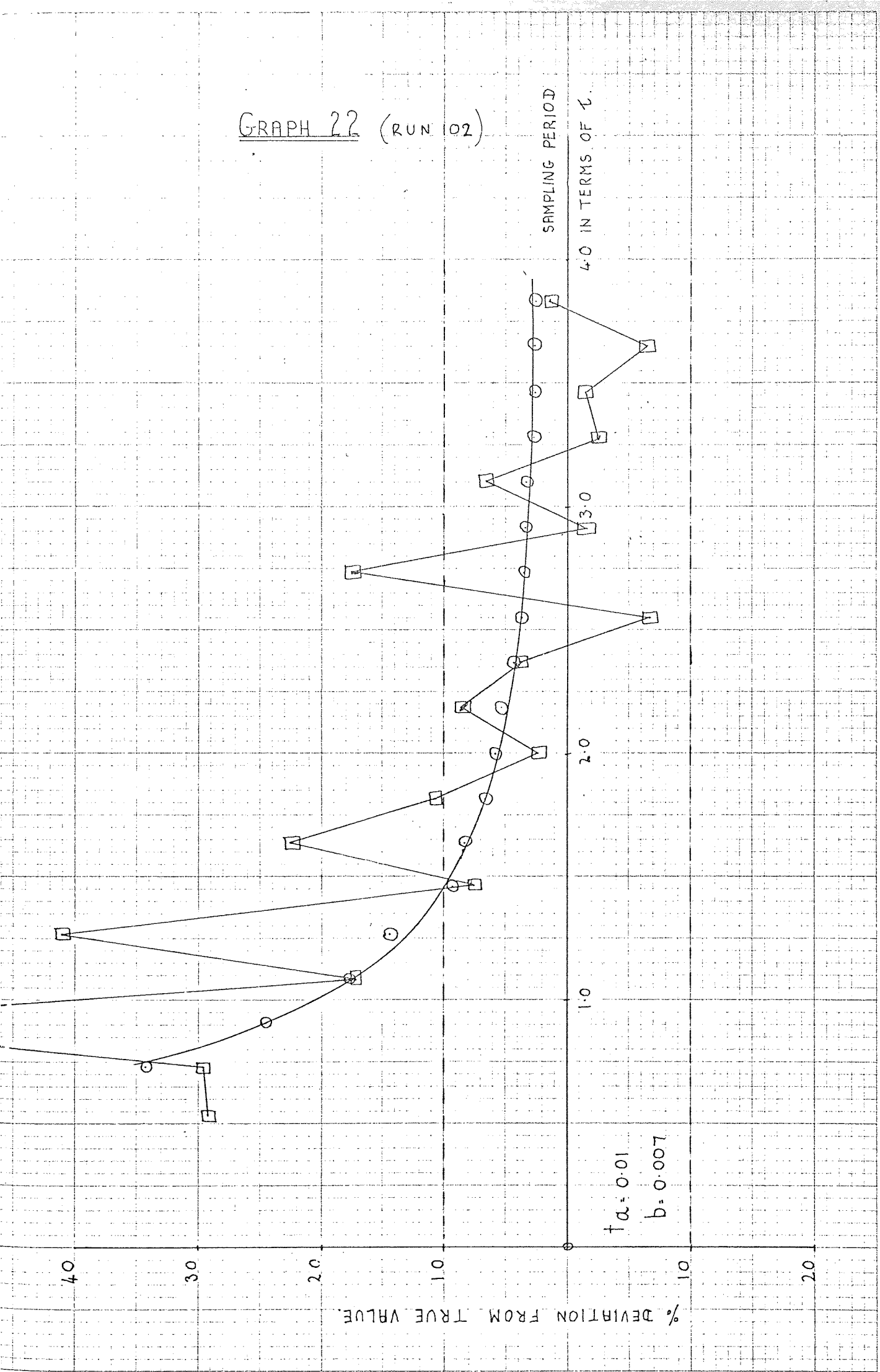
$C = 0.004$



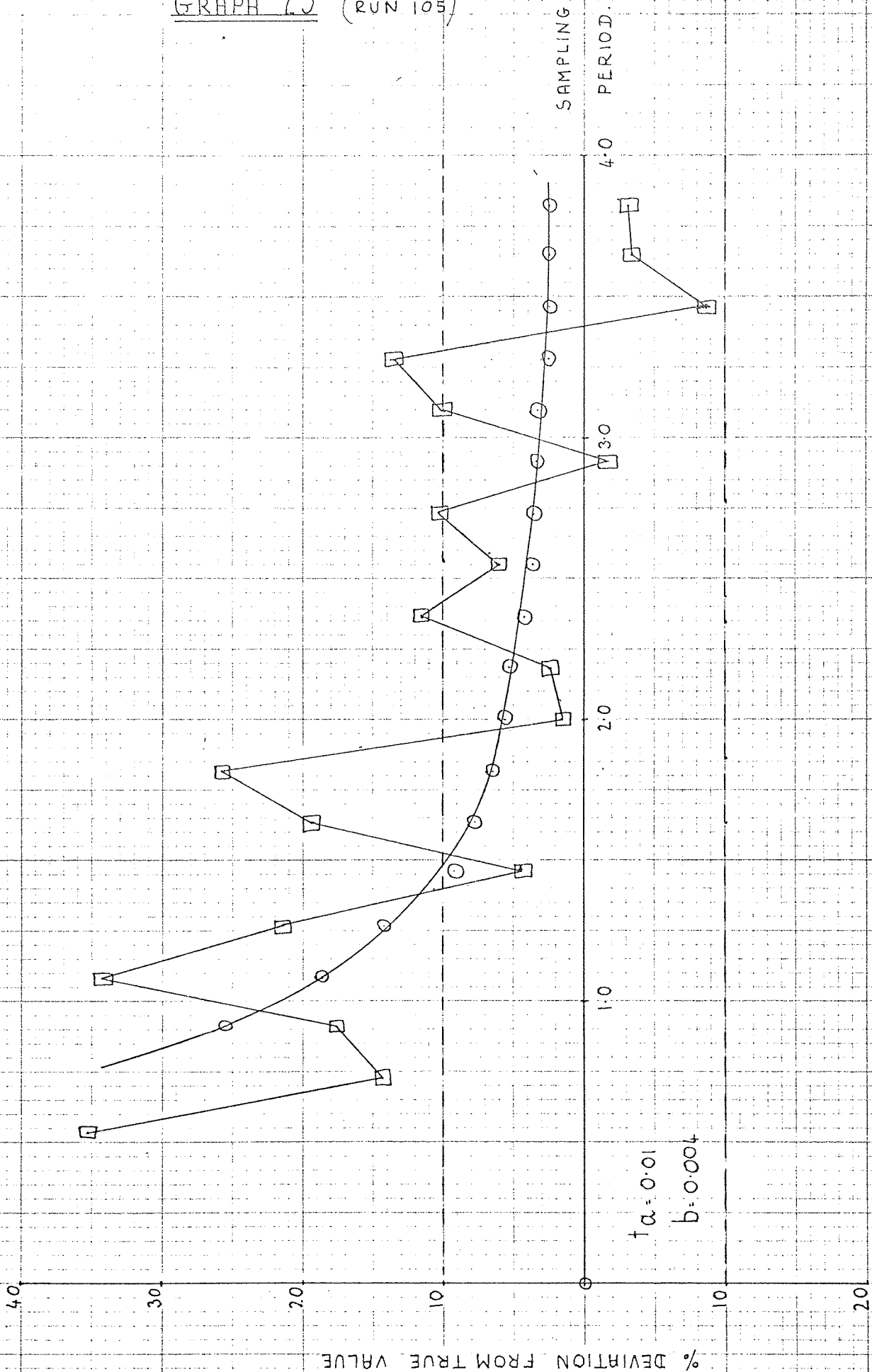
GRAPH 21 (RUNS 206, 207, 208)



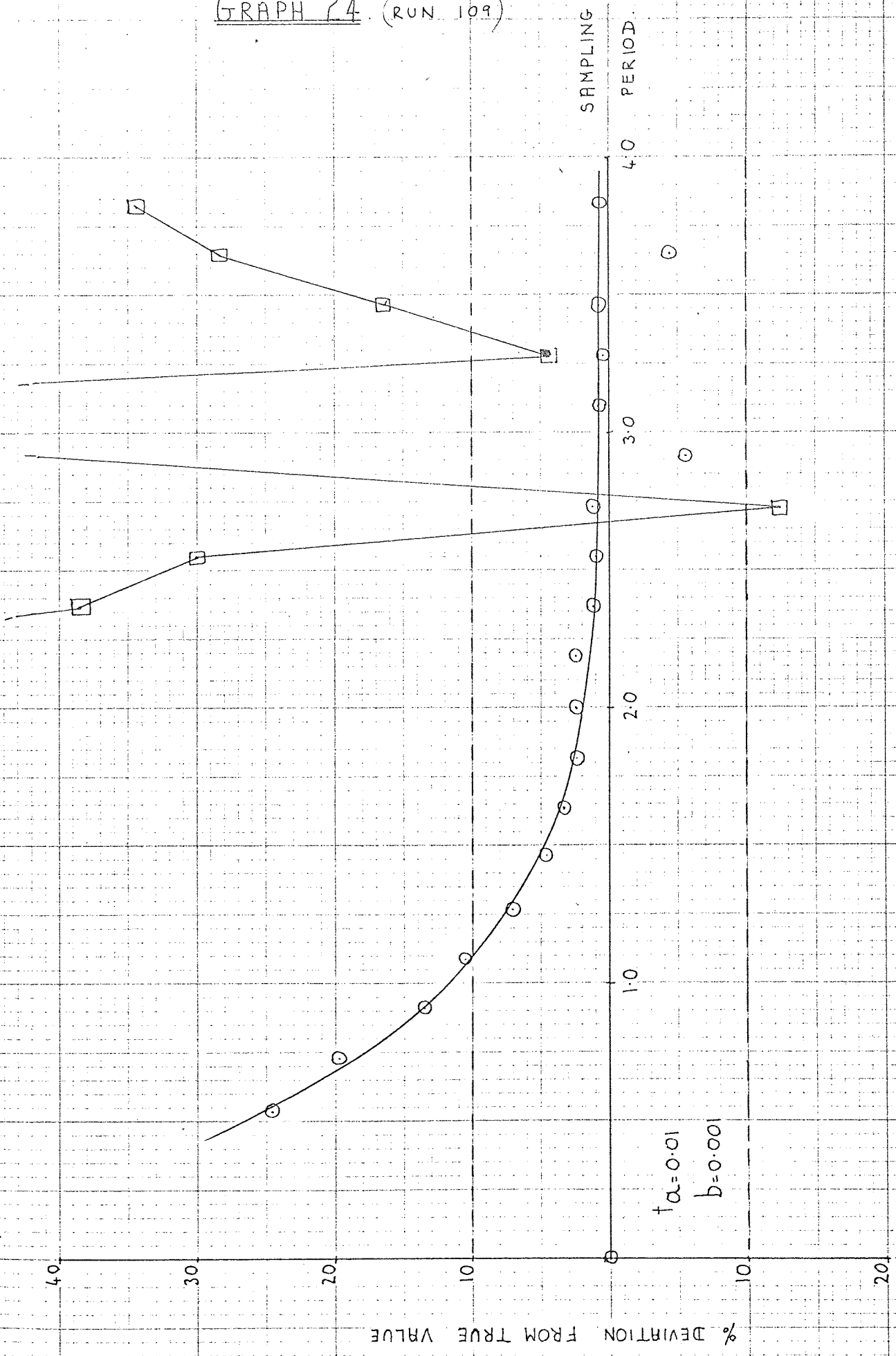
GRAPH 22 (RUN 02)



GRAPH 23 (RUN 105)

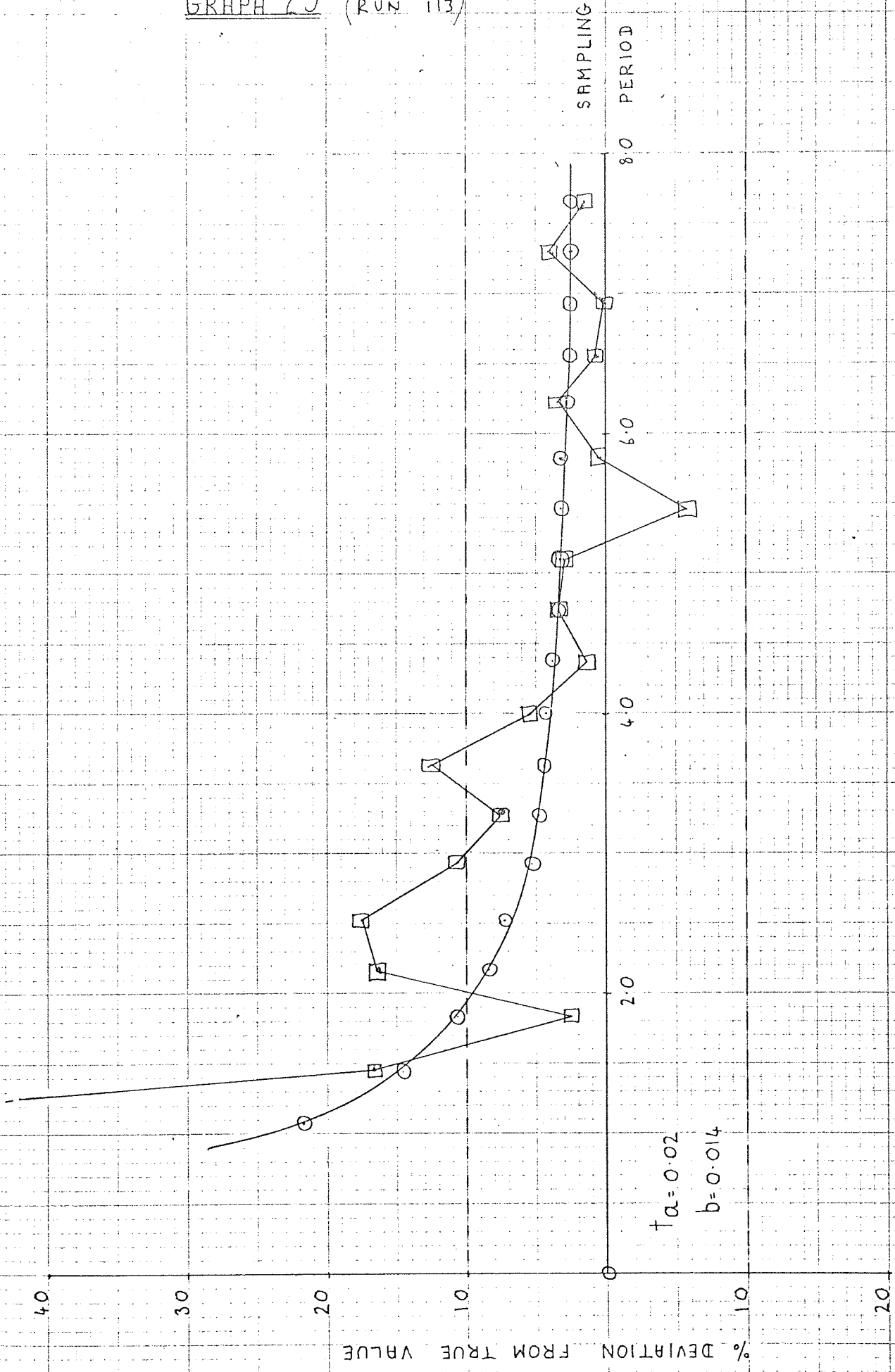


GRAPH 24 (RUN 109)

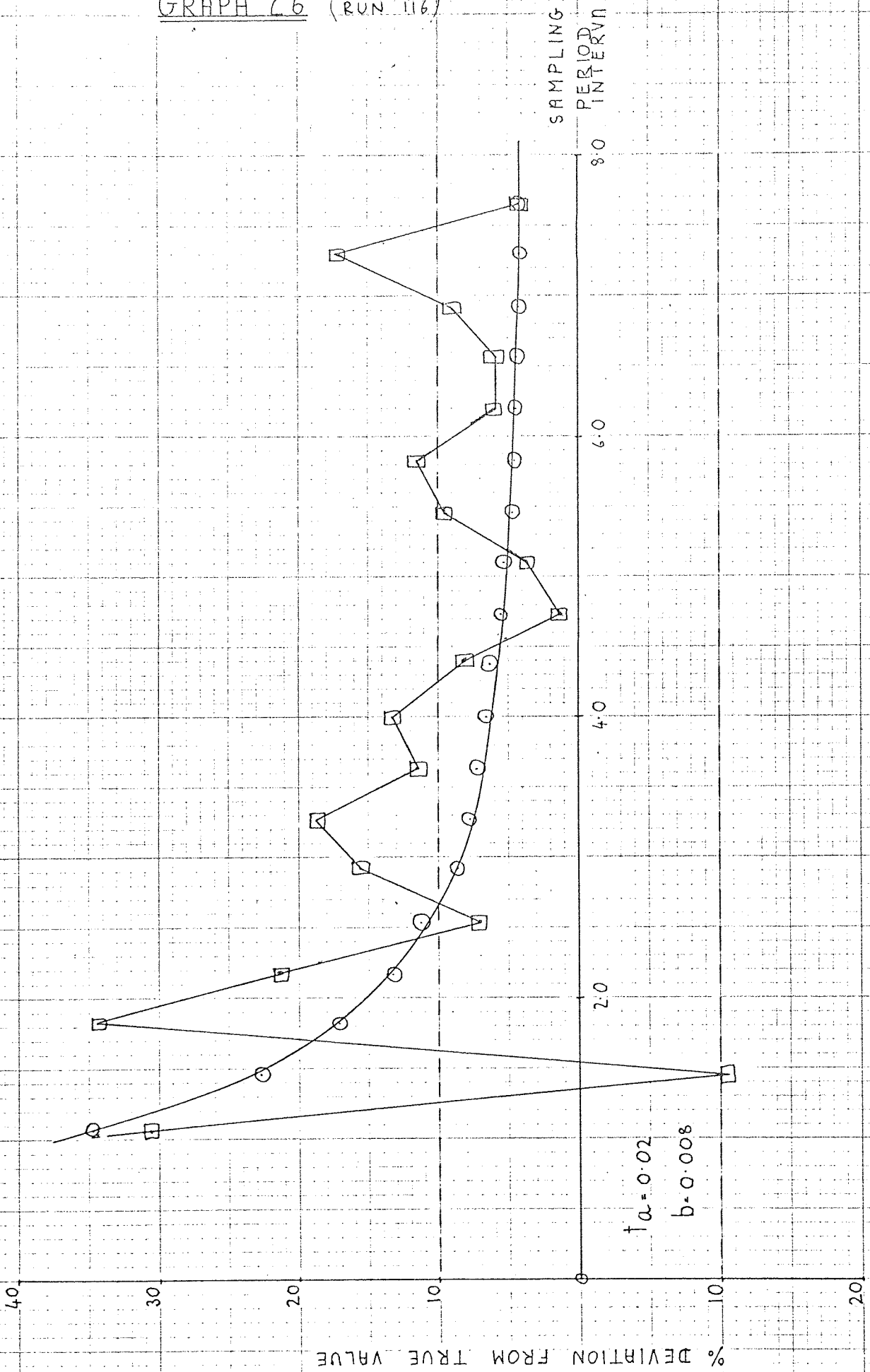


$t_a = 0.01$
 $b = 0.001$

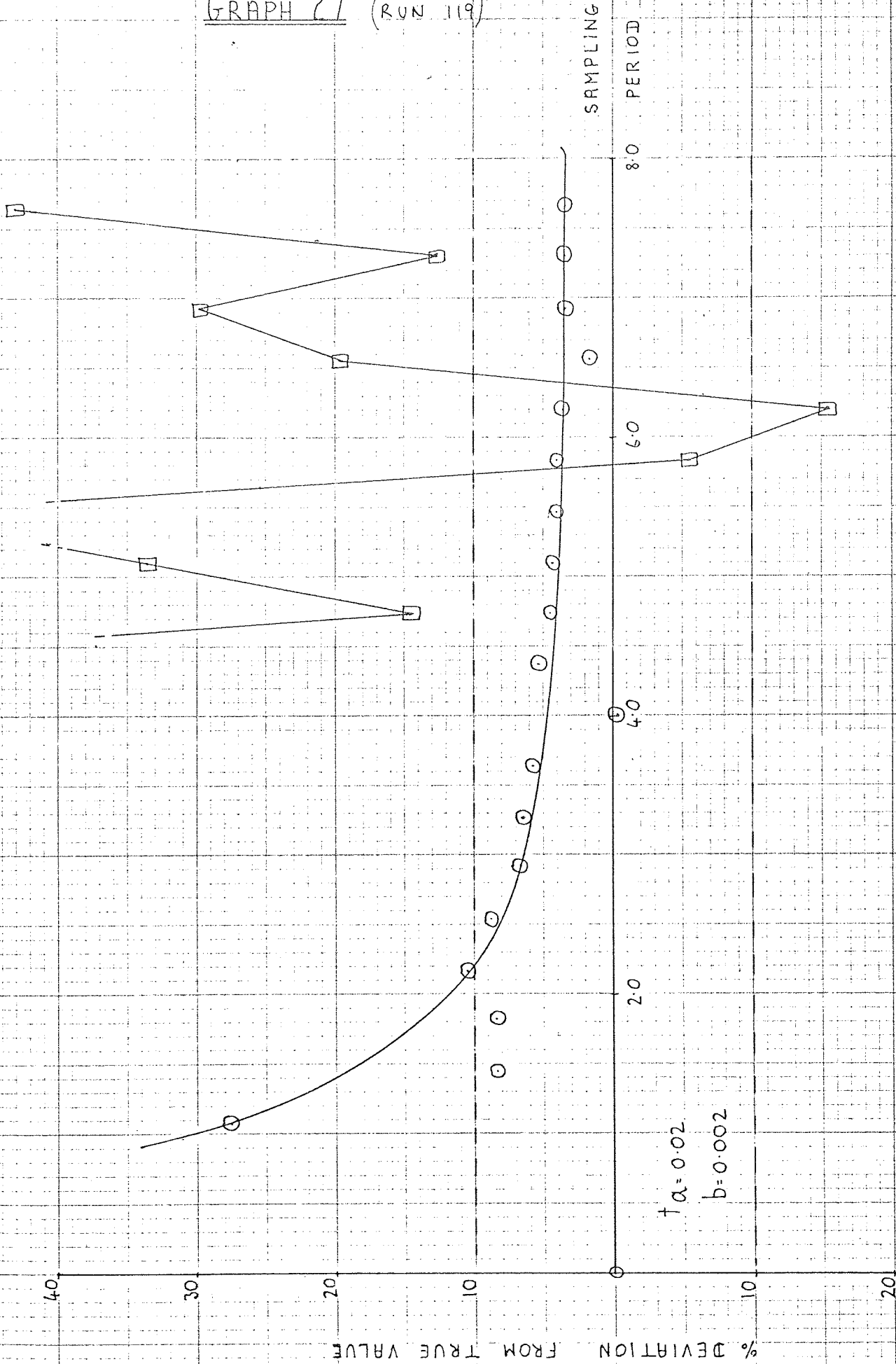
GRAPH 25 (RUN 113)



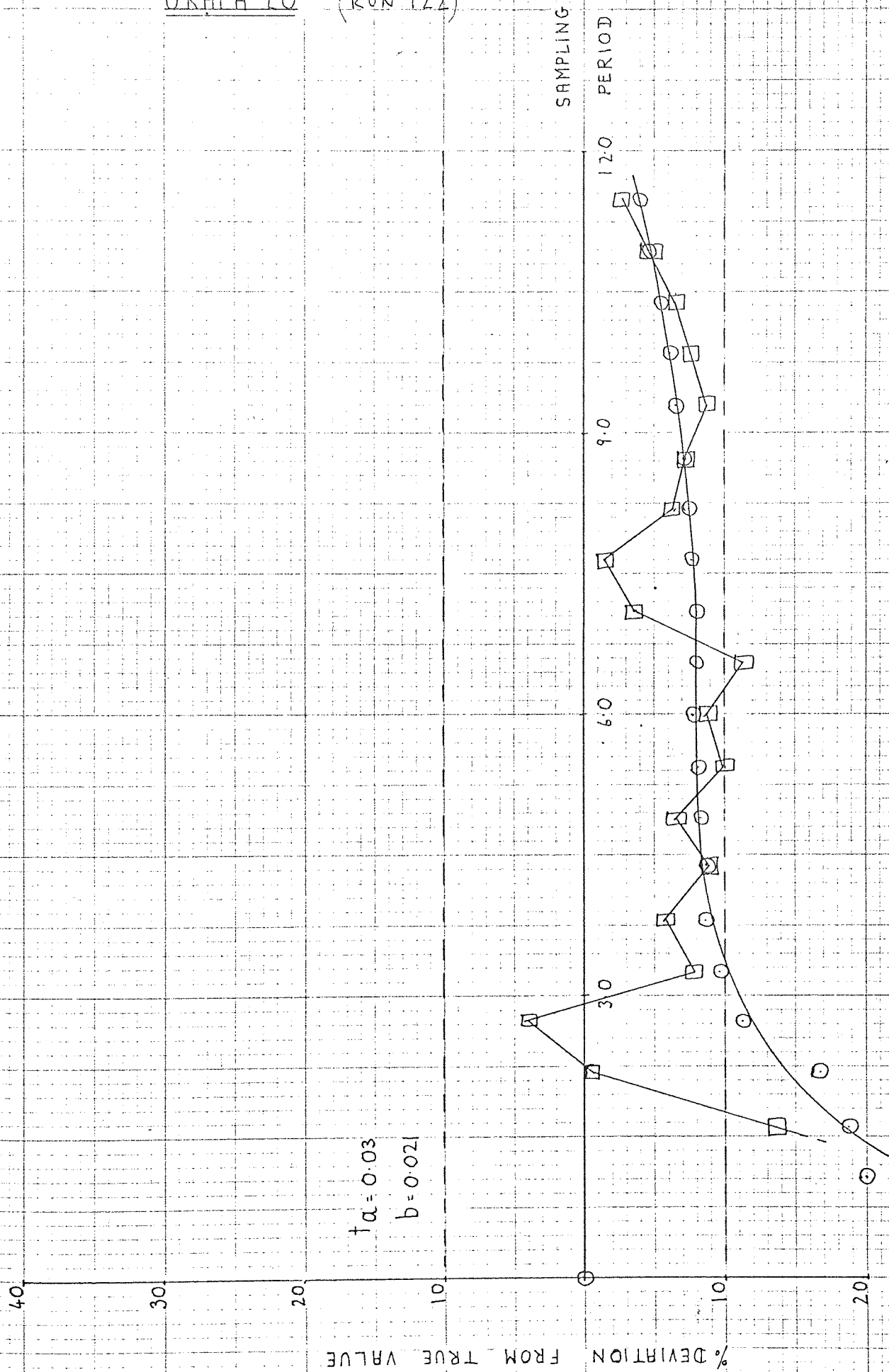
GRAPH 26 (RUN 116)



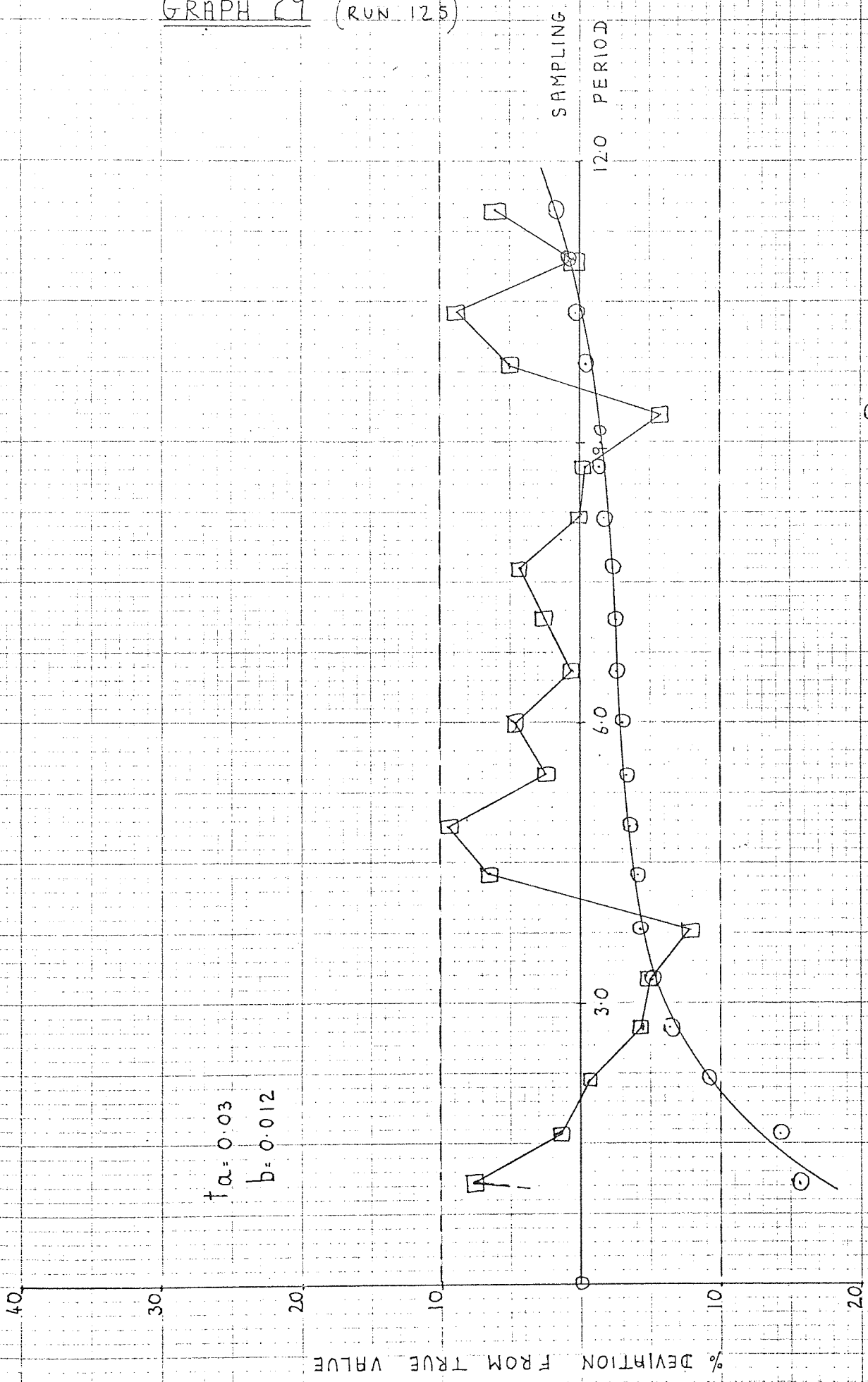
GRAPH 27 (RUN 119)



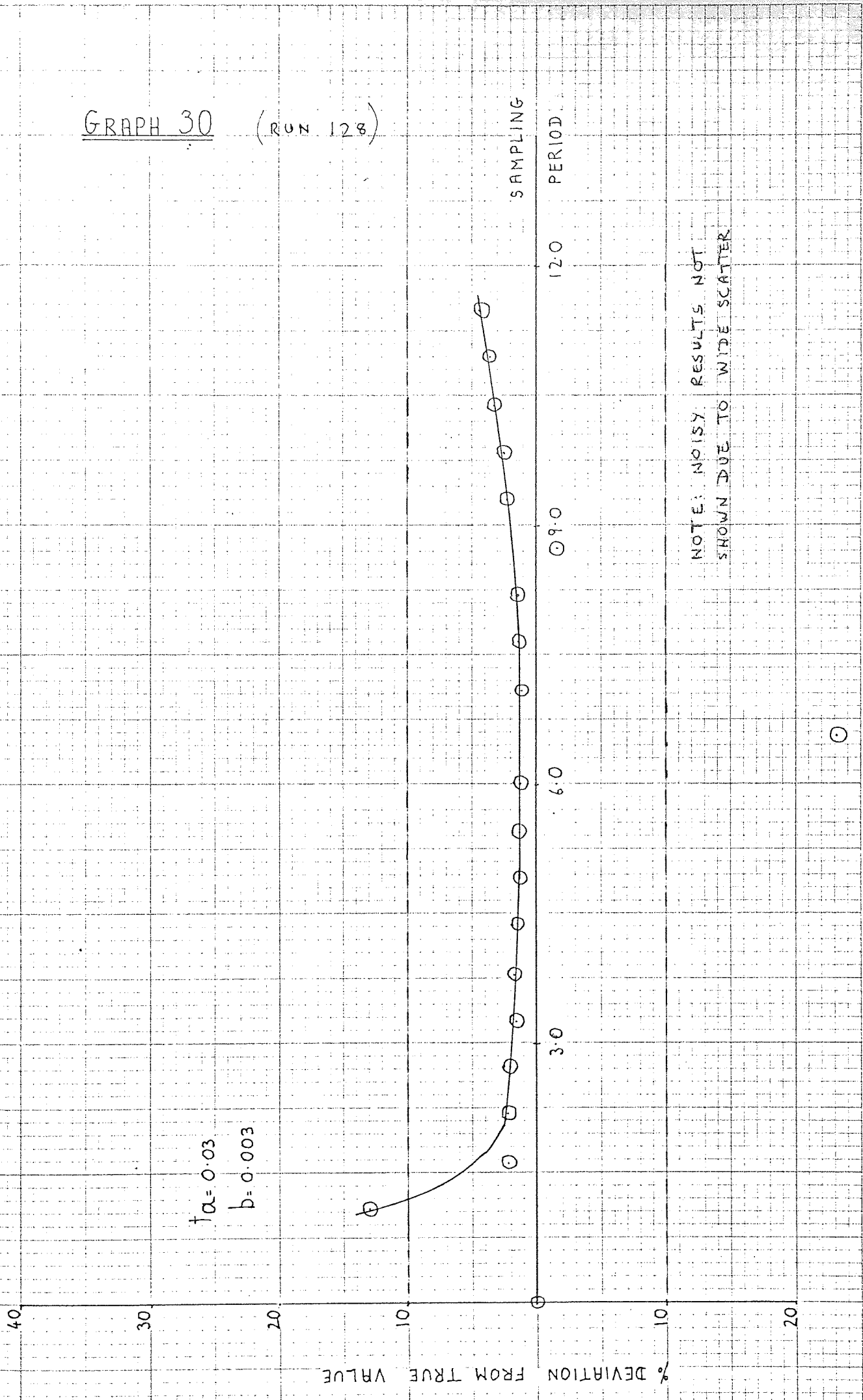
GRAPH 28 (RUN 122)



GRAPH 29 (RUN 125)



GRAPH 30 (RUN 128)



GRAPH 31 (RUN 200)

SAMPLING PERIOD

4.0

3.0

2.0

1.0

$t_{\alpha} = 0.01$

$C = 0.007$

20

10

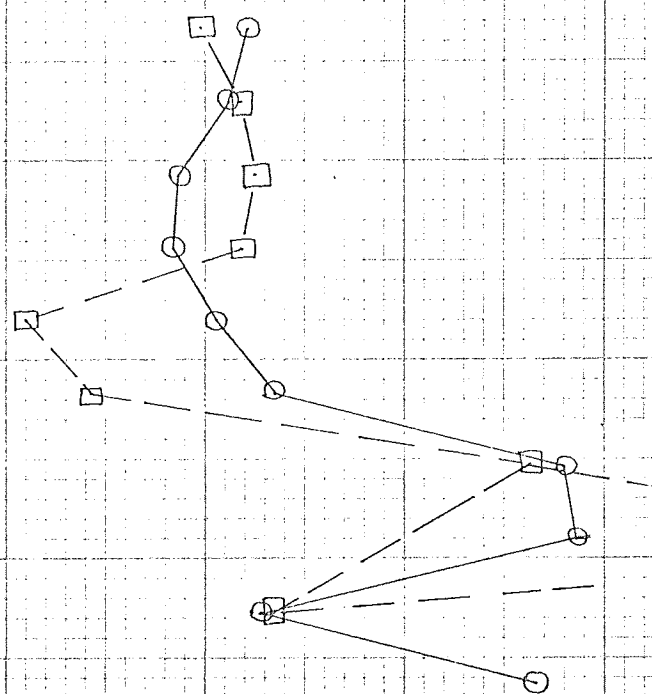
% DEVIATION FROM TRUE VALUE

10

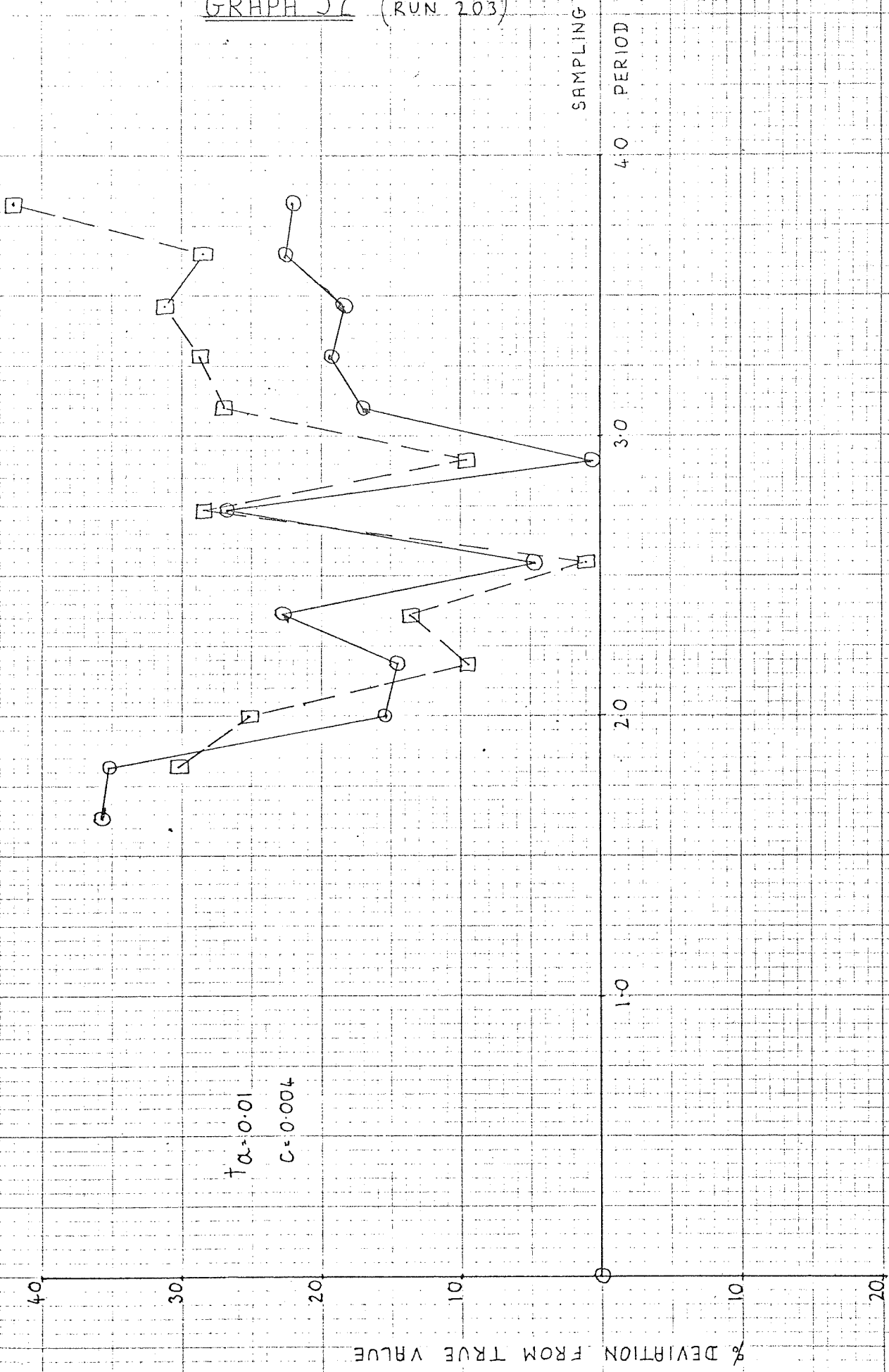
20

30

40



GRAPH 32 (RUN 203)



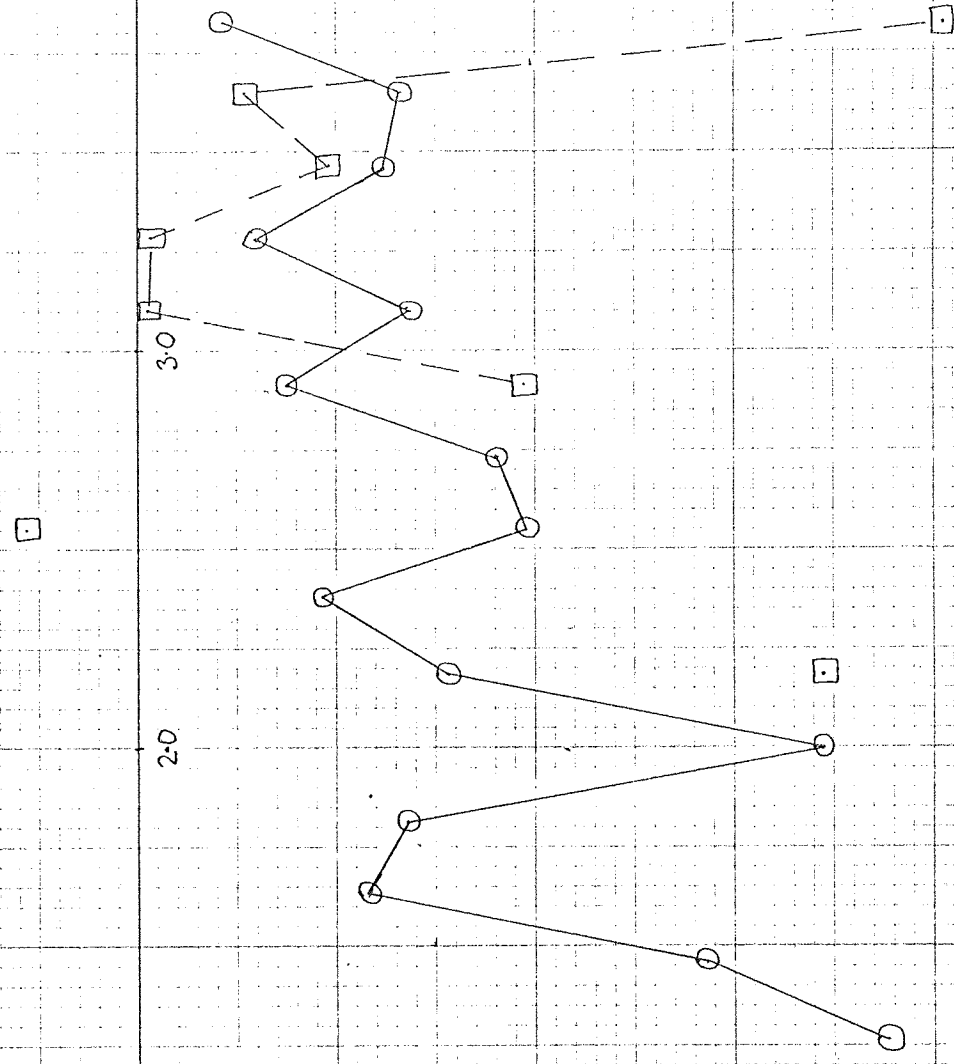
GRAPH 33 (RUN 206)

SAMPLING PERIOD

$\alpha = 0.01$
 $C = 0.001$

20
10
0
10
20
30
40
% DEVIATION FROM TRUE VALUE

40
30
20
10



Appendix V

Tables are given of $w_{i,i}^{s-1}$ and t_i for $N = 3 - 15$. The former tables are taken from Price (3), whilst the latter are taken from Bellman (1).

(a) Tables of $w_{i,i}^{s-1}$ for $N = 3 - 15$

N= 3

.27777778 .44444444 .27777778

.03130602 .22222222 .24647176

.00352824 .11111111 .21869398

N= 4

.17392742 .32607258 .32607258 .17392742

.01207610 .10760704 .21846554 .16185132

.00083847 .03551134 .14636984 .15061368

.00005822 .01171908 .09806640 .14015630

N= 5

.11846344 .23931434 .28444444 .23931434
.11846344

.00555713 .05522545 .14222222 .18408888
.11290631

.00026069 .01274412 .07111111 .14160755
.10760987

.00001223 .00294090 .03555555 .10892944
.10256188

.00000057 .00067866 .01777778 .08379230
.09775069

N= 6

.08566225 .18038079 .23395697 .23395697
 .18038079 .08566225

 .00289241 .03055566 .08906518 .14489180
 .14982513 .08270984

 .00009766 .00517599 .03390626 .08973288
 .12444546 .07997510

 .00000330 .00087679 .01290779 .05557243
 .10336498 .07727472

 .00000011 .00014852 .00491387 .03441654
 .08585544 .07466552

 .00000000 .00002516 .00187066 .02131449
 .07131193 .07214442

N= 7

.06474248 .13985270 .19091503 .20897959
 .19091503 .13985270 .06474248

 .00164744 .01807378 .05671654 .10448980
 .13419849 .12177892 .06309504

 .00004192 .00233575 .01684920 .05224490
 .09433115 .10604089 .06148952

 .00000107 .00030186 .00500552 .02612245
 .06630749 .09233676 .05992486

 .00000003 .00003901 .00148703 .01306122
 .04660903 .08040367 .05840001

 .00000000 .00000504 .00044176 .00653061
 .03276254 .07001275 .05691396

 .00000000 .00000065 .00013124 .00326531
 .02302953 .06096470 .05546572

N= 8

.05061427 .11119052 .15685332 .18134189
 .18134189 .15685332 .11119052 .05061427

 .00100495 .01130438 .03721091 .07403875
 .10730314 .11964241 .09988614 .04960932

 .00001995 .00114928 .00882769 .03022874
 .06349312 .09125919 .08973104 .04862432

 .00000040 .00011684 .00209423 .01234187
 .03756998 .06960942 .08060838 .04765888

 .00000001 .00001188 .00049682 .00503897
 .02223081 .05309572 .07241318 .04671261

 .00000000 .00000121 .00011786 .00205733
 .01315435 .04049962 .06505117 .04578513

 .00000000 .00000012 .00002796 .00083997
 .00778366 .03089174 .05843763 .04487606

 .00000000 .00000001 .00000663 .00034295
 .00460573 .02356317 .05249646 .04398505

N= 9

.04063719 .09032408 .13030535 .15617354
 .16511968 .15617354 .13030535 .09032408
 .04063719

 .00064694 .00740517 .02518989 .05276687
 .08255984 .10340667 .10511547 .08291891

 .03999025

 .00001030 .00060711 .00486956 .01782852
 .04127992 .06846832 .08479515 .07612085
 .03935361

 .00000016 .00004977 .00094136 .00602378
 .02063996 .04533470 .06840303 .06988012
 .03872711

 .00000000 .00000408 .00018198 .00203527
 .01031998 .03001732 .05517975 .06415104
 .03811057

 .00000000 .00000033 .00003518 .00068766
 .00515999 .01987527 .04451272 .05889165
 .03750386

 .00000000 .00000003 .00000680 .00023234
 .00257999 .01315995 .03590777 .05406345
 .03690680

 .00000000 .00000000 .00000131 .00007850
 .00129000 .00871355 .02896629 .04963109
 .03631925

 .00000000 .00000000 .00000025 .00002652
 .00064500 .00576948 .02336669 .04556211
 .03574105

N= 10

.03333567 .07472567 .10954318 .13463336
 .14776211 .14776211 .13463336 .10954318
 .07472567 .03333567

.00043492 .00504162 .01755925 .03814194
 .06288206 .08488005 .09649142 .09198393
 .06968405 .03290075

.00000567 .00034015 .00281466 .01080570
 .02676027 .04875825 .06915518 .07723935
 .06498259 .03247150

.00000007 .00002295 .00045118 .00306128
 .01138818 .02800855 .04956336 .06485825
 .06059832 .03204785

.00000000 .00000155 .00007232 .00086727
 .00484638 .01608915 .03552194 .05446178
 .05650986 .03162973

.00000000 .00000010 .00001159 .00024570
 .00206244 .00924221 .02545850 .04573182
 .05269723 .03121707

.00000000 .00000001 .00000186 .00006961
 .00087770 .00530907 .01824604 .03840123
 .04914184 .03080979

.00000000 .00000000 .00000030 .00001972
 .00037352 .00304973 .01307690 .03224569
 .04582632 .03040782

.00000000 .00000000 .00000005 .00000559
 .00015895 .00175188 .00937218 .02707686
 .04273449 .03001110

.00000000 .00000000 .00000001 .00000158
 .00006765 .00100634 .00671702 .02273657
 .03985127 .02961955

N=

11

.02783428 .06279018 .09314511 .11659688
 .13140227 .13646254 .13140227 .11659688
 .09314511 .06279018 .02783428

 .00030299 .00354568 .01256751 .02803595
 .04799184 .06823127 .08341043 .08856093
 .08057760 .05924450 .02753129

 .00000330 .00020022 .00169566 .00674130
 .01752799 .03411563 .05294657 .06726629
 .06970575 .05589904 .02723159

 .00000004 .00001131 .00022879 .00162096
 .00640172 .01705782 .03360898 .05109198
 .06030077 .05274249

 .00000000 .00000064 .00003087 .00038976
 .00233809 .00852891 .02133402 .03880681
 .05216475 .04976419 .02664195

 .00000000 .00000004 .00000416 .00009372
 .00085394 .00426445 .01354223 .02947564
 .04512647 .04695407 .02635193

 .00000000 .00000000 .00000056 .00002253
 .00031188 .00213223 .00859622 .02238816
 .03903783 .04430264 .02606507

 .00000000 .00000000 .00000008 .00000542
 .00011391 .00106611 .00545664 .01700489
 .03377069 .04180093 .02578134

 .00000000 .00000000 .00000001 .00000130
 .00004160 .00053306 .00346372 .01291603
 .02921421 .03944048 .02550069

 .00000000 .00000000 .00000000 .00000031
 .00001519 .00026653 .00219867 .00981034
 .02527251 .03721333 .02522310

 .00000000 .00000000 .00000000 .00000008
 .00000555 .00013326 .00139565 .00745143
 .02186264 .03511194 .02494853

N= 12

.02358767	.05346966	.08003916	.10158371
.11674627	.12457352	.12457352	.11674627
.10158371	.08003916	.05346966	.02358767
.00021747	.00256341	.00920840	.02096088
.03690166	.05448638	.07008714	.07984461
.08062282	.07083076	.05090625	.02337020
.00000201	.00012289	.00105941	.00432509
.01166403	.02383143	.03943220	.05460699
.06398703	.06268178	.04846574	.02315473
.00000002	.00000589	.00012188	.00089244
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.05078388	.05547033	.04614222	.02294125
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.00000000	.00000001	.00000161	.00003800
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.03198849	.04344097	.04182403	.02252018
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.00003680	.00038147	.00222287	.00817074
.02014938	.03402031	.03790996	.02210684
.00000000	.00000000	.00000000	.00000033
.00001163	.00016685	.00125062	.00558810
.01599173	.03010632	.03609250	.02190302
.00000000	.00000000	.00000000	.00000007
.00000368	.00007298	.00070362	.00382179
.01269198	.02664263	.03436218	.02170108
.00000000	.00000000	.00000000	.00000001
.00000116	.00003192	.00039587	.00261378
.01007311	.02357743	.03271481	.02150100
.00000000	.00000000	.00000000	.00000000
.00000037	.00001396	.00022272	.00178761
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13

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 .10390802 .11314159 .11627578 .11314159
 .10390802 .08907299 .06943676 .04606075
 .02024200

.00016008 .00189774 .00688889 .01592851
 .02865301 .04353358 .05813789 .06960801
 .07525501 .07314448 .06254787 .04416301
 .02008192

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 .00790117 .01675045 .02906894 .04282487
 .05450317 .06006440 .05634244 .04234346
 .01992310

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 .03947372 .04932336 .05075265 .04059887
 .01976554

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 .01960922

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 .02070526 .03326012 .04118176 .03732238
 .01945414

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 .01930029

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 .01899623

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 .01884600

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 .01869695

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 .01854909

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 .01840239

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 .10259923 .09276920 .07860158 .06075929
 .04007904 .01755973

.00012043 .00143413 .00524956 .01228964
 .02248500 .03492927 .04800088 .05963105
 .06766996 .07028420 .06631194 .05550973
 .03864491 .01743930

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 .04463214 .05324902 .05594384 .05071372
 .03726210 .01731970

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 .03464314 .01708296

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 .03340352 .01696580

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 .00001881 .00015974 .00084972 .00311264
 .00844607 .01754394 .02833963 .03533061
 .03220826 .01684945

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 .00557066 .01329172 .02390863 .03227807
 .03105576 .01673389

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 .00000110 .00001851 .00016842 .00095541
 .00367416 .01007013 .02017043 .02948926
 .02994451 .01661913

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 .02887302 .01650515

.00000000	.00000000	.00000000	.00000000
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.00159831	.00578020	.01435609	.02461369
.02783987	.01639196		

.00000000	.00000000	.00000000	.00000000
.00000002	.00000073	.00001494	.00016247
.00105418	.00437922	.01211146	.02248708
.02684368	.01627954		

.00000000	.00000000	.00000000	.00000000
.00000000	.00000025	.00000666	.00009002
.00069529	.00331780	.01021779	.02054421
.02588315	.01616790		

.00000000	.00000000	.00000000	.00000000
.00000000	.00000008	.00000297	.00004987
.00045858	.00251365	.00862020	.01876921
.02495698	.01605701		

N=

15

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 .09921574 .09308050 .08313460 .06978534
 .05357961 .03518302 .01537662

.00009232 .00110346 .00406652 .00961580
 .01783353 .02819635 .03962706 .05064456
 .05958868 .06488415 .06530107 .06016954
 .04951309 .03407956 .01528430

.00000055 .00003461 .00030864 .00132497
 .00382554 .00854136 .01582716 .02532228
 .03578879 .04522916 .05129308 .05187871
 .04575521 .03301072 .01519254

.00000000 .00000109 .00002342 .00018257
 .00082063 .00258739 .00632142 .01266114
 .02149464 .03152815 .04029000 .04473028
 .04228254 .03197539 .01510133

.00000000 .00000003 .00000178 .00002516
 .00017604 .00078378 .00252479 .00633057
 .01290962 .02197751 .03164724 .03856685
 .03907344 .03097254 .01501066

.00000000 .00000000 .00000013 .00000347
 .00003776 .00023743 .00100841 .00316528
 .00775348 .01531998 .02485846 .03325268
 .03610789 .03000114 .01492054

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 .00465672 .01067919 .01952598 .02867075
 .03336742 .02906020 .01483096

.00000000 .00000000 .00000000 .00000007
 .00000174 .00002179 .00016086 .00079132
 .00279681 .00744420 .01533738 .02472018
 .03083494 .02814878 .01474192

.00000000 .00000000 .00000000 .00000001
 .00000037 .00000660 .00006425 .00039566
 .00167976 .00518917 .01204730 .02131396
 .02849467 .02726594 .01465342

.00000000 .00000000 .00000000 .00000000
 .00000008 .00000200 .00002566 .00019783
 .00100886 .00361725 .00946299 .01837708
 .02633202 .02641079 .01456544

.00000000 .00000000 .00000000 .00000000
 .00000002 .00000061 .00001025 .00009892
 .00060592 .00252149 .00743305 .01584488
 .02433351 .02558246 .01447799

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.00000000	.00000018	.00000409	.00004946
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.02248667	.02478011	.01439107	
.00000000	.00000000	.00000000	.00000000
.00000000	.00000006	.00000163	.00002473
.00021856	.00122523	.00458610	.01177915
.02078001	.02400292	.01430467	
.00000000	.00000000	.00000000	.00000000
.00000000	.00000002	.00000065	.00001236
.00013127	.00085408	.00360232	.01015609
.01920288	.02325011	.01421879	
.00000000	.00000000	.00000000	.00000000
.00000000	.00000001	.00000026	.00000618
.00007884	.00059536	.00282957	.00875667
.01774544	.02252091	.01413342	

(b) Tables of t_{α} for $N = 3 - 15$

$N = 3$

2.183011
0.693147
0.119574

$N = 4$

2.667410
1.108634
0.400492
0.071960

$N = 5$

3.059523
1.466354
0.693147
0.262359
0.048046

$N = 6$

3.388323
1.775520
0.965769
0.479150
0.185601
0.034348

$N = 7$

3.671195
2.046127
1.213762
0.693147
0.352509
0.138382
0.025775

$N = 8$

3.919296
2.286055
1.438709
0.895796
0.524726
0.270804
0.107214
0.020055

$N = 9$

4.140187
2.501226
1.643438
1.085084
0.693147
0.412298
0.214821
0.085541
0.016048

N = 10

4.339217
 2.696097
 1.830738
 1.261241
 0.854343
 0.554365
 0.333101
 0.174705
 0.069852
 0.013133

N = 11

4.520308
 2.874069
 2.003044
 1.425235
 1.007232
 0.693147
 0.454490
 0.275032
 0.144938
 0.058126
 0.010945

N = 12

4.686415
 3.037776
 2.162400
 1.578225
 1.151746
 0.826945
 0.575157
 0.379921
 0.231101
 0.122223
 0.049129
 0.009262

N = 13

4.839821
 3.189298
 2.310507
 1.721346
 1.288247
 0.955107
 0.693147
 0.485760
 0.322624
 0.197019
 0.104484
 0.042074
 0.007940

N = 14

4.982325
 3.330295
 2.448775
 1.855635
 1.417266
 1.077505
 0.807498
 0.590541
 0.416188
 0.277568
 0.170022
 0.090362
 0.036438
 0.006882

N = 15

5.115372
 3.462117
 2.578382
 1.982016
 1.539381
 1.194272
 0.917784
 0.693147
 0.509831
 0.360861
 0.241453
 0.148258
 0.078931
 0.031866
 0.006022

Appendix VI

In this appendix all Assembler language listings for the PDS. 1020 computer are given.

General Data-Logging Program

```

BGN
  JMP A0      /START.
  JMP R1      /CHANNEL RANGE.
  JMP R3      /GAINS.
  JMP R5      /CHANNEL PRINT-OUT.
  JMP R8      /INPUT MODE AND FILTER.
  JMP RL      /SCALE.
  JMP A5      /RETURN.
  ELA
  STA VL
  JMP A6+2
A0 OUT 403
  BCI GENERAL DATA LOGGING PROGRAM.
  OUT 403
  OUT 403
  SWL 1
  JPL FR
  JPL IN
A1 TSW 22
  TOV A2
  JMP A1
A2 TSW 88
  TOV A6
  JMP JC
A5 TSW 22
  TOV A5
  JMP A1
A6 JPL CR
  JMP A8
  JPL CR
  JPL SH
  JPL SQ
  JMP **
A8 JPL GC
  JPL GH
  JPL GP
A9 JPL CH
  JMP CP
FR OUT 403
  OUT 403
  BCI FILTER (IN OR NO?):
  LMW FW
  EIR
  TXH *
  LDH ZO
  ITY
  AND DD+1
  ALS 2
  CPY BB
  ITY
  ... AND DD+1
  ADD BB
  AND FO
  TOV F2
  LDA FA
  CPY FX
  RTN
F2 LDA ZO
  CPY FX
  RTN
CR ELA
  STA CZ
  LMW UN
  EIR
JL JPL **      /CHANNEL RANGE.
  CPX AZ
  JPL RR      /RANGE CHECK.
  TXL JL
  LDA AA
  SUB AZ
  TMI KK
  LDA AA
  CPY BB
  LDA AZ
  CPY AA
  LDA BB
  CPY AZ
KK LDA AZ
  SUB AA
  CPY CC
  JPL BC      /BINARY CONVERSION.
  CPY CB
  OUT 403
  OUT 403
  BCI FIRST CHANNEL NO.:
  LDA AA
  JPL S1
  OUT 403
  OUT 403
  BCI LAST CHANNEL NO.:
  LDA AZ
  JPL S1
  OUT 403
  OUT 403
CZ JMP **
RR SUB TT
  TMI ER
  SUB TT
  TMI RS
  OUT 403

```

ER BCI CHANNEL OUTSIDE PERMITTED RANGE.

HLT **
 RS RTN
 S1 ALS 23
 OTY
 ALS 1
 OTY
 RTN
 BC CPY BB
 ARS 1
 IZE EN
 SUB UN
 EIR
 LDA BB
 BD SUB T1
 BAD TB
 STA BB
 TXH BD
 EN LMW BB
 RTN
 SH ELA
 STA N2
 OUT 403
 OUT 403
 BCI CALIBRATION FACTORS(INPUT BASES, THEN GRADIENTS).
 OUT 403
 OUT 403
 JMP CN
 SP ELA
 STA L3
 LDA CC
 CPY CO
 LMW **
 STA LL
 STA LC
 STA LA
 V7 JPL LO
 JPL S2
 OUT 423
 SWL 1
 LDA CO
 SUB UN
 TMI L3
 CPY CO
 LMW LL
 BAD LO
 STA LL
 STA LC
 STA LA
 JMP V7
 L3 JMP **
 LO SWL 2
 ELA
 STA LA+1
 LDA ZO
 IDK
 ALS 5
 LL CPY **
 LDA ZO
 IDK
 CPY EE

LMW AT
 EIR
 LDA EE
 L1 ARS 1
 TZE L2
 TXH L1
 L2 EIR
 BRS
 STA *+2
 LDA EE
 ALS 0
 LC ADD **
 LA CPY **
 JMP **
 SQ ELA
 STA *+9
 LMW QZ
 STA SP+4
 JPL SP
 OUT 403
 OUT 403
 LMW QY
 STA SP+4
 JPL SP
 JMP **
 GC LMW AG
 STA G3
 LDA CC
 CPY CO
 LDA AA
 GO ADD T3
 CPY BB
 LMW TH
 EIR
 LDA BB
 OPP
 IDP
 SSP
 AND DX
 G5 ARS 1
 TZE G2
 TXH G5
 G2 EIR
 ALS 3
 ADD FX
 ADD BB
 G3 CPY **
 LDA CO
 SUB UN
 CPY CO
 TMI G4
 LMW G3
 BAD G5
 STA G3
 LDA CC
 SUB CO
 ADD AA
 JMP GO
 G4 RTN
 GH ELA
 STA N2
 OUT 403

OUT 403	OUT 403
BCI GAINS.	JMP CN
OUT 403	CP TSW 88
OUT 403	TOV A4
JMP CN	JMP A5
GP ELA	A4 OUT 403
STA Q6	OUT 403
LMW AG	JPL RC
BAD CB	LMW AC
STA Q1	BAD CB
LMW CB	STA Y1
EIR	LMW AV
Q1 LDX **	STA Y6
SUB FX	LMW A5
TH ARS 3	STA Y2
SUB UN	LMW CB
TZE Q2	EIR
SUB UN	Y1 LDX **
TZE Q3	JPL OV
SUB UN	TSW 11
TZE Q4	TOV Y3
LDA T3	JPL S4
JPL S3	JMP Y5
JMP Q5	Y3 SWL 2
Q2 LDA UN	Y2 MPY **
JPL S3	ARS 3
JMP Q5	Y6 ADD **
Q3 LDA T1	JPL S2
JPL S3	LMW Y6
JMP Q5	BAD Y3
Q4 LDA T2	STA Y6
JPL S3	LMW Y2
Q5 OUT 423	BAD Y3
TXH Q1	STA Y2
Q6 JMP **	SWL 1
S3 ALS 21	Y5 OUT 423
OTY	TXH Y1
JMP V6	ZX JMP CP
RC LMW AC	S4 TMI V1
BAD CB	JMP V2
STA C1	V1 OUT 400
LMW AG	V2 ALS 21
BAD CB	OTY
STA G1	OUT 41L
LMW CB	TZE *+7
EIR	V6 ALS 1
LDA CL	OTY
OPP	ALS 1
IDP	OTY
G1 LDX **	ALS 1
OPP	OTY
IDP	RTN
C1 CPX **	CN LMW CB
TXH G1	EIR
RTN	LDA AA
CH ELA	N1 CPY BB
STA N2	JPL S1
OUT 403	OUT 423
OUT 403	LDA BB
BCI CHANNEL READINGS.	ADD UN
OUT 403	TXH N1


```

OUT 403
OUT 403
N2 JMP **
S2 CPY EE
EIR
STA BB
LMW 02
BLS
EIR
LDA EE
TMI V3
JMP V4
V3 OUT 400
V4 ARS 5
U1 ARS 1
TXE U2
TXH U1
U2 EIR
BRS
STA *+7
BLS
COM 1
BAD FW
EIR
LDA EE
ALS 16
ALS 0
U3 ALS 1
OTY
TXH U3
OUT 41L
U4 ALS 1
TZE U5
OTY
JMP U4
U5 LMW BB
EIR
RTN
JC JPL **
ROT
JMP JC
H1 LDA Z0
IDK
RTN
J1 TSW 44
TOV J2
JMP J1
J2 LDA SS
OPP
IDP
AND DX
J3 TSW 44
TOV J3
RTN
IN OUT 403
OUT 403
BCI INPUT FROM SCAN OR K/BD? :
SWL 2
LMW TH
BLS
EIR
LDA Z0
I1 ALS 2
CPY EE
ITY
AND DD
ADD EE
TXH I1
AND IP
TOV I2
LMW JK
STA JL
STA JC
JMP I3
I2 LMW JS
STA JL
STA JC
I3 OUT 403
OUT 403
SWL 1
RTN
JS PZE J1
JK PZE H1
QZ PZE AV
QY PZE AS
DX HEX DDDD+
NX DEC 9999+
WY PZE R6
WZ PZE CP
IP HEX 1429+
HEX 192L+
Z0 HEX +
DD HEX +
HEX 3D+
SS HEX L000+
CL HEX 9000+
FW HEX 4+
AT HEX 8+
UN HEX 1+
T1 HEX 10+
T2 HEX 100+
T3 HEX 1000+
FO HEX 182L+
FA HEX 4000+
TT HEX 20+
TB HEX L+
EE BSS 2
CC BSS 1
CO BSS 1
BB BSS 1
CB BSS 1
FX BSS 1
AA BSS 1
AZ BSS 1
R1 ELA
STA R2
JPL CR
R2 JMP **
R3 ELA
STA R4
JPL GC
JPL GH

```

```

JPL GP
R4 JMP **
R5 ELA
  STA R7
  LMW WY
  STA ZX
  JPL CH
  JMP A4
R6 LMW WZ
  STA ZX
R7 JMP **
R8 ELA
  STA R9
  JPL FR
  JPL IN
R9 JMP **
RL ELA
  STA RA
  JPL SH
  JPL SQ
RA JMP **
OV CPY BB
  SSP
  AND NX
  TOV OL
  LDA BB
  RTN
OL OUT 403
  BCI OVERFLOW!
  OUT 403
  JMP A8
AS PZE *+4
AG PZE *+11
AC PZE *+30
AV PZE *+49

FIN

```

Off-Line Identification Program for the Model $\frac{dx}{dt} + ax = a$

```

BGN                                OUT 403
  JMP HD                            OUT 403
ZO HEX +                            OUT 403
  HEX +                             IIK
  HEX +                             E8 LMW XT
  HEX +                             STA K2
  HEX +                             LMW NP
  HEX +                             EIR
BB JMP E1                          /INPUT MATRIX.          OUT 403
CC JMP E2                          /INPUT TIME SCALE.     OUT 403
DD JMP E3                          /COMPUTE X(T).        BCI VALUES OF X(T)
EE JMP E4                          /INITIALISE STORAGE.  OUT 403
FF JMP E5                          /COMPUTE X(S).        OUT 403
GG JMP E6                          /PRINT X(S).          K1 JPL FO
HH JMP E7                          /COMPUTE AND PRINT ESTIMATED VALUES. K2 MZE **
II JMP E8                          /PRINT X(T).          OUT 403
  HEX +                             TXH *+2
HD OUT 403                          IIK
  OUT 403                          LMW K2
  BCI MODELLING TECHNIQUE TEST PROGRAM. BAD TH

```


STA K2		LDA Z0	
JMP K1		CPX **	
E6 LMW XS		TXH *-1	
STA C2		SWL 1	
LMW NP		JMP E5	
EIR		IN LMW SV	
OUT 403		EIR	
OUT 403		SWL 2	
BCI VALUES OF X(S)		LDA Z0	
OUT 403		TH IDK	
OUT 403		CPY BS+1	
C1 JPL FO		ARS 1	
C2 MZE **		TZE *+2	
OUT 403		TXH *-2	
TXH *+2		EIR	
IIK		BRS	
LMW C2		STA *+2	
BAD TH		LDA BS+1	
STA C2		ALS 0	
JMP C1		CPY BS+1	
E5 SWL 1		SWL 1	
LDA NO		LDA Z0	
CPY C0		IDK	
LMW MX		CPY BS	
STA A2		RTN	
LMW XS		E1 SWL 1	
AA STA A3		OUT 403	
STA A4		OUT 403	
LMW XT		OUT 403	
STA A1		BCI NO. OF QUADRATURE POINTS:	
LMW NP		LDA Z0	
EIR		UN IDT	
A0 JPL IT		CPY NO	
A1 LDX **	/X(T)	SUB UN	
A2 MPX **	/MATRIX	JPL BC	
MPX TS		CPY NP	
A3 ADX **	/X(S)	LDA NO	
A4 CPX **	/X(S)	ALS 23	
SWL 1		OTY	
LMW A2		ALS 1	
BAD TH		OTY	
STA A2		OUT 403	
TXH *+2		LDA NO	
JMP A5		CPY C0	
LMW A1		LMW MX	
BAD TH		STA B2	
STA A1		B0 LMW NP	
JMP A0		EIR	
A5 LDA C0		B1 JPL IT	
SUB UN		B2 SAV **	/MATRIX VALUES.
TZE E7		SWL 1	
CPY C0		LMW B2	
LMW A3		BAD TH	
BAD TH		STA B2	
JMP AA		TXH B1	
E4 SWL 6		LDA C0	
LMW FT		SUB UN	
EIR		TZE *+3	
LMW XS		CPY C0	
BAD FT		JMP B0	
STA *+2		LMW NP	

```

EIR
LMW TI
STA B4
B3 JPL IT
B4 SAV ** /TIMES.
SWL 1
TXH *+2
JMP E2
LMW B4
BAD TH
STA B4
JMP B3
BC CPY CO
ARS 1
TZE EN
SUB UN
EIR
LDA CO
BD SUB TN
BAD TB
STA CO
TXH BD
EN LMW CO
RTN
E2 OUT 403
OUT 403
BCI TIME SCALE:
JPL IN
JPL IT
LDX BS
CPX TS
SWL 1
JPL FO
MZE TS
OUT 403
E3 SWL 1
OUT 403
OUT 403
BCI INPUT TIME CONSTANT
OUT 403
OUT 403
JPL IN
JPL IT
LDX BS
CPX TC
SWL 1
LMW NP
EIR
LMW TI
STA D1
LMW XT
STA D2
CO JPL IT
D1 LDX **
MPX TS
MPX TC
CNP **
CPX BS
SWL 1
JPL EX
PZE BS
PZE BS
IIK
JPL IT
LDX UM
SUX BS
D2 CPX **
SWL 1
TXH *+2
JMP E4
LMW D1
BAD TH
STA D1
LMW D2
BAD TH
STA D2
JMP DO
E7 SWL 1
LMW XS
STA F2
LMW NP
EIR
JPL IT
LDX ZO
CPX SS
CPX ES
CPX ET
LDX UM
DVX TS
CPX UP
F1 JPL IT
LDX SS
ADX UP
CPX SS
F2 MPX **
CPX BS
SUX UM
CPX BT
LDX BS
MPX SS
MPX BT
ADX ES
CPX ES
LDX BT
MPX BT
ADX ET
CPX ET
SWL 1
TXH *+7
JPL IT
LDX ES
DVX ET
CNP **
CPX ES
JMP *+5
LMW F2
BAD TH
STA F2
JMP F1
OUT 403
OUT 403
BCI TRUE TIME CONSTANT:

```

```

JPL FO
MZE TC
OUT 403
OUT 403
BCI ESTIMATED TIME CONSTANT:
JPL FO
MZE ES
OUT 403
OUT 403
IIK
TI HEX L00+
XS HEX L30+
XT HEX L60+
MX HEX L90+
NO BSS 1
NP BSS 1
TS BSS 3
CO BSS 1
SV HEX M+
FT HEX 2L+
TN HEX 10+
TB HEX L+
SS BSS 3
BS BSS 3
TC BSS 3
UP BSS 3
ES BSS 3
ET BSS 3
BT BSS 3
UM HEX 1+
    HEX 1000+
    HEX +
IT BSS 275
FO BSS 70
EX BSS 1

```

```
FIN
```

Off-Line Identification Program for the Model $\frac{dx}{dt} + ax = b$

```

BGN
    JMP HD
ZO HEX +
    HEX +
    HEX +
    HEX +
    HEX +
    HEX +
BB JMP E1    /INPUT MATRIX.
CC JMP E2    /INPUT TIME SCALE.
DD JMP E3    /COMPUTE X(T).
EE JMP E4    /INITIALISE STORAGE.
FF JMP E5    /COMPUTE X(S).
GG JMP E6    /PRINT X(S).
HH JMP E7    /COMPUTE AND PRINT ESTIMATED VALUES.
II JMP E8    /PRINT X(T).
    HEX +
HD OUT 403
    OUT 403

```

BCI MODELLING TECHNIQUE TEST PROGRAM.

```

OUT 403
OUT 403
OUT 403
IIK
E8 LMW XT
STA K2
LMW NP
EIR
OUT 403
OUT 403
BCI VALUES OF X(T).
OUT 403
OUT 403
K1 JPL F0
K2 MZE **
OUT 403
TXH *+2
IIK
LMW K2
BAD TH
STA K2
JMP K1
E6 LMW XS
STA C2
LMW NP
EIR
OUT 403
OUT 403
BCI VALUES OF X(S)
OUT 403
OUT 403
C1 JPL F0
C2 MZE **
OUT 403
TXH *+2
IIK
LMW C2
BAD TH
STA C2
JMP C1
E5 SWL 1
LDA NO
CPY CO
LMW MX
STA A2
LMW XS
AA STA A3
STA A4
LMW XT
STA A1
LMW NP
EIR
AO JPL IT
A1 LDX ** /X(T)
A2 MPX ** /MATRIX
MPX TS
A3 ADX ** /X(S)
A4 CPX ** /X(S)
SWL 1
LMW A2
BAD TH
STA A2
TXH *+2
JMP A5
LMW A1
BAD TH
STA A1
JMP A0
A5 LDA CO
SUB UN
TZE E7
CPY CO
LMW A3
BAD TH
JMP AA
E4 SWL 6
LMW FT
EIR
LMW XS
BAD FT
STA *+2
LDA Z0
CPX **
TXH *-1
SWL 1
JMP E5
IM LMW SV
EIR
SWL 2
LDA Z0
TH IDK
CPY BS+1
ARS 1
TZE *+2
TXH *-2
EIR
BRS
STA *+2
LDA BS+1
ALS 0
CPY BS+1
SWL 1
LDA Z0
IDK
CPY BS
RTN
E1 SWL 1
OUT 403
OUT 403
OUT 403
BCI NO. OF QUADRATURE POINTS:
LDA Z0
UN IDT
CPY NO
SUB UN
JPL BC
CPY NP
LDA NO
ALS 23

```

OTY
 ALS 1
 OTY
 OUT 403
 LDA NO
 CPY CO
 LMW MX
 STA B2
 B0 LMW NP
 EIR
 B1 JPL IT
 B2 SAV ** /MATRIX VALUES.
 SWL 1
 LMW B2
 BAD TH
 STA B2
 TXH B1
 LDA CO
 SUB UN
 TZE *+3
 CPY CO
 JMP BO
 LMW NP
 EIR
 LMW TI
 STA B4
 B3 JPL IT
 B4 SAV ** /TIMES.
 SWL 1
 TXH *+2
 JMP E2
 LMW B4
 BAD TH
 STA B4
 JMP B3
 BC CPY CO
 ARS 1
 TZE EN
 SUB UN
 EIR
 LDA CO
 BD SUB TN
 BAD TB
 STA CO
 TXH BD
 EN LMW CO
 RTN
 E2 OUT 403
 OUT 403
 BCI TIME SCALE:
 JPL IN
 JPL IT
 LDX BS
 CPX TS
 SWL 1
 JPL FO
 MZE TS
 OUT 403
 E3 SWL 1
 OUT 403

OUT 403
 BCI INPUT TIME CONSTANTS!
 OUT 403
 OUT 403
 JPL IN
 JPL IT
 LDX BS
 CPX TC
 SWL 1
 JPL IN
 JPL IT
 LDX BS
 CPX TD
 SWL 1
 LMW NP
 EIR
 LMW TI
 STA D1
 LMW XT
 STA D2
 D0 JPL IT
 D1 LDX **
 MPX TS
 MPX TC
 CNP **
 CPX BS
 SWL 1
 JPL EX
 PZE BS
 PZE BS
 IIK
 JPL IT
 LDX UM
 SUX BS
 DVX TC
 MPX TD
 D2 CPX **
 SWL 1
 TXH *+2
 JMP E4
 LMW D1
 BAD TH
 STA D1
 LMW D2
 BAD TH
 STA D2
 JMP DO
 E7 SWL 1
 LMW XS
 STA F2
 STA F3
 LMW NP
 EIR
 JPL IT
 LDX ZO
 CPX SS
 CPX BS
 CPX BT
 CPX BU
 CPX BW

	CPX BV	MZE TC
	LDX UM	OUT 403
	DVX TS	JPL FO
	CPX UP	MZE TD
F1	JPL IT	OUT 403
	LDX SS	OUT 403
	ADX UP	BCI ESTIMATED TIME CONSTANTS:
	CPX SS	OUT 403
F2	MPX **	OUT 403
	CPX BZ	JPL FO
	ADX BS	MZE ES
	CPX BS	OUT 403
	LDX BZ	JPL FO
	MPX SS	MZE ET
	CPX BZ	OUT 403
	ADX BT	OUT 403
	CPX BT	IJK
	LDX BZ	TI HEX 100+
F3	MPX **	XS HEX 130+
	CPX BZ	XT HEX 160+
	ADX BU	MX HEX 190+
	CPX BU	NO BSS 1
	LDX BZ	NP BSS 1
	MPX SS	TS BSS 3
	ADX BV	CO BSS 1
	CPX BV	SV HEX M+
	LDX BW	FT HEX 2L+
	ADX UM	TN HEX 10+
	CPX BW	TB HEX L+
	SWL 1	SS BSS 3
	TXH *+19	BS BSS 3
	JPL IT	TC BSS 3
	LDX BS	TD BSS 3
	MPX BX	BU BSS 3
	DVX BW	BV BSS 3
	CNP **	BW BSS 3
	ADX BU	BZ BSS 3
	CPX BZ	UP BSS 3
	LDX BS	ES BSS 3
	MPX BT	ET BSS 3
	DVX BW	BT BSS 3
	SUX BV	UM HEX 1+
	DVX BZ	HEX 1000+
	CPX ES	HEX +
	MPX BS	IT BSS 275
	ADX BT	FO BSS 70
	DVX BW	EX BSS 1
	CPX ET	
	JMP *+6	FIN
	LMW F2	
	BAD TH	
	STA F2	
	STA F3	
	JMP F1	
	OUT 403	
	OUT 403	
	BCI TRUE TIME CONSTANTS:	
	OUT 403	
	OUT 403	
	JPL FO	

On-Line Identification Program

BGN		TW SWL 2	
	JMP *+10	A2 MPX **	
Z0	HEX +	ARS 5	
	HEX +	MPY TF	/TIME FACTOR.
	HEX +	ARS 7	
	HEX +	A3 ADX **	
	HEX +	A4 CPX **	
	HEX +	SWL 1	
	JMP QU	/QUADRATURE INFORMATION. LDA CX	
	JMP CU	/CHANNEL INFORMATION. TZE *+2	
	JMP AA	JPL XX	
	SWL 1	SWL 2	
	OUT 403	TXH A0	
	BC1 MODEL PREDICTION PROGRAM.	SWL 1	
	OUT 403	LMW A1	
	OUT 403	BAD UN	
	OUT 403	STA A1	
	JMP QU	LDA NO	
AA	JPL ZZ	SUB UN	
	TSW 22	TZE *+5	
	TOV *+2	CPY NO	
	JMP *-2	LMW A3	
	TSW II	BAD NT	
	TOV *+2	JMP A5	
	JMP C2	LDA NN	
	LDA CC	ADD UN	
	OPP	CPY NN	
	LDA Z0	SUB NP	
	IDP	TZE CN	
C1	CPY CB	LMW A2	
	LDA CC	BAD NT	
	OPP	STA A2	
	LDA Z0	JPL T1+9	
	IDP	JMP A6	
	CPY BB	ZZ ELA	
	SUB CB	STA Z2	
	SSP	LMW NB	
	SUB SB	ELA	
	TMI *+2	LMW NR	
	JMP C2	BAD VV	
	LDA BB	STA Z5	
	JMP C1	LMW NR	
C2	JPL T1	EIR	
	LMW MM	Z4 SWL 2	
	BAD NR	LDA Z0	
	STA A2	Z5 CPX **	
	LMW DA	TXH Z5	
	STA A1	ELA	
A6	LDA NC	EIR	
	CPY NO	SWL 1	
	LMW VV	TXH *+2	
	BAD NR	JMP TH	
A5	STA A3	LMW Z5	
	STA A4	BAD NT	
	LMW NR	STA Z5	
	EIR	EIR	
A0	SWL 1	ELA	
A1	LDA **	JMP Z4-2	
		TH SWL 3	

LDA Z0
 CPY SC
 SWL 1
 LDA N1
 ADD WT
 CPY CH
 LMW DA
 STA DB
 Z3 LMW TI
 STA TJ
 STA *+1
 LDA **
 CPY CX
 Z2 JMP **
 QU SWL 1
 LDA Z0
 CPY SW
 TSW 88
 TOV *+3
 LDA UN
 CPY SW
 LDA SW
 TZE *+4
 TSW 88
 TOV *+4
 JMP *-2
 TSW 88
 TOV *-1
 OUT 403
 BCI NO. OF QUADRATURE POINTS:
 LDA Z0
 JPL IN /INPUT ROUTINE.
 CPY NP
 JPL PR /PRINTOUT ROUTINE.
 OUT 403
 OUT 403
 OUT 403
 LDA NP
 SUB UN
 JPL BC /BINARY CONVERSION.
 STA NQ
 BLS
 STA NR
 LDA NP
 JPL BC
 BLS
 STA NT
 LMW NR
 BAD MM
 STA Q1
 LMW NR
 STA IR
 LMW NR
 EIR
 SWL 2
 LDA Z0
 JPL IN
 Q1 CPX ** /MATRIX
 TXH *-3
 LMW IR

EIR
 TXH *+2
 JMP *+7
 EIR
 STA IR
 LMW Q1
 BAD NT
 STA Q1
 JMP Q1-5
 SWL 1
 LMW NQ
 BAD TI
 STA Q2
 LMW NQ
 EIR
 LDA Z0
 JPL IN
 Q2 CPX ** /TIMES.
 TXH Q2-2
 IIK
 CU OUT 403
 BCI FIRST CHANNEL NO.:
 SWL 1
 LDA Z0
 JPL IN
 CPY N1
 JPL PR
 OUT 403
 OUT 403
 BCI LAST CHANNEL NO.:
 LDA Z0
 JPL IN
 CPY N2
 JPL PR
 LDA N2
 SUB N1
 ADD UN
 CPY NC
 SUB UN
 JPL BC
 STA NB
 SWL 2
 OUT 403
 OUT 403
 BCI TIME FACTOR:
 LDA Z0
 JPL IN
 CPY S0
 DEC 2+
 MZE TF
 HEX 6+
 OUT 403
 OUT 403
 BCI TIME CORRECTION FACTOR:
 LDA Z0
 JPL IN
 CPY TC
 JPL S0
 DEC 2+
 MZE TC

HEX 6+
 OUT 403
 SWL 1
 TSW 11
 TOV *+2
 JMP AA
 OUT 403
 OUT 403
 OUT 403
 BCI CONTROL CHANNEL NO.:
 LDA ZO
 JPL IN
 CPY BB
 JPL PR
 LDA BB
 ADD WT
 CPY CC
 OUT 403
 OUT 403
 BCI CONTROL SIGNAL INITIATE AMPLITUDE:
 LDA ZO
 JPL IN
 CPY BB
 JPL PR
 LDA BB
 CPY SB
 OUT 403
 OUT 403
 OUT 403
 CT JMP AA
 T1 LDA CL
 OPP
 LDA CO
 ADD UN
 CPY CO
 IDP
 ARS 4
 SUB CX
 TZE RC
 LDA SC
 SUB NN
 TZE T1
 TMI *+2
 RTN
 OUT 403
 BCI SCAN ERROR.
 OUT 403
 IIK
 RC LDA ZO
 CPY CO
 LMW DB
 BAD NB
 STA R2
 LMW NB
 EIR
 R1 LDA CH
 OPP
 ADD UN
 CPY CH
 IDP
 R2 CPX **

TXH R1
 LDA SC
 ADD UN
 CPY SC
 SUB NP
 TZE R3
 LMW DB
 BAD UN
 BAD NB
 STA DB
 LMW TJ
 BAD UN
 STA TJ
 STA *+1
 LDA **
 CPY CX
 LDA N1
 ADD WT
 CPY CH
 JMP T1
 R3 LDA ZO
 CPY CX
 RTN
 XX ELA
 STA *+6
 EIR
 STA IR
 JPL T1
 LMW IR
 EIR
 JMP **
 IN TSW 44
 TOV *+3
 IDT
 RTN
 IDK
 RTN
 PR CPY BB
 LMW TH
 EIR
 LDA BB
 ARS 1
 TZE *+2
 TXH *-2
 EIR
 STA *+6
 COM 1
 BAD TH
 EIR
 OUT 413
 LDA BB
 ALS 0
 ALS 20
 ALS 1
 OTY
 TXH *-2
 RTN
 BC CPY BB
 ARS 1
 TZE EN
 SUB UN

EIR
 LDA BB
 BD SUB TN
 BAD TB
 STA BB
 TXH BD
 EN LMW BB
 RTN
 VV HEX SL7+
 MM HEX CM5+
 DA HEX LC9+
 TI HEX LLL+
 CL DEC 9000+
 WT DEC 1000+
 TN DEC 10+
 TB HEX L+
 UN HEX 1+
 SW BSS 1
 BB BSS 1
 CC BSS 1
 CB BSS 1
 NP BSS 1
 NQ BSS 1
 NR BSS 1
 NT BSS 1
 CH BSS 1
 N1 BSS 1
 N2 BSS 1
 NC BSS 1
 NB BSS 1
 SB BSS 1
 IR BSS 1
 NO BSS 1
 SC BSS 1
 NN BSS 1
 CO BSS 1
 DB BSS 1
 CX BSS 1
 TJ BSS 1
 TC BSS 2
 TF BSS 2
 SO BSS 77
 CN IIK 77

FIN

Parameter Estimation Routine for the On-Line Identification Program.

Model: $\frac{dx}{dt} + ax = a$

BGN

TW SWL 2
 LDA TC
 ALS 2
 JPL FL /FLOAT ROUTINE.
 PZE F1
 SWL 2
 LDA TF

/FLOATING POINT INTERPRETER.

/FLOATING POINT OUTPUT.

ALS 2
 JPL FL
 PZE F2
 JPL IT
 LDX UM
 DVX F2
 CPX F3
 SWL 1
 LMW NB
 STA IR
 LMW VV
 STA L1
 LMW TK
 LD STA L3
 STA L4
 TH SWL 3
 LDA ZO
 CPY SS
 CPY BU
 CPY BV
 LO LMW NQ
 EIR
 SWL 2
 L1 LDA **
 ALS 2
 JPL FL
 PZE FB
 JPL IT
 LDX SS
 ADX F3
 CPX SS
 MPX FB
 CPX BT
 MPX SS
 MPX BT
 CPX BS
 LDX BT
 MPX SS
 SUX BS
 ADX BU
 CPX BU
 LDX BT
 MPX TU
 SUX UM
 CPX BS
 LDX BT
 MPX BT
 SUX BS
 MPX F1
 ADX BV
 CPX BV
 SWL 1
 LMW L1
 BAD TW
 STA L1
 TXH LO+2
 JPL IT
 LDX BU
 DVX BV
 L3 CPX **

SWL 1
 JPL FO
 L4 MZE **
 OUT 403
 LMW IR
 EIR
 TXH *+5
 OUT 403
 OUT 403
 OUT 403
 IIK
 EIR
 STA IR
 LMW L3
 BAD TH
 JMP LD
 VV HEX SL7+
 UM HEX 1+
 HEX 1000+
 HEX +
 TU HEX 1+
 HEX 2000+
 HEX +
 BU BSS 3
 TK HEX L82+
 BV BSS 3
 BS BSS 3
 BT BSS 3
 F1 BSS 3
 F2 BSS 3
 F3 BSS 3
 FB BSS 3
 SS BSS 3
 IR NSS 1
 FO BSS 70
 IT BSS 270
 FL NSS 1
 ZO SYN 1
 NQ SYN 23D
 NB SYN 246
 TF SYN 252
 TC SYN 250

FIN

On-line Monitor Program (Single Cycle)

```

BGN
  JMP AR
ZO HEX +
  HEX +
  HEX +
UN HEX 1+
JJ BSS 1
  JMP AZ      /INPUT SCAN INFORMATION
  JMP P1      /READ DATA
  JMP P2      /HEAD DATA TAPE
  JMP P3      /PUNCH DATA
  JMP P5      /END DATA TAPE
  JMP P6      /STOP CODE
AR OUT 403
  BCI DATA LOGGER SCANNER
  OUT 403
  OUT 403
  OUT 403
  IIK
AZ SWL 1
  BCI DATA VALUES PER CHANNEL:
  LDA ZO
  TH IDK
  CPY NN
  JPL PR
  OUT 403
  OUT 403
  BCI NO. OF CHANNELS:
  LDA ZO
  IDK
  CPY NC
  JPL PR
  OUT 403
  OUT 403
  BCI FIRST CHANNEL:
  LDA ZO
  IDK
  CPY CC
  JPL PR
  LDA CC
  ADD TX
  CPY CC
  OUT 403
  OUT 403
  OUT 403
  OUT 403
  IIK
P1 SWL 1
  LDA NN
  CPY CO
  LDA NC
  JPL BC
  STA NB
  LDA NC
  SUB UN
  JPL BC
  STA IR
  EIR
  LMW S1
  BAD IR
  STA A4
  LDA CC
  CPY CM
  JPL CR
  CPY CD
  JPL CR
  AND DD
  SUB CD
  SSP
  SUB TN
  TMI *-5
  JMP A7
CR LDA CC
  OPP
  IDP
  RTN
A7 LDA CL
  OPP
  IDP
A6 LDA CM
  OPP
  ADD UN
  CPY CM
  IDP
A4 CPX **
  TXH A6
  LDA CO
  SUB UN
  TZE P1-1
  CPY CO
  LMW A4
  BAD NB
  STA A4
  LDA CC
  CPY CM
  LMW IR
  EIR
  JMP A7
P2 SWL 3
  LMW F1
  EIR
  LDA ST
  OPB
  ARS 2
  TXH *-2
  SWL 1
  LDA ZO
  IDK
  TMI *+3
  OPB
  JMP *-4
  LDA NL
  OPB
  LMW FI
  EIR
  LDA ZO

```

	OPB		RTN
	TXH *-1	PR	ALS 21
	IIK		OTY
P3	SWL 1		ALS 1
	LDA NN		OTY
	MPY NC		ALS 1
	CPY CO		OTY
	LMW S1		ALS 1
	STA A2		OTY
	STA A3		RTN
A2	LDA **	BC	CPY JJ
	TMI *+2		ARS 1
	JMP *+3		TZE EN
	LDA SN		SUB UN
	OPB		EIR
	LMW UN		LDA JJ
	EIR	BD	SUB TN
	LDA NP		BAD NL
	OPB		STA JJ
	ARS 2		TXH BD
	TXH *-2	EN	LMW JJ
	LMW TH		RTN
	EIR	TN	DEC 10+
A1	EIR	TX	HEX 1000+
	STA *+3	NN	BSS 1
	EIR	NC	BSS 1
A3	LDA **	IR	BSS 1
	ARS 0	CC	BSS 1
	AND FI	NB	BSS 1
	BAD AD	CO	BSS 1
	STA *+1	CM	BSS 1
	LDA **	CD	BSS 1
	OPB	CL	HEX 9000+
	TXH A1	ST	HEX 5LS4+
	JPL ZZ		HEX LOA3+
	LDA CO		HEX AD44+
	SUB UN	NP	HEX 2M30+
	TZE P5+7	DD	HEX DDDD+
	CPY CO	NL	HEX L+
	LMW A2	FI	HEX D+
	BAD UN	SN	HEX 25+
	STA A2	SC	HEX 84+
	STA A3	SP	HEX LO+
	JMP A2	TL	HEX OLOL+
P5	SWL 3		HEX LLLL+
	LMW FI		HEX LLLL+
	EIR	AD	PZE *+1
	LDA TL		HEX 30+
	OPB		HEX CI+
	ARS 2		HEX C2+
	TXH *-2		HEX 33+
	IIK		HEX C4+
P6	LMW SC		HEX 35+
	OPB		HEX 36+
	IIK		HEX C7+
ZZ	LMW UN		HEX C8+
	EIR		HEX 39+
	LDA SP	SI	PZE *+1
	OPB		
	TXH *-1		FIN

On-Line Monitor Program (Repetitive Operation)

BGN		LMW QS
JMP AR		BAD ST
ZO HEX +		STA *+1
HEX +		LDA **
HEX +		TZE R6
UN HEX 1+		CPY SQ
HEX +		LMW QS
JMP AZ	/INPUT SCAN INFORMATION.	BAD TI
JMP P2	/HEAD DATA TAPE.	STA *+1
JMP P5	/END DATA TAPE.	LMW **
JMP P6	/STOP CODE.	STA R4+3
JMP P3	/CONTROL PROGRAM.	SWL 2
JMP P8	/COUNTER SET.	LMW QU
AR OUT 403		EIR
BCI DATA LOG-GER SCANNER (MOD.).		LDA ZO
OUT 403		CPX TT+28
OUT 403		TXH *-1
OUT 403		R4 SWL 2
IIK		LMW QU
P3 SWL 1		EIR
LDA ZO		LDX **
IDK		ADX TT+28
CPY B0		CPX TT+28
P7 JPL YY		TXH *-3
LDA LG		LMW QU
OPP		EIR
LDA ZO		R3 LDX TT+28
FY IDP		CPY BS
TMI P7		ARS 4
JPL YY		ALS 4
JPL P1	/READ DATA.	SUB BS
LMW LG		ADD FV
EIR		TMI *+4
LDA ZO		TZE *+3
OPB		LDA BS
TXH *-1		JMP *+3
JPL CO	/SORT AND PUNCH DATA.	LDA BS
LDA B0		ADD UN
SUB UN		ARS 4
TZE *+3		JPL EC
CPY B0		CPY JJ
JMP P7		LDA ZO
IIK		CPY BS
YY LDA CL		LMW NC
OPP		AND UN
IDP		TZE *+3
RTN		LDA JJ
CO ELA		CPY BS
STA R9		LMW NC
SWL 1		BRS
LDA UN		TZE *+3
CPY QS		LDA JJ
R1 LDA QS		BLS
MPY TH		BAD BS
CPY QT		CPX SU+14
SUB UN		SWL 2
JPL EC		EIR
BLS		BLS
STA QU		EIR

TXH R3
 SWL 1
 LMW QU
 BRS
 8 STA IR
 EIR
 LDX SU+14
 BAD S1
 STA R5+2
 STA R7
 LMW NB
 5 STA JR
 EIR
 LDX **
 TMI *+2
 JMP *+3
 LDA SN
 OPB
 LMW UN
 EIR
 LDA NP
 OPB
 ARS 2
 TXH *-2
 LMW TH
 EIR
 A1 EIR
 STA *+4
 LMW JR
 EIR
 R7 LDX **
 ARS 0
 AND FI
 BAD AD
 STA *+1
 LDA **
 OPB
 LMW *-6
 EIR
 TXH A1
 JPL ZZ
 LMW JR
 EIR
 TXH *+2
 JMP *+3
 EIR
 JMP R5
 LMW IR
 EIR
 TXH *+2
 JMP *+3
 EIR
 JMP R8
 LDA SQ
 SUB UN
 TZE *+3
 CPY SQ
 JMP R4
 R6 LDA QS
 ADD UN

CPY QS
 SUB FY
 TMI R1
 TZE R1
 R9 JMP **
 SQ BSS 1
 P8 SWL 1
 LDA UN
 CPY QS
 LMW QS
 BAD ST
 STA P9+2
 STA P9+4
 LMW QS
 BAD TI
 STA *+1
 LMW **
 STA P9
 TOV *+1
 LDA NN
 ALS 4
 SWL 2
 P9 DVP **
 SWL 1
 CPY **
 JPL PU
 PZE **
 LDA QS
 ADD UN
 CPY QS
 SUB FY
 TMI P8+3
 TZE P8+3
 IIK
 ST PZE *
 BSS 5
 PU ELA 5
 STA A2+3
 BAD UN
 STA A3
 LMW TH
 EIR
 A2 EIR
 STA *+5
 EIR
 LMW **
 STA *+1
 LDA **
 ARS 0
 AND FI
 BAD AD
 STA *+1
 LDA **
 OPB
 TXH A2
 JPL ZZ
 A3 JMP **
 EC SWL 1
 CPY JJ
 LMW TH
 EIR

/NO. OF SETS.

STA IR
 LDA ZO
 CPY VL
 LDA JJ
 ARS 1
 TZE *+2
 TXH *-2
 EIR
 COM 1
 BAD TH
 ED STA JR
 STA *+2
 LDA JJ
 ARS 0
 AND FI
 TZE *+11
 SUB UN
 EIR
 LMW JR
 BAD S2
 STA *+2
 LDA ZO
 BAD **
 TXH *-1
 BAD VL
 STA VL
 LMW JR
 EIR
 TXH *+2
 JMP *+3
 EIR
 JMP ED
 LMW IR
 BRS
 EIR
 LMW VL
 RTN
 AZ SWL 1
 BCI DATA VALUES PER CHANNEL:
 LDA ZO
 TH IDK
 CPY NN
 JPL PR
 OUT 403
 OUT 403
 BCI NO. OF CHANNELS:
 LDA ZO
 IDK
 CPY NC
 JPL PR
 OUT 403
 OUT 403
 BCI FIRST CHANNEL:
 LDA ZO
 IDK
 CPY CC
 JPL PR
 LDA CC
 ADD TX
 CPY CC

OUT 403
 OUT 403
 OUT 403
 OUT 403
 IIK
 P1 SWL 1
 ELA
 STA EF
 LDA NN
 CPY CO
 LDA NC
 SUB UN
 STA NB
 LDA NC
 SUB UN
 JPL EC
 STA IR
 EIR
 LMW S1
 BAD UN
 BAD IR
 STA A4
 LDA CC
 CPY CM
 JPL CR
 CPY CD
 JPL CR
 AND DD
 SUB CD
 SSP
 SUB TN
 TMI *-5
 JMP A7
 CR LDA CC
 OPP
 IDP
 RTN
 A7 LDA CL
 OPP
 IDP
 A6 LDA CM
 OPP
 ADD UN
 CPY CM
 IDP
 A4 CPX **
 TXH A6
 LDA CO
 SUB UN
 EF TZE **
 CPY CO
 LMW A4
 BAD NC
 STA A4
 LDA CC
 CPY CM
 LMW IR
 EIR
 JMP A7
 P2 SWL 3

LMW	FI	DD	HEX	DDDD+
EIR		NL	HEX	L+
LDA	SZ	FI	HEX	D+
OPB		SN	HEX	25+
ARS	2	SC	HEX	84+
TXH	*-2	SP	HEX	L0+
SWL	1	TL	HEX	010L+
LDA	Z0		HEX	LLLL+
IDK			HEX	LLLL+
TMI	*+3	AD	PZE	*+1
OPB			HEX	30+
JMP	*-4		HEX	C1+
LDA	NL		HEX	C2+
OPB			HEX	33+
LMW	FI		HEX	C4+
EIR			HEX	35+
LDA	Z0		HEX	36+
OPB			HEX	C7+
TXH	*-1		HEX	C8+
IIK			HEX	39+
5 SWL	3	TT	BSS	30
LMW	FI	SU	BSS	15
EIR		JJ	BSS	1
LDA	TL	QS	BSS	1
OPB		QT	BSS	1
ARS	2	QU	BSS	1
TXH	*-2	JR	BSS	1
IIK		VL	BSS	1
6 LMW	SC	BS	BSS	2
OPB		LG	HEX	1035+
IIK		FV	HEX	+
Z LMW	UN		HEX	5000+
EIR		S2	PZE	*+1
LDA	SP		HEX	1+
OPB			HEX	L+
TXH	*-1		HEX	64+
RTN			HEX	3M7+
PR ALS	21	TI	PZE	*
OTY			PZE	K1
ALS	1		PZE	K2
OTY			PZE	K3
ALS	1		PZE	K4
OTY			PZE	K5
ALS	1		HEX	1+
OTY			HEX	+
RTN			HEX	5+
			HEX	7968+
FN DEC	10+	K1	HEX	18+
FX HEX	1000+		HEX	2566+
NN BSS	1		HEX	1+
NC BSS	1		HEX	+
ER BSS	1		HEX	5+
CC BSS	1		HEX	4035+
NB BSS	1		HEX	13+
CO BSS	1		HEX	9499+
BO BSS	1		HEX	28+
CM BSS	1		HEX	1172+
CD BSS	1		HEX	51+
EL HEX	9000+		HEX	6921+
SZ HEX	5LS4+	K2	HEX	98+
	HEX		HEX	6469+
	HEX		HEX	1+
NP HEX	2M30+		HEX	+

HEX 5+
 HEX 3303+
 HEX 13+
 HEX 3862+
 HEX 25+
 HEX 6916+
 HEX 43+
 HEX 1921+
 HEX 67+
 HEX 6149+
 HEX 102+
 HEX 4077+
 HEX 155+
 HEX 8590+
 3 HEX 257+
 HEX 9877+
 HEX 1+
 HEX +
 HEX 5+
 HEX 3040+
 HEX 13+
 HEX 1962+
 HEX 24+
 HEX 9515+
 HEX 41+
 HEX 0193+
 HEX 62+
 HEX 0986+
 HEX 89+
 HEX 2863+
 HEX 124+
 HEX 3518+
 HEX 170+
 HEX 3979+
 HEX 233+
 HEX 4701+
 HEX 327+
 HEX 9827+
 4 HEX 505+
 HEX 9830+
 HEX 1+
 HEX +
 HEX 5+
 HEX 2916+
 HEX 13+
 HEX 1071+
 HEX 24+
 HEX 6194+
 HEX 40+
 HEX 0952+
 HEX 59+
 HEX 9238+
 HEX 84+
 HEX 6614+
 HEX 115+
 HEX 1025+
 HEX 152+
 HEX 3936+
 HEX 198+
 HEX 3182+
 HEX 255+

HEX 6262+
 HEX 329+
 HEX 1292+
 HEX 428+
 HEX 1604+
 HEX 574+
 HEX 9115+
 K5 HEX 849+
 HEX 4474+
 SI PZE *

FIN

-Line Statistical Analysis Program.

N		JPL FO
OUT 403		MZE MN
OUT 403		OUT 403
BCI STATISTICAL CHECK.		OUT 403
OUT 403		BCI STANDARD DEVIATION:
OUT 403		JPL FO
SWL 1		MZE VA
LDA ZO		OUT 403
BCI CHANNEL COMMAND?		OUT 403
OUT 403		BCI SAMPLE SIZE:
OUT 403		JPL FO
OUT 403		MZE CO
IDK		OUT 403
CPY CH		OUT 403
SWL 3		IJK
LDA ZO		CH BSS 1
CPY CO		ZO HEX +
CPY C1		HEX +
CPY C2		HEX +
A SWL 1		CO BSS 3
LDA CH		C1 BSS 3
OPP		C2 BSS 3
LDA ZO		CC BSS 3
IDP		VA BSS 3
ALS 4		MN BSS 3
JPL FL		UM HEX 1+
PZE CC		HEX 1000+
JPL IT		HEX +
LDX CO		FL BSS 43
ADX UM		IT BSS 270
CPX CO		FO BSS 66
LDX CC		SQ BSS 1
ADX C1		
CPX C1		FIN
LDX CC		
MPX CC		
ADX C2		
CPX C2		
TSW 88		
TRA *+2		
JMP AA		
LDX C1		
DVX CO		
CPX MN		
LDX C1		
MPX C1		
DVX CO		
CPX CC		
LDX CO		
SUX UM		
CPX CO		
LDX C2		
SUX CC		
DVX CO		
CPX VA		
SWL 1		
JPL SQ		
PZE VA		
BCI MEAN:		